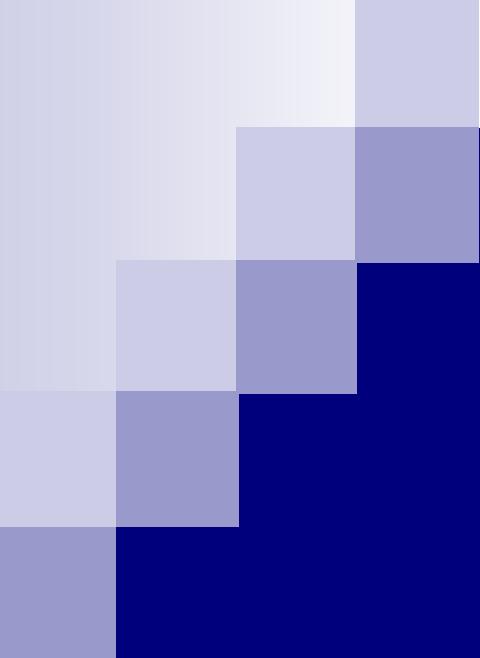


Cold Rydberg atoms



Dipole-dipole interactions with cold Rydberg atoms

*Frozen Rydberg gas
or dipole gas*

Resonant collisions (Cs: $n < 42$)

by adding a small electric field $2 \times E(np_{3/2}) = E(ns) + E((n+1)s)$

Resonant Rydberg-Rydberg atom collisions

(T.F. Gallagher et al., P.R.L. 40, 1362 (1981) with Na)

Resonant transfer of internal energy $n < 42$



Long-range dipole-dipole interaction:

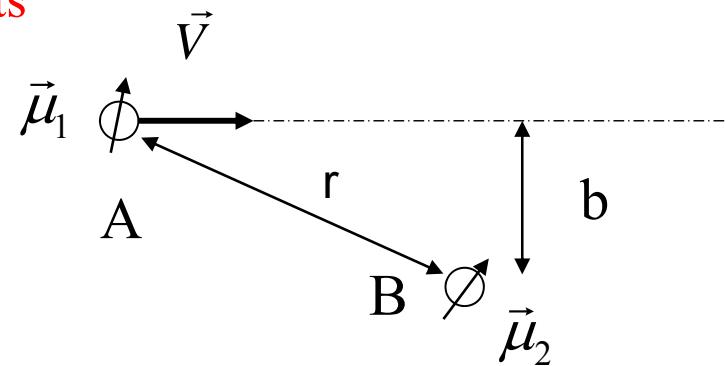
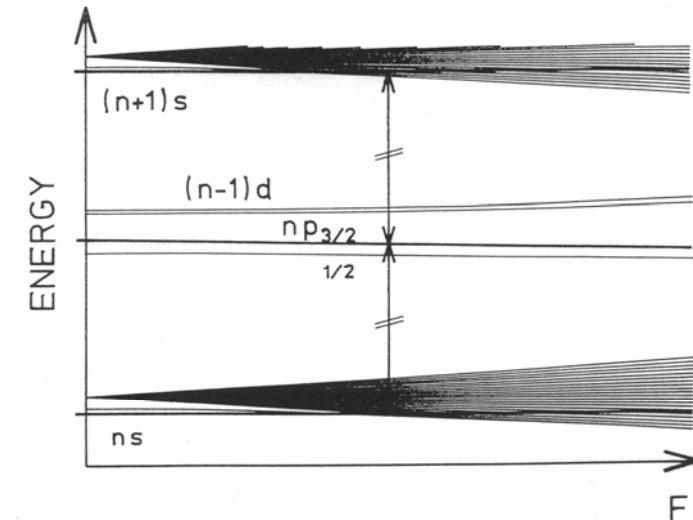
$$W = \frac{\vec{\mu}_1 \cdot \vec{\mu}_2}{r^3} - \frac{3(\vec{\mu}_1 \cdot \vec{r})(\vec{\mu}_2 \cdot \vec{r})}{r^5} \approx \frac{\mu_1 \mu_2}{r^3}$$

Characterized by huge Rydberg dipole moments

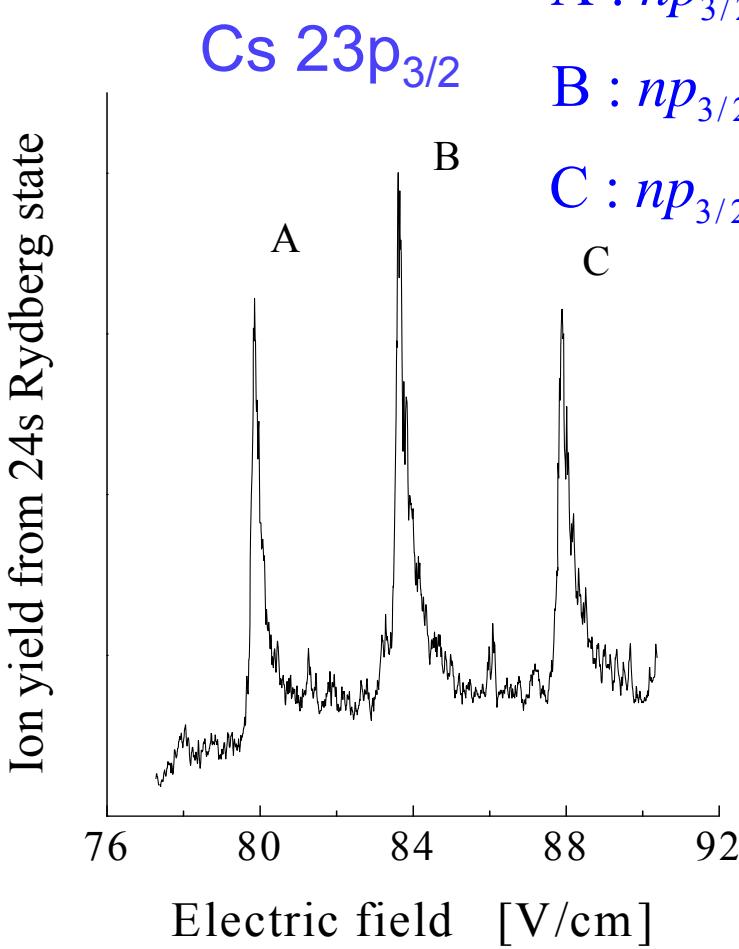
$$\langle ns | \mu_i | np \rangle \approx \langle ns | \mu_i | (n-1)p \rangle \sim n^2 \text{a.u.}$$

Characteristic time: $\tau_c \approx \frac{b}{v}$; $W_c \tau_c \sim 1$

$$\text{Impact parameter: } b \approx \sqrt{\frac{\mu_1 \mu_2}{v}}$$



Resonant collisions in an atomic beam (10 ns pulsed excitation and hot atoms)



A : $np_{3/2} |m| = 1/2 + np_{3/2} |m| = 1/2 \rightarrow ns + (n+1)s$

B : $np_{3/2} |m| = 1/2 + np_{3/2} |m| = 3/2 \rightarrow ns + (n+1)s$

C : $np_{3/2} |m| = 3/2 + np_{3/2} |m| = 3/2 \rightarrow ns + (n+1)s$

**Electric field selective
detection of ns level**

$T \approx 300 \text{ K}$, $v \approx 300 \text{ m/s}$

Huge impact parameter: $b_0 \sim 1 \mu\text{m}$

Long collision time: $\tau_C \sim 10 \text{ ns}$

The width depends of the velocity

Dipole-dipole interaction between cold Rydberg atoms (Försters resonances)

(10 ns pulsed excitation)

- Large impact parameter (40 μm) comparable to the size of the volume (300 μm): ***many-body effects?***

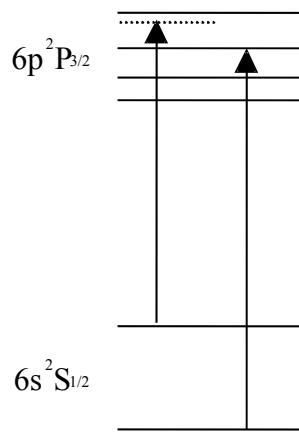
- ***No collision!***

Approximation of frozen Rydberg gas:

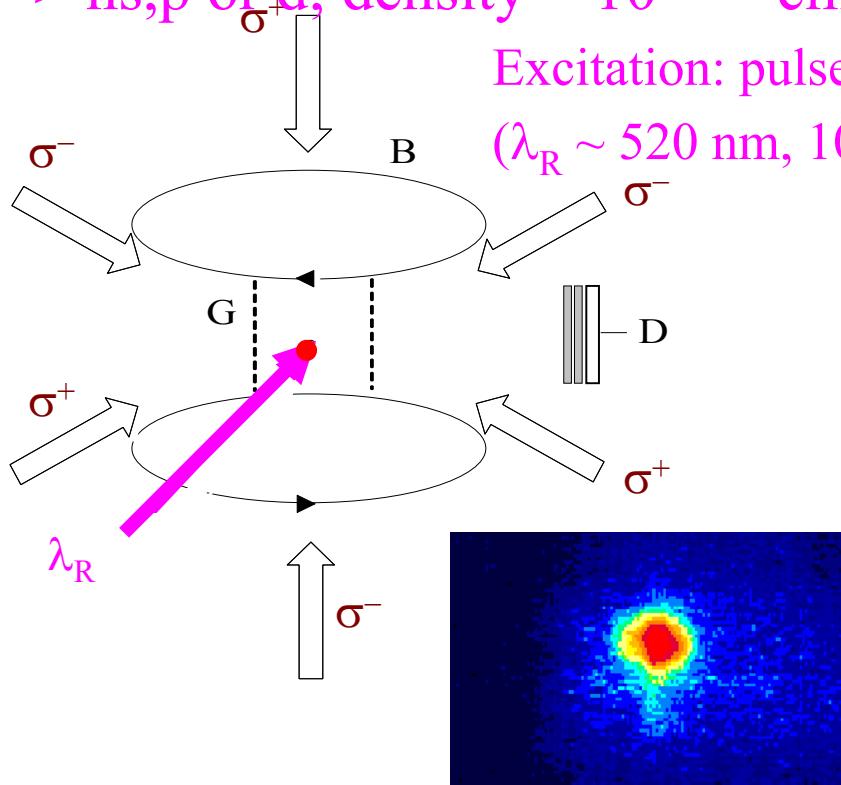
- small displacement (100 nm) of the atoms in 1 μs compared to the average distance of two atoms (5-50 μm).
- but « too long » collisionnal time (500 μs) compared to the life time (\sim a few 10 μs).

Experimental set-up: Cs (Rb) magneto-optical trap ($T \sim 20\text{-}200 \mu\text{K}$)

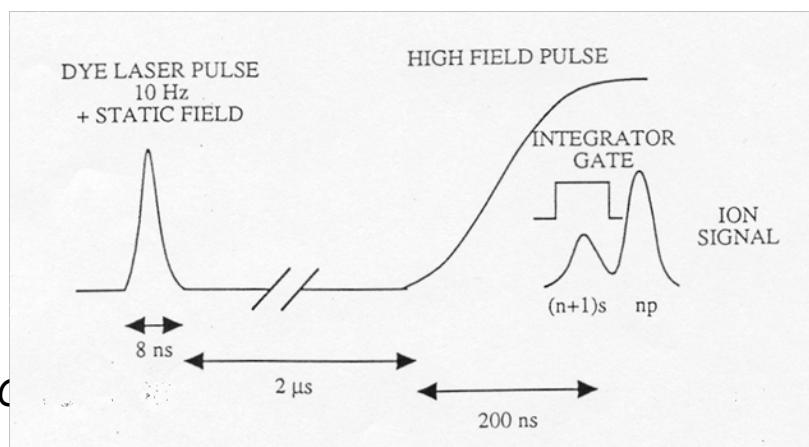
Cs(Rb) : $6(5)\text{p}_{3/2} + h\nu_R \rightarrow \text{ns, p or d}$; density $\sim 10^{7\text{-}10} \text{ cm}^{-3}$



F=5
F=4
F=3
F=2

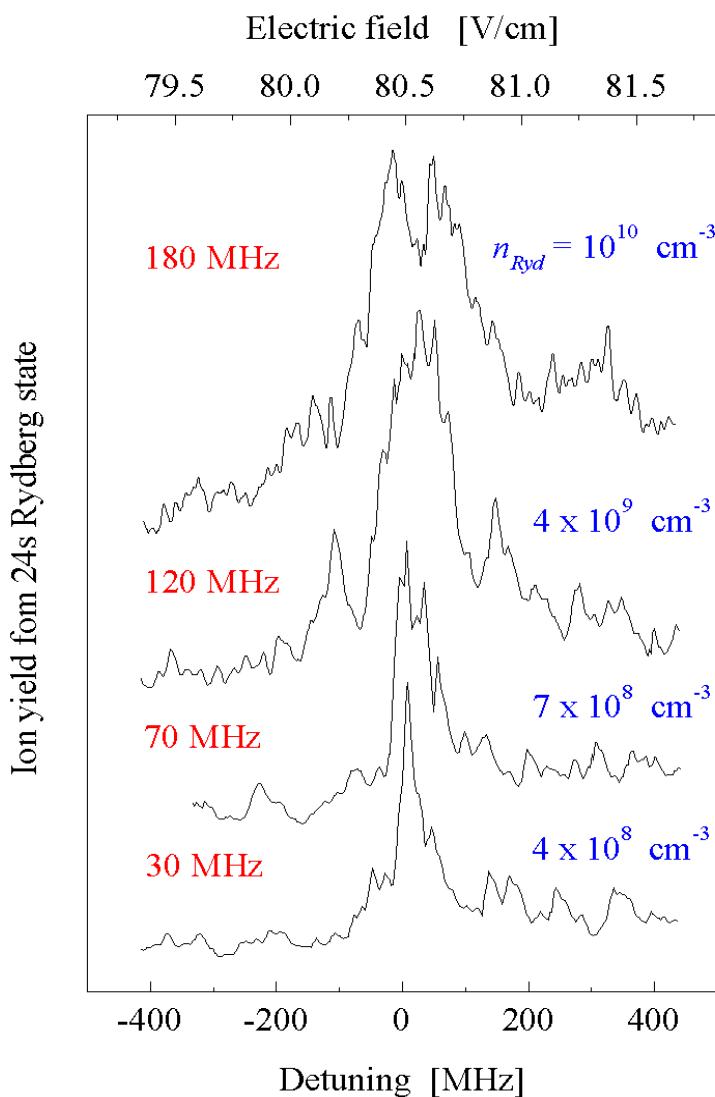


Excitation: pulsed dye-laser
($\lambda_R \sim 520 \text{ nm}, 10 \text{ Hz}$)



Selective detection
by electric-field ionization
spectroscopy &
dynamics

Dipole-dipole interactions in a frozen Rydberg gaz



$$23p_{3/2}(|m_j|=1/2) + 23p_{3/2}(|m_j|=1/2)$$

$$\rightarrow 23s + 24s$$

Population Transfer $\sim 10\text{-}15\%$

Interaction between the closest neighbors leads to a too small width: $W_{typ} \approx \frac{\mu_1 \mu_2}{\bar{R}_{AB}^3} < 1.5 \text{ MHz}$

The frozen Rydberg gas cannot be explained in the framework of two-body effects

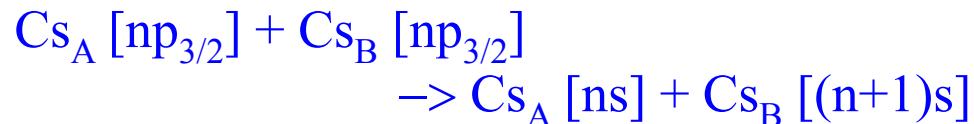
- Many-body effects in a frozen Rydberg, I. .Mourachko, D. Comparat, F . de Tomasi,, A. Fioretti, P. Nosbaum, V. Akulin et P. Pillet, Phys. Rev. Lett., 80, 253 (1998)
- Resonant dipole-dipole energy transfer in a nearly frozen Rydberg gas, W.R. Anderson, J.R. Veale, and T.F. Gallagher, Phys. Rev. Lett., 80, 249 (1998)

Many-body effects

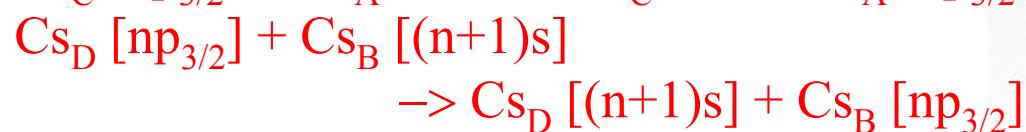
Interplay with a two-body effect and many-body phenomena

Elementary processes:

I - Resonant transfer of internal energy



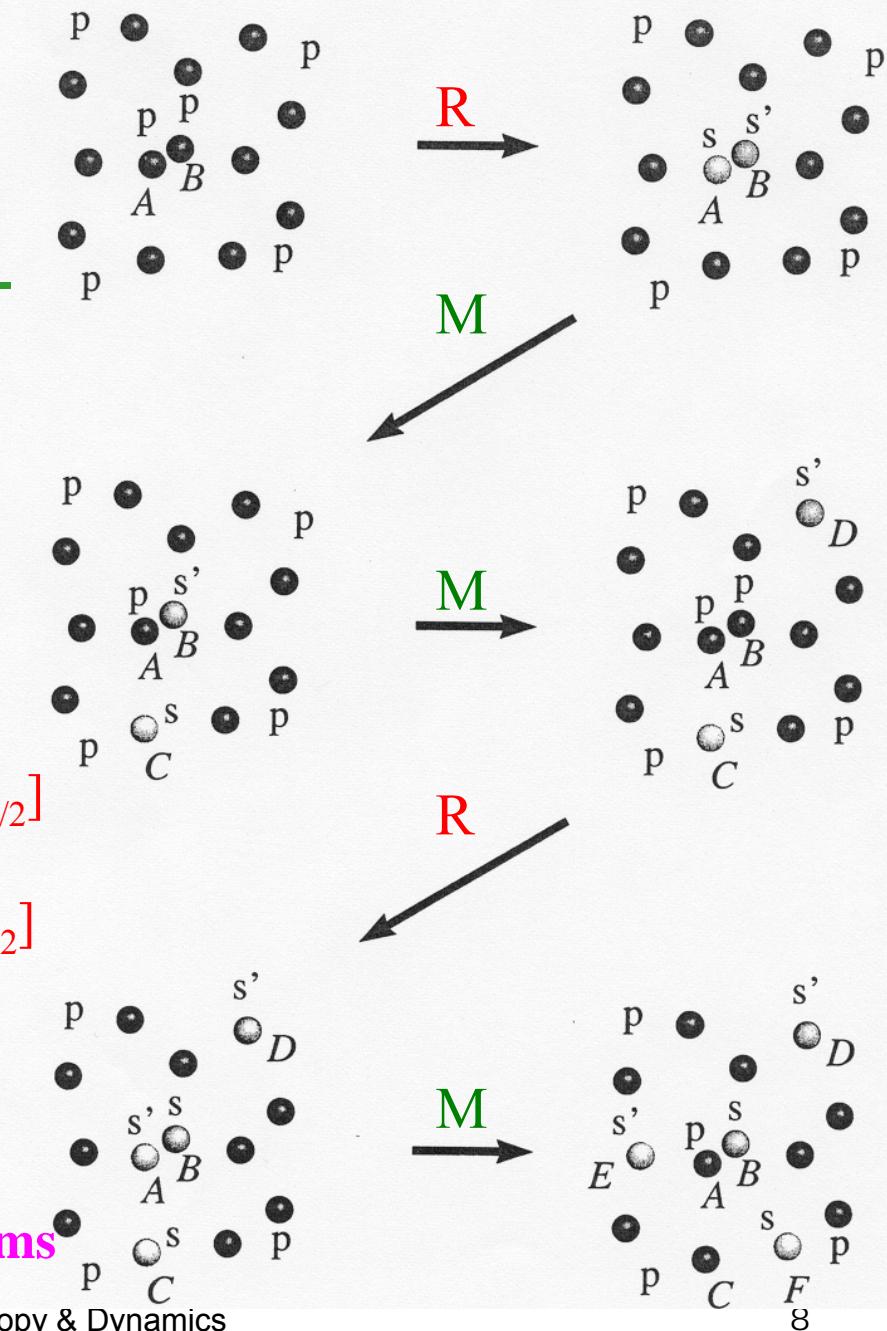
II - Migration of the reaction products



(no sensitive to the electric field)

Mourachko et al., PRA 70, 031401 (2004)

Importance of the “fluctuations”
in the Rydberg density of pairs of close atoms



Rb (Virginia)

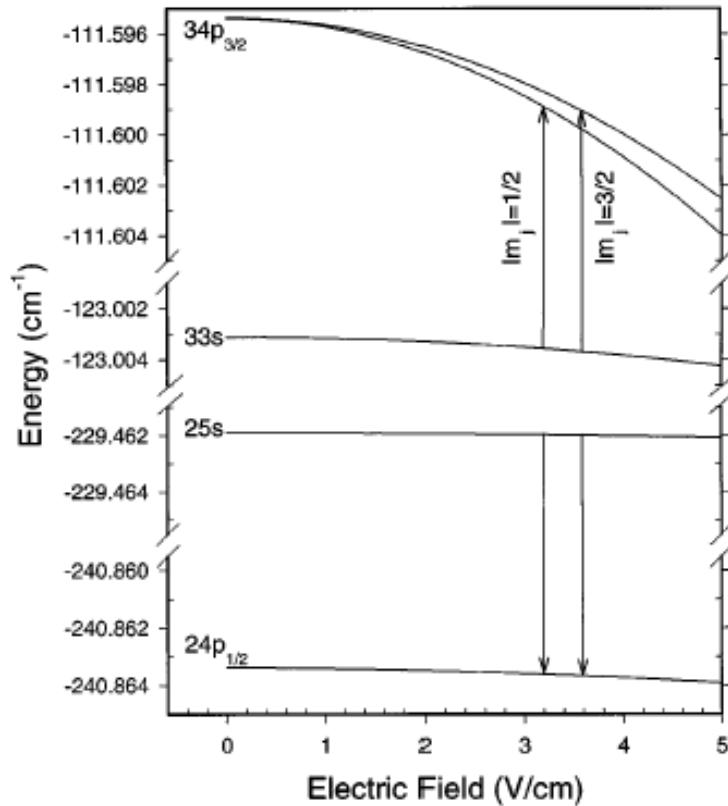


FIG. 1. Energy levels of Rb in an electric field showing the two energy transfer resonances of Eq. (1).

$$33s + 25s \rightarrow 34p_{3/2} + 24p_{1/2}$$

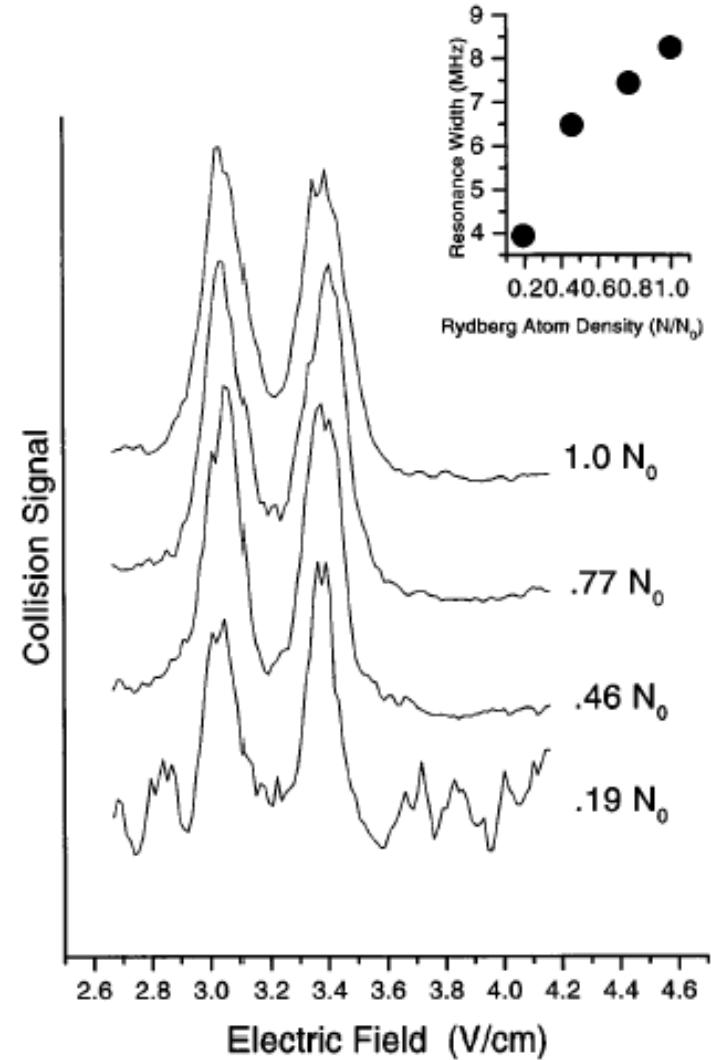


FIG. 2. The $25s_{1/2} + 33s_{1/2} \rightarrow 24p_{1/2} + 34p_{3/2}$ resonances at 300 μ K observed in the MOT at four densities, $0.19N_0$, $0.46N_0$, $0.77N_0$, and N_0 . The inset shows the width of the observed resonances vs relative density.

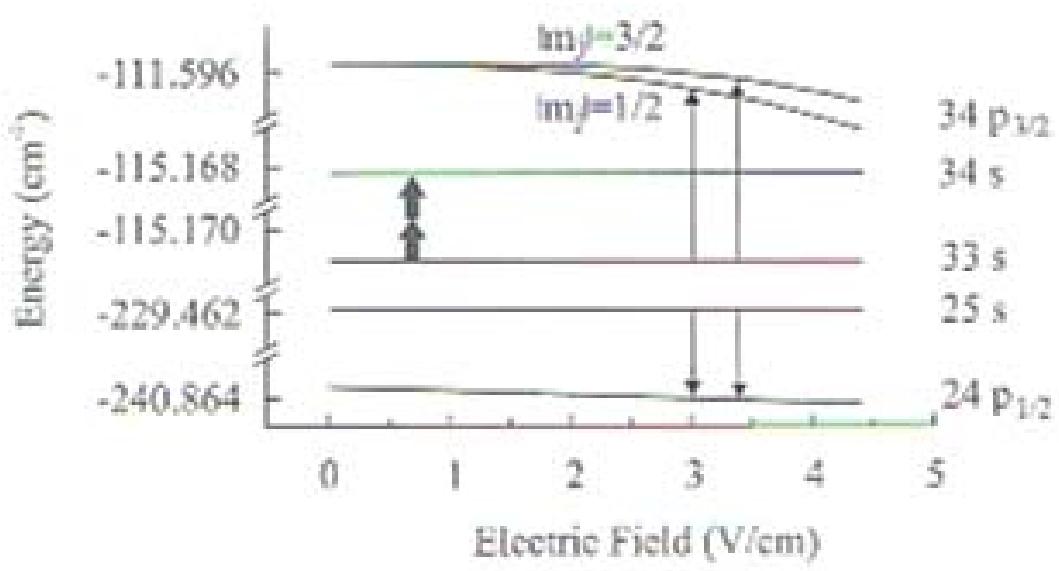
Control of many-body interactions

$$\mu_{33s34p} = 126 \text{ a.u.}$$
$$\mu_{34s34p} = 930 \text{ a.u.}$$

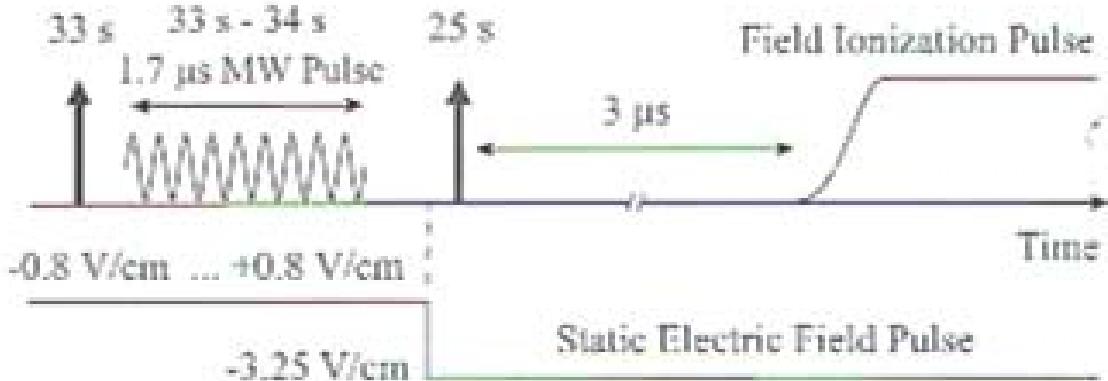
$$\mu_{25s24p} = 492 \text{ a.u.}$$

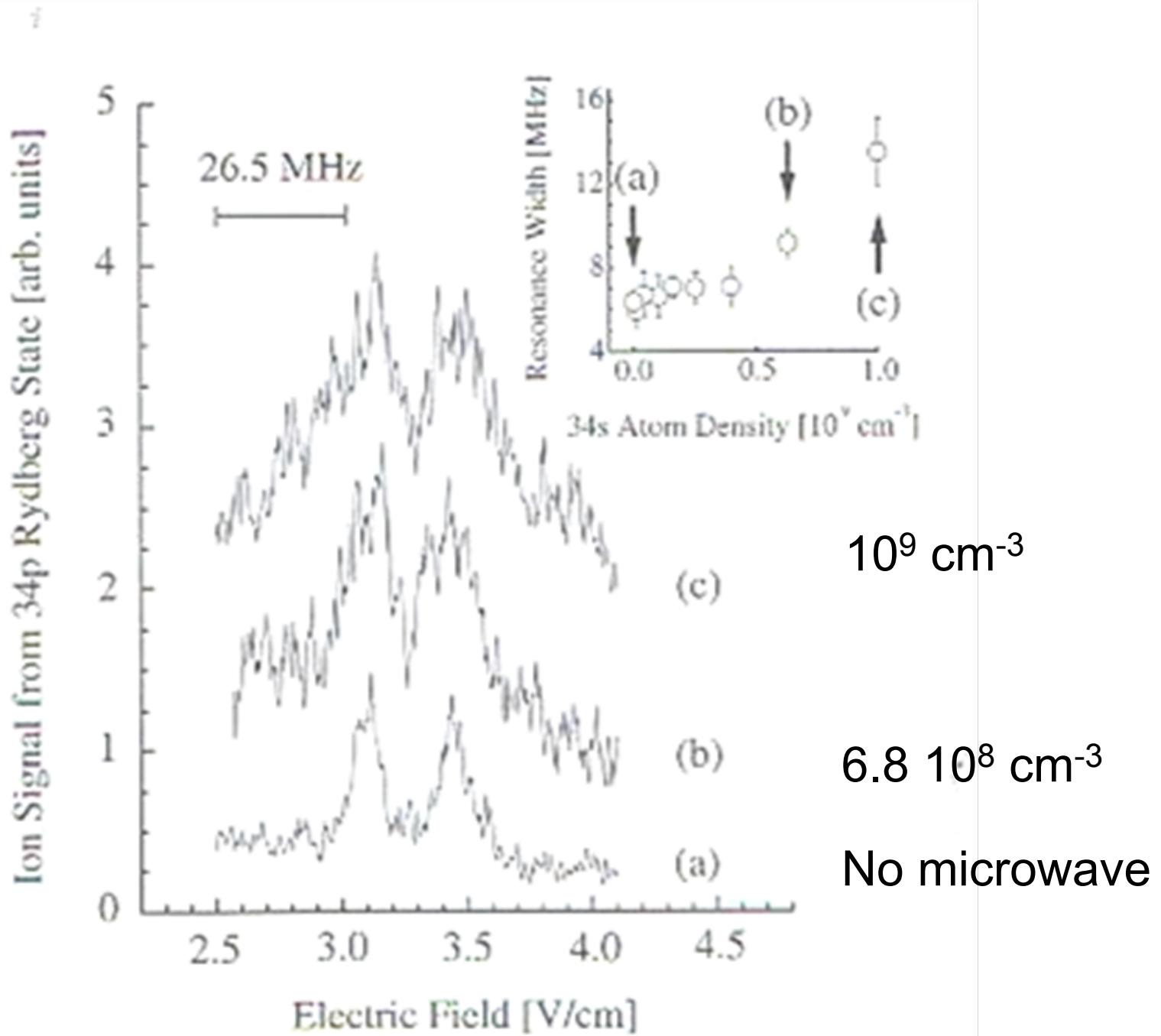
Microvawe:
117 GHz

(a)



(b)





How to test the coherence

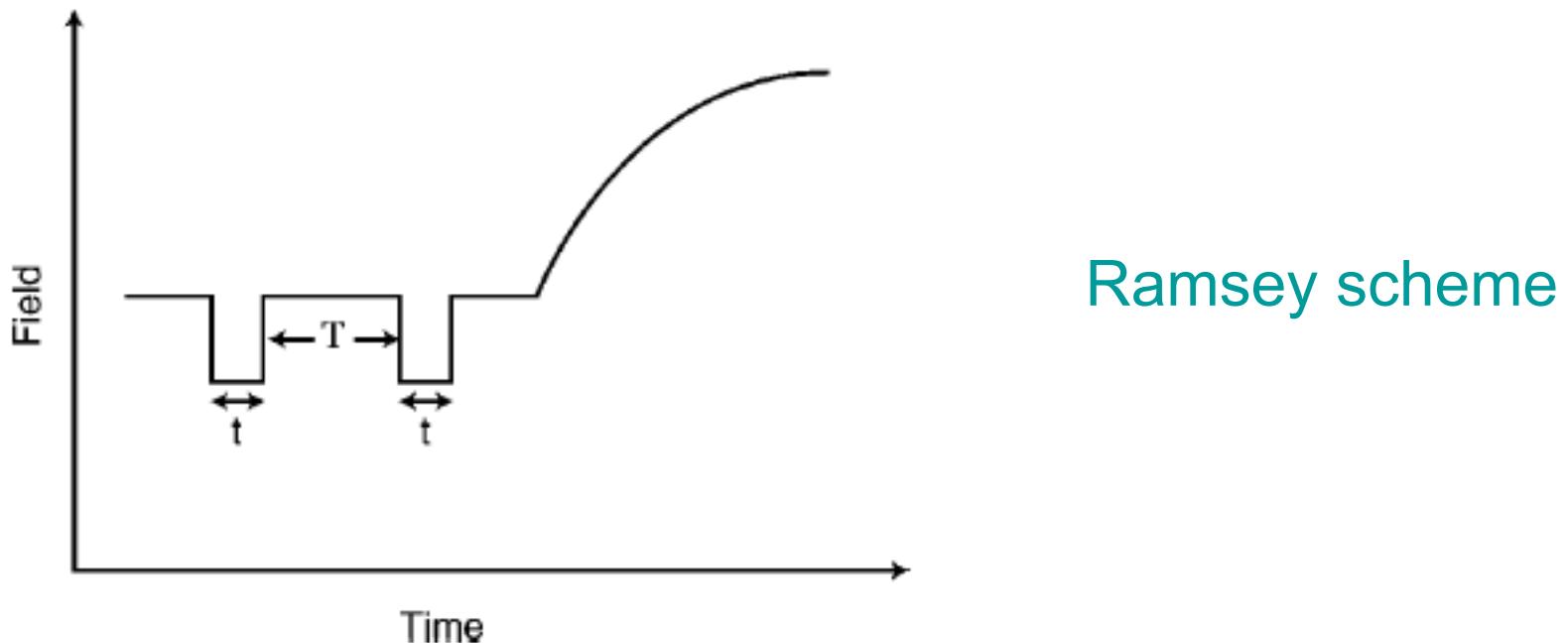


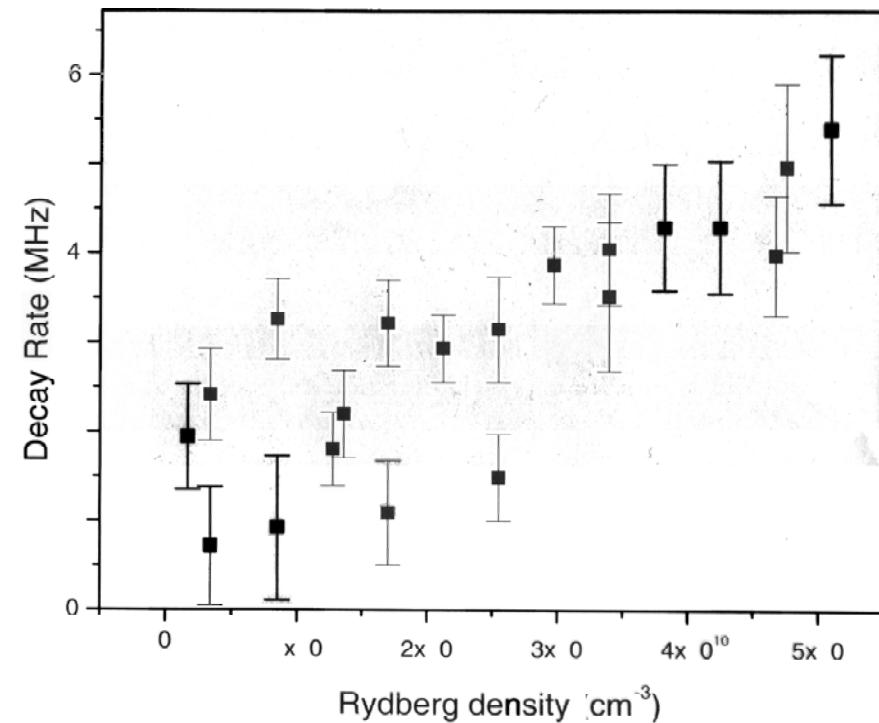
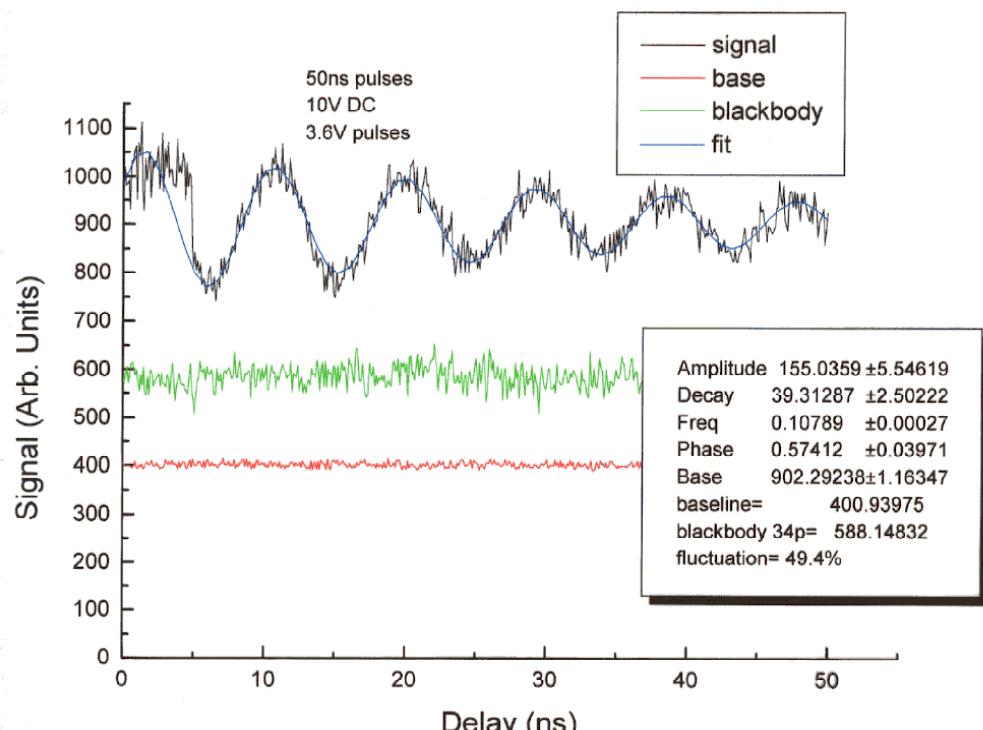
FIG. 4. Timing diagram for the Ramsey double field pulse and subsequent field ionization pulse. $T = 0 - 50$ ns and $t = 50$ ns.

The migration of the reaction product has been tested by T.F. Gallagher (Charlottesville, Virginia) through a Ramsey experiment

Rb: $25s + 33s \rightarrow 24p + 34p$ (Stark tuned, 34p selectively detected)

Rb: $25s + 24p \rightarrow 24p + 25s$ and $33s + 34s \rightarrow 34s + 33s$ (always resonant)

Charlottesville: W.R. Anderson *et al.*, PRA65, 063404 (2002)

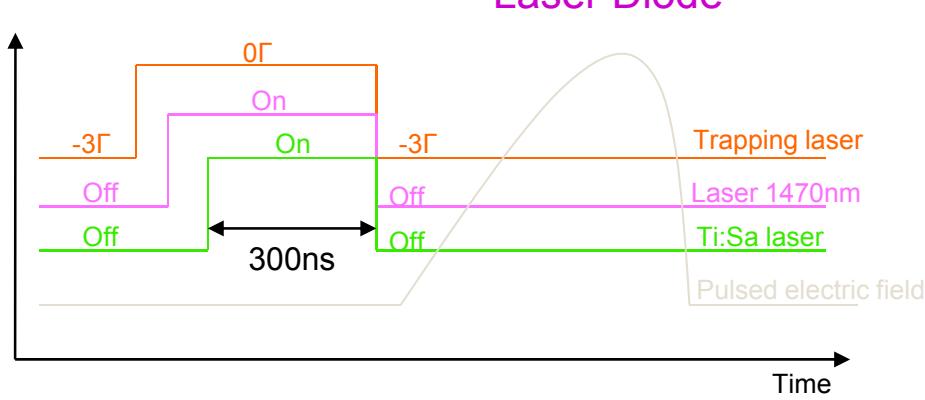
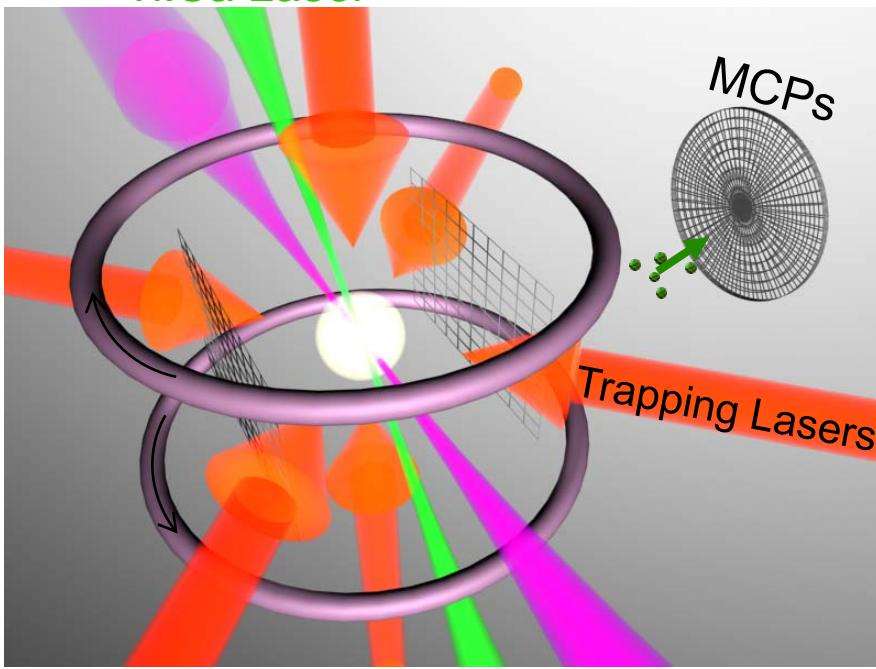


Why cold Rydberg atoms?

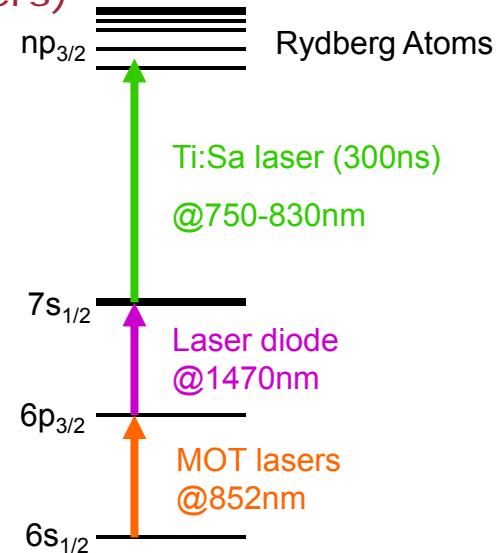
- Crucial role of cold collisions in a cold atomic sample: losses, photoassociation, evaporative cooling, sympathetic cooling, Feshbach resonance, three-body collisions...
Long time interaction!
- Rydberg atoms: huge electric dipole, long-range interactions,... *Two-body collisions.*
- Cold Rydberg atoms: *What new?*
Frozen Rydberg gas, many-body effects...

High-resolution laser excitation of Rydberg atoms

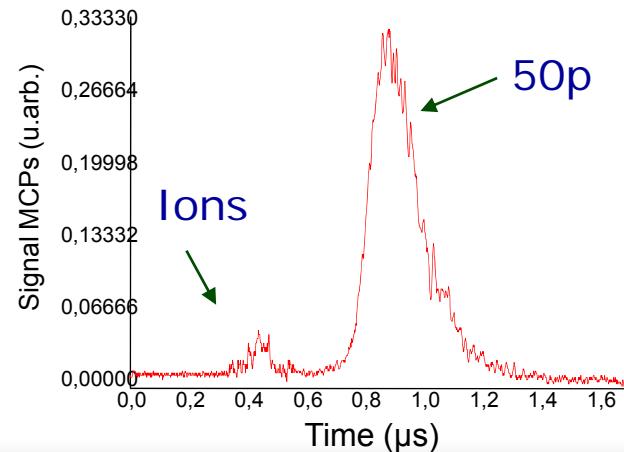
- Cs Magneto-Optical Trap (MOT)
Ti:Sa Laser

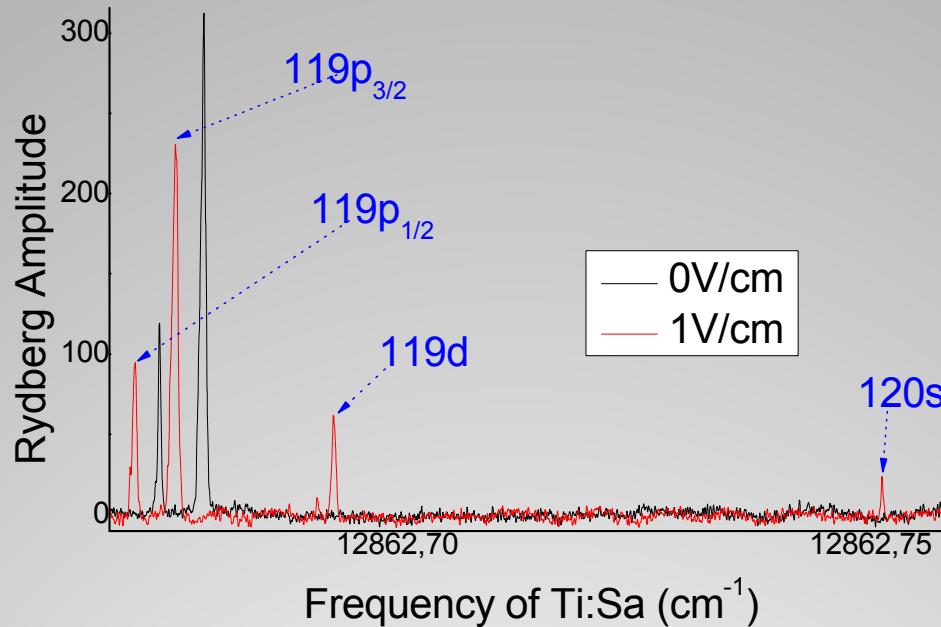


Excitation scheme (with cw lasers)



Selective field ionization





- Need to compensate spurious electric field better as $F \ll 1 \text{ mV/cm}$
- $\Delta_{\text{Laser}} \sim 5 \text{ MHz}$
- No ion during the 300 ns excitation (repetition rate 80 Hz)

High n Rydberg spectra

Dipole Blockade of the high-resolution excitation

The cold Rydberg atoms have the properties
of both cold atoms and Rydberg atoms

Frozen Rydberg gases (no motion) at the frontier of the solid state physics

- Stark-Rydberg manifold states have permanent dipole (High λ)

$$\mu = -\frac{3}{2}n(n_1 - n_2), \mu_{\max} \sim \pm \frac{3}{2}n^2$$

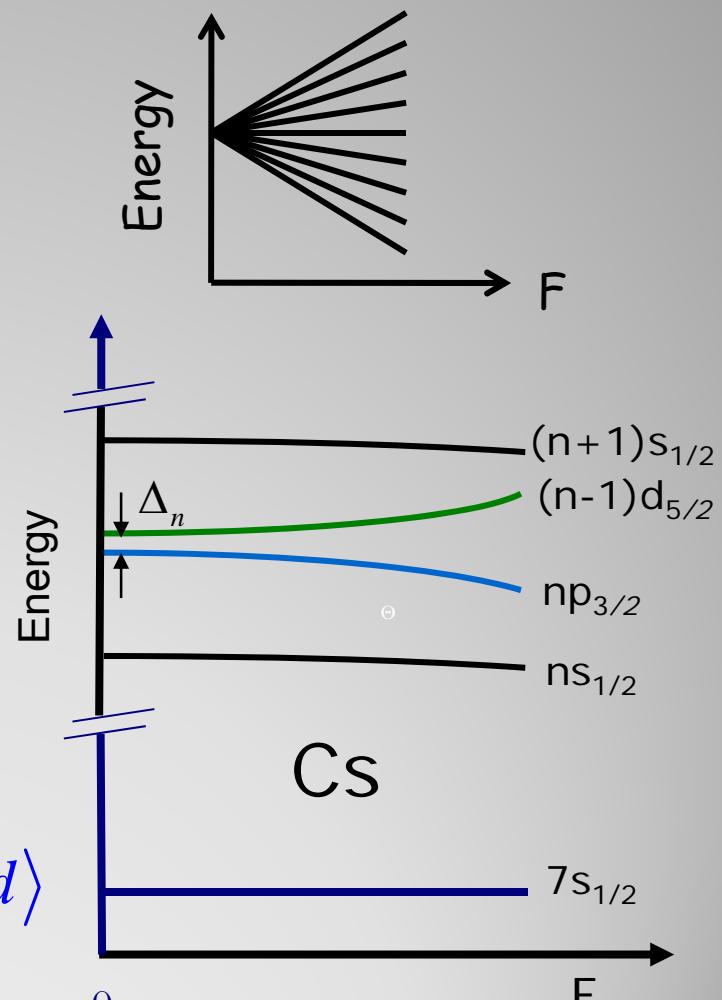
$$n = n_1 - n_2 + |m| + 1$$

- p and d strongly Stark-coupled

$$\mu \approx \mu_{dp} \sin \theta, \mu_{dp} \sim n^2 (\text{a.u.})$$

$$\tan(\theta) = \frac{|W_n|}{\Delta_n / 2}, W_n = -\mu_{dp} F_z$$

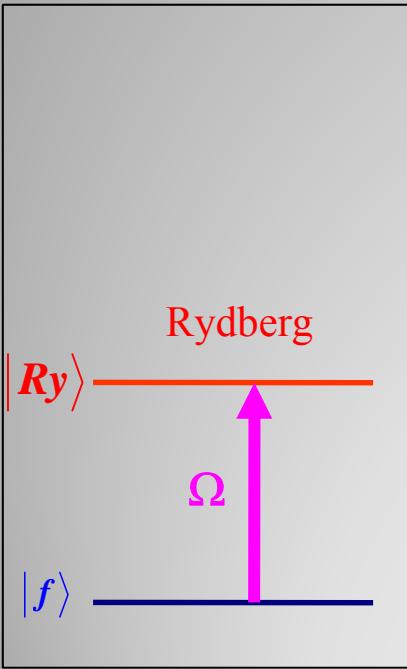
$$|np, F\rangle \approx \cos\left(\frac{\theta}{2}\right)|np\rangle - \sin\left(\frac{\theta}{2}\right)|(n-1)d\rangle$$



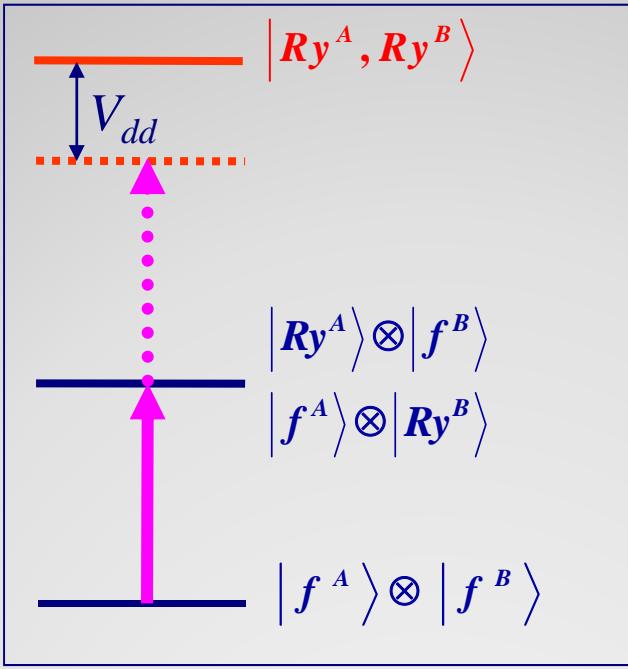
Dipole induced by electric field

$$n = 30 \quad \mu_{\max} \sim 3500 \text{ Debye} ; \quad n = 100 \quad \mu_{\max} \sim 38000 \text{ Debye}$$

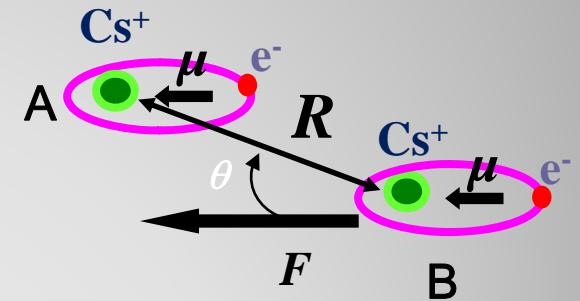
Single atom



Pair of atoms

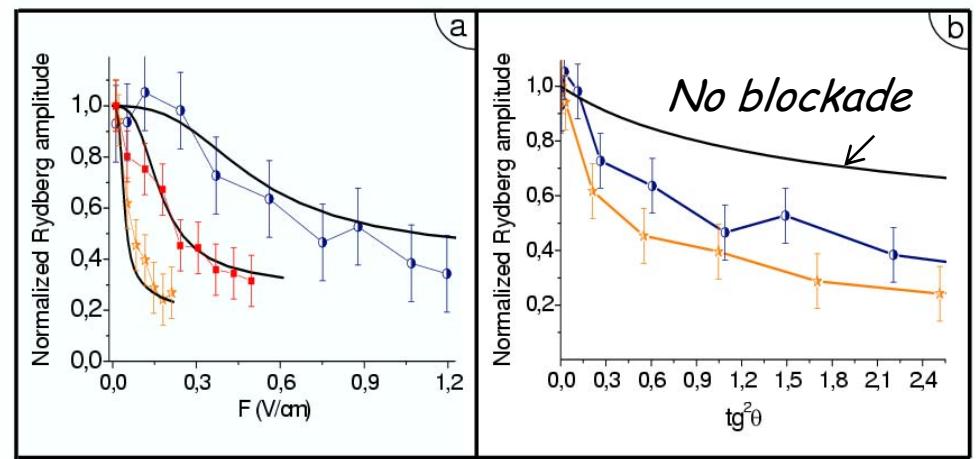
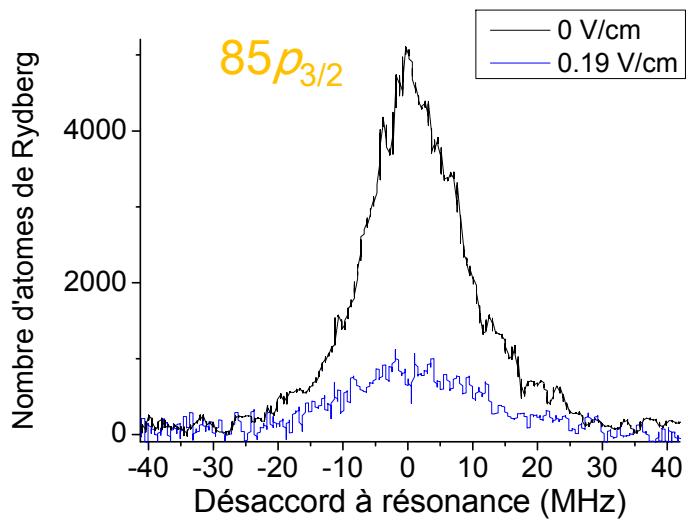
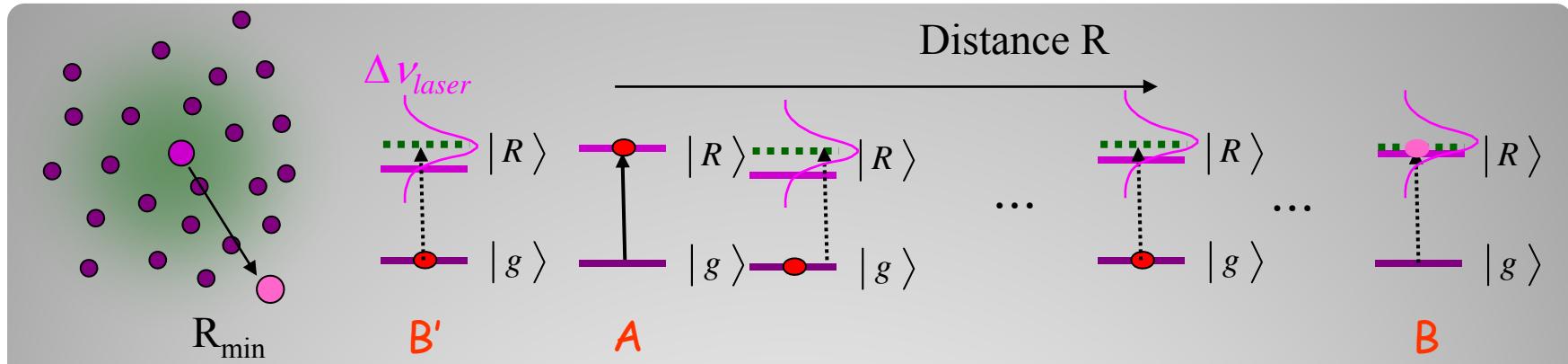


$$V_{dd} = \frac{\vec{\mu}_A \cdot \vec{\mu}_B - 3(\vec{\mu}_A \cdot \hat{n}_{AB})(\vec{\mu}_B \cdot \hat{n}_{AB})}{R_{AB}^3}$$



Dipole-dipole interaction between two atoms

Dipole blockade of the excitation / Conditionnal excitation



60, 70 and 85 p_{3/2}

Dipole blockade in an atomic sample

Spectrally broadband excitation: band of levels

Limitation of the high-resolution excitation

Role of the nearest neighbor

$$\text{Recall : } \tan(\theta) = \frac{|W_n|}{\Delta_n / 2}$$

Dipole-dipole interaction

Förster resonance

$$H = H_R + \sum_{i=1}^N (H_{Ai} + H_{RAi})$$

$$H_R = \sum_{kl} hck a_{kl}^+ a_{kl}^- ; \quad H_{Ai} = \hbar\omega_0 |2,i\rangle\langle 2,i| ; \quad H_{RAi} = -\vec{E} \cdot \vec{\mu}_i$$

$$\vec{E} = i \sum_{kl} \sqrt{\frac{hck}{2\epsilon_0 L^3}} a_{kl}^- \vec{e}_l \exp(i\vec{k} \cdot \vec{x}_i) + h.c.$$

$$\vec{\mu}_i = \vec{\mu}_i^+ + \vec{\mu}_i^- ; \quad \vec{\mu}_i^+ = \langle 2 | \vec{\mu} | 1 \rangle | 2, i \rangle \langle 1, i | = \langle 2 | \vec{\mu} | 1 \rangle r_i^+ ; \quad \vec{\mu}_i^- = \left(\vec{\mu}_i^+ \right)^+$$

Master equation in Born-Markov approximation (interaction representation)

$$\frac{d\sigma}{dt} = -\frac{\Gamma}{2} \sum_{i=1}^N \left([r_i^+ r_i^-, \sigma(t)]_+ - 2r_i^- \sigma(t) r_i^+ \right) - \frac{1}{i\hbar} \sum_{j \neq i} \left[\vec{E}_j^+ \cdot \vec{\mu}_i^- \sigma(t) - \sigma(t) \left(\vec{E}_j^+ \right)^+ \cdot \vec{\mu}_i^- \right]$$

\vec{E}_j^+ electric dipole field created by j in i

$$\vec{E}_j^+ = \frac{1}{4\pi\epsilon_0} \left\{ k_0^2 \left(\frac{\vec{x}_{ij}}{x_{ij}} \times \vec{\mu}_i^+ \right) \times \frac{\vec{x}_{ij}}{x_{ij}} \frac{e^{ik_0 x_{ij}}}{x_{ij}} + \left[3 \frac{\vec{x}_{ij}}{x_{ij}} \left(\frac{\vec{x}_{ij}}{x_{ij}} \cdot \vec{\mu}_i^+ \right) - \vec{\mu}_i^+ \right] \left(\frac{1}{x_{ij}^3} - \frac{ik_0}{x_{ij}^2} \right) e^{ik_0 x_{ij}} \right\}$$

N two-level (1,2) atoms (i)

Master equation $\frac{d\sigma}{dt} = -\frac{\Gamma}{2} \sum_{i=1}^N \left([r_i^+ r_i^-, \sigma(t)]_+ - 2r_i^- \sigma(t) r_i^+ \right)$

$$-\frac{\Gamma}{2} \sum_{j \neq i} \left([r_i^+ r_j^-, \sigma(t)]_+ - 2r_j^- \sigma(t) r_j^+ \right) + \frac{1}{i\hbar} \sum_{j \neq i} \left[H_{dd}^{(i,j)}, \sigma(t) \right]$$

We have the terms of cooperative spontaneous emission (superradiance) and those corresponding to dipole-dipole interaction ($H_{dd}^{(i,j)}$)

$$H_{dd}^{(i,j)} = \frac{\mu_i \mu_j}{4\pi \epsilon_0} \left\{ \left(1 - 3 \cos^2 \theta_{ij} \right) \frac{1}{x_{ij}^3} - \frac{\left(1 + \cos^2 \theta_{ij} \right) k_0^2}{2} \frac{1}{x_{ij}} \right\}$$

We have the classical term of dipole-dipole interaction

+ another term a priori much smaller when $k_0 x_{ij} \ll 1$

$\omega_0 \sim 1/(2n^3)$ a.u. ; $k_0^{-1} = \lambda = \lambda / 2\pi = 115 \mu m$ ($n = 20$), 390 ($n = 30$), 930 ($n = 40$), $1.8 mm$ ($n = 50$), 3 ($n = 60$), 7.5 ($n = 80$), 14.5 ($n = 100$)

Small volume: $K_0 x_{ij} < 1$

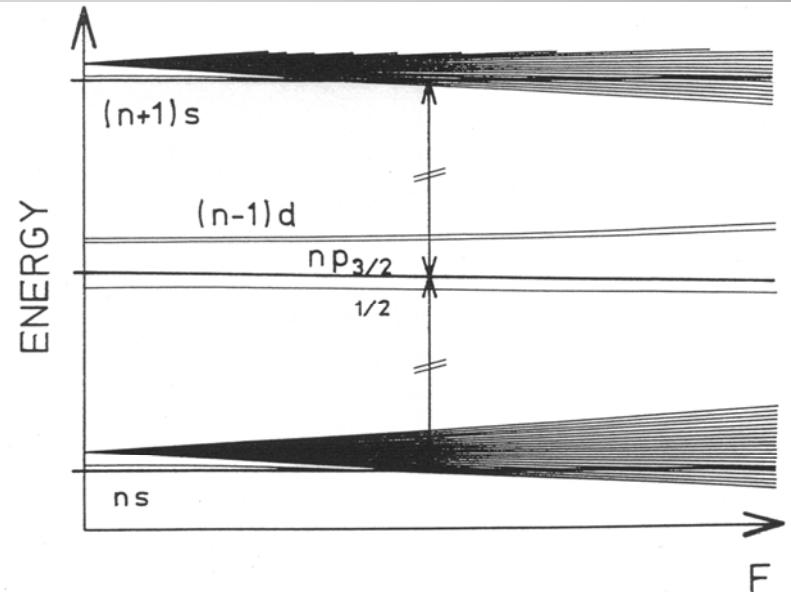
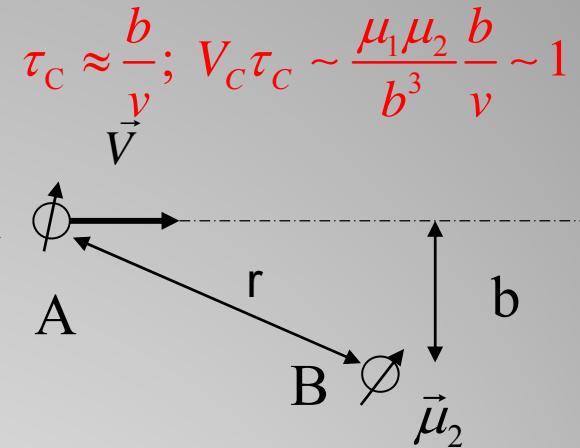
Förster resonances

Dipole-dipole coupling

- **Resonant Rydberg-Rydberg atom collisions** (T.F. Gallagher et al., P.R.L. 40, 1362 (1981) with Na Impact parameter $b \sim \mu/v^{1/2} \sim 1 \mu\text{m}$ at $T \sim 500 \text{ K}$)
- Cs [np_{3/2}] + Cs [np_{3/2}] \rightarrow Cs [ns] + Cs [(n+1)s]

$$V_{dd} = \frac{\vec{\mu}_A \cdot \vec{\mu}_B - 3(\vec{\mu}_A \cdot \vec{n}_{AB})(\vec{\mu}_B \cdot \vec{n}_{AB})}{R_{AB}^3}$$

$$\begin{aligned} \langle ns, (n+1)s | V_{dd} | np_{3/2}, np_{3/2} \rangle &\sim \\ \left\langle ns \left| \vec{\mu}_A \right| np_{3/2} \right\rangle \left\langle (n+1)s \left| \vec{\mu}_B \right| np_{3/2} \right\rangle &\sim \frac{n^4}{R^3} \end{aligned}$$



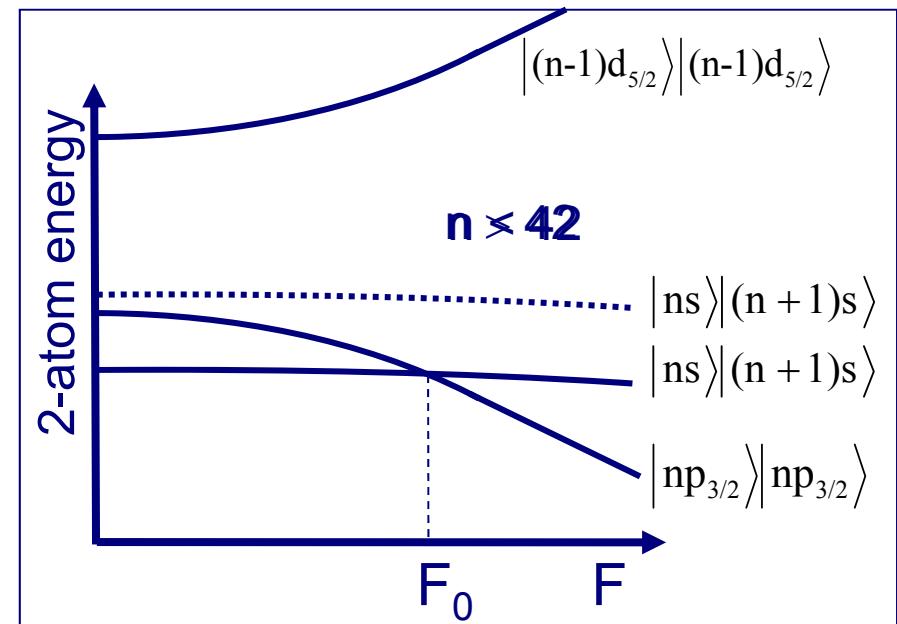
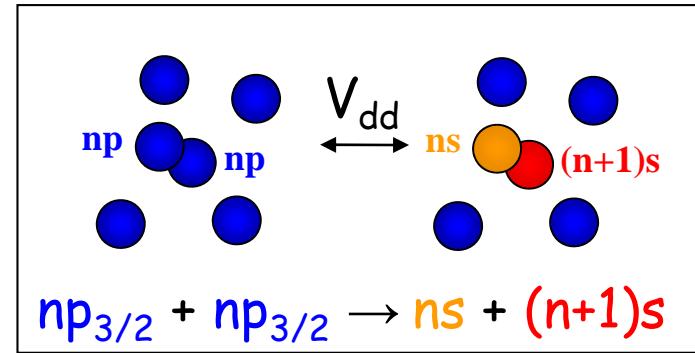
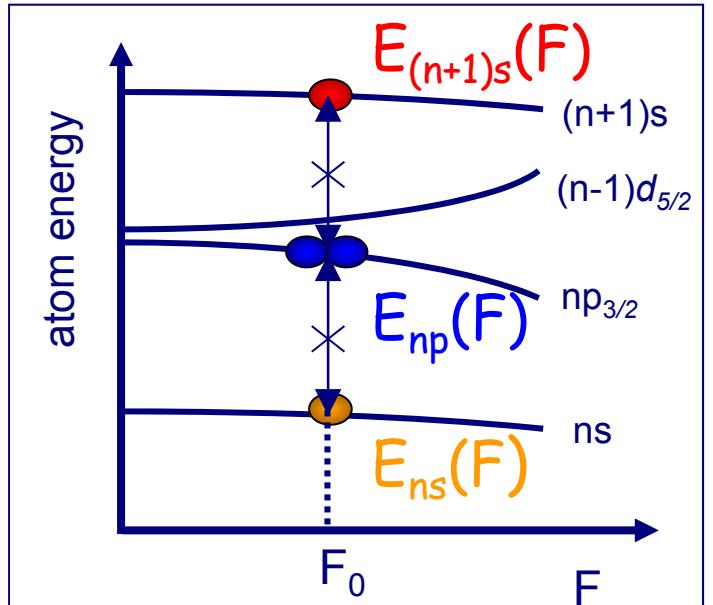
Förster resonances

$$n = 60 \quad R = 1 \mu\text{m} \quad V_{dd} \sim 14 \text{ GHz}$$

Föster resonances - dipole dipole interaction

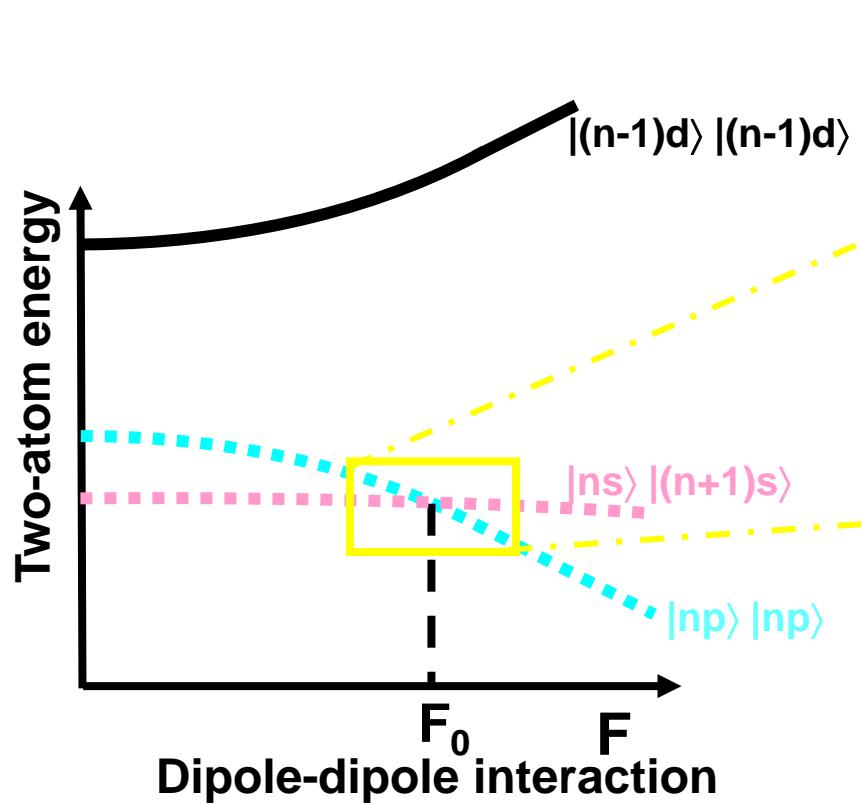
Resonance at F_0

$$Cs: 2 E_{np}(F_0) = E_{ns}(F_0) + E_{(n+1)s}(F_0)$$

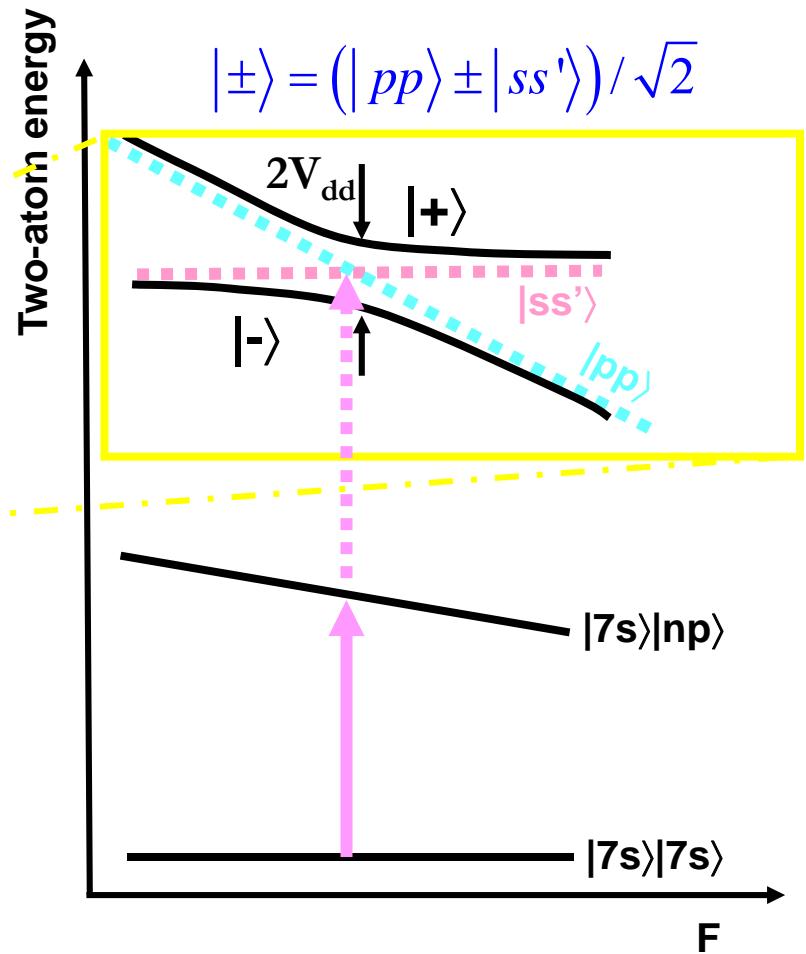


FRET (Förster resonance energy transfer)

Excitation of a pair of atoms at a Förster resonance

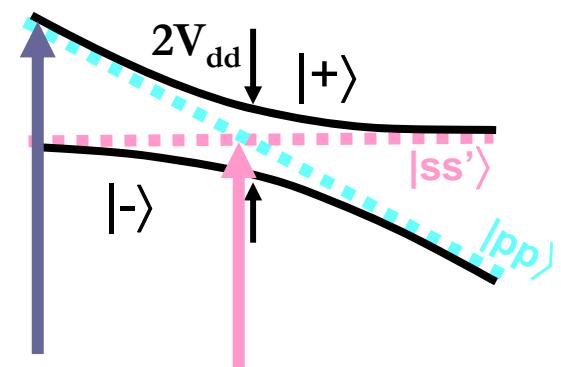
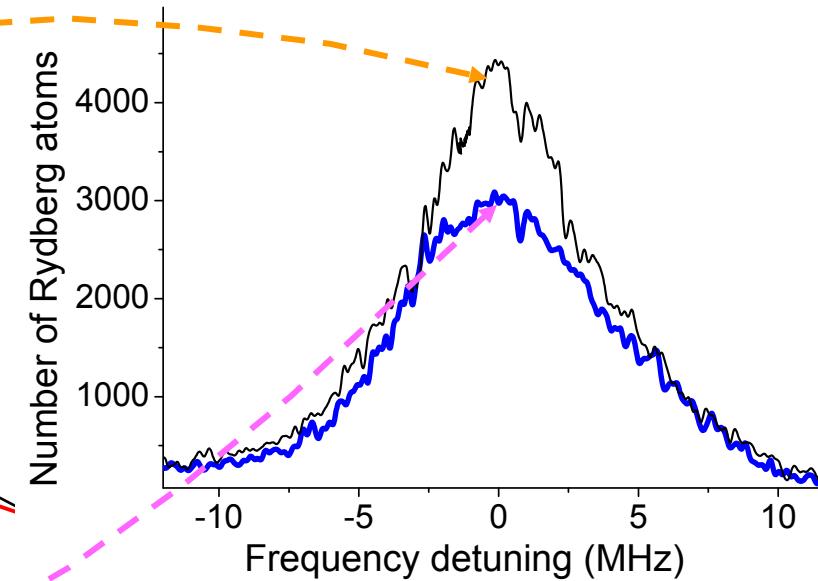
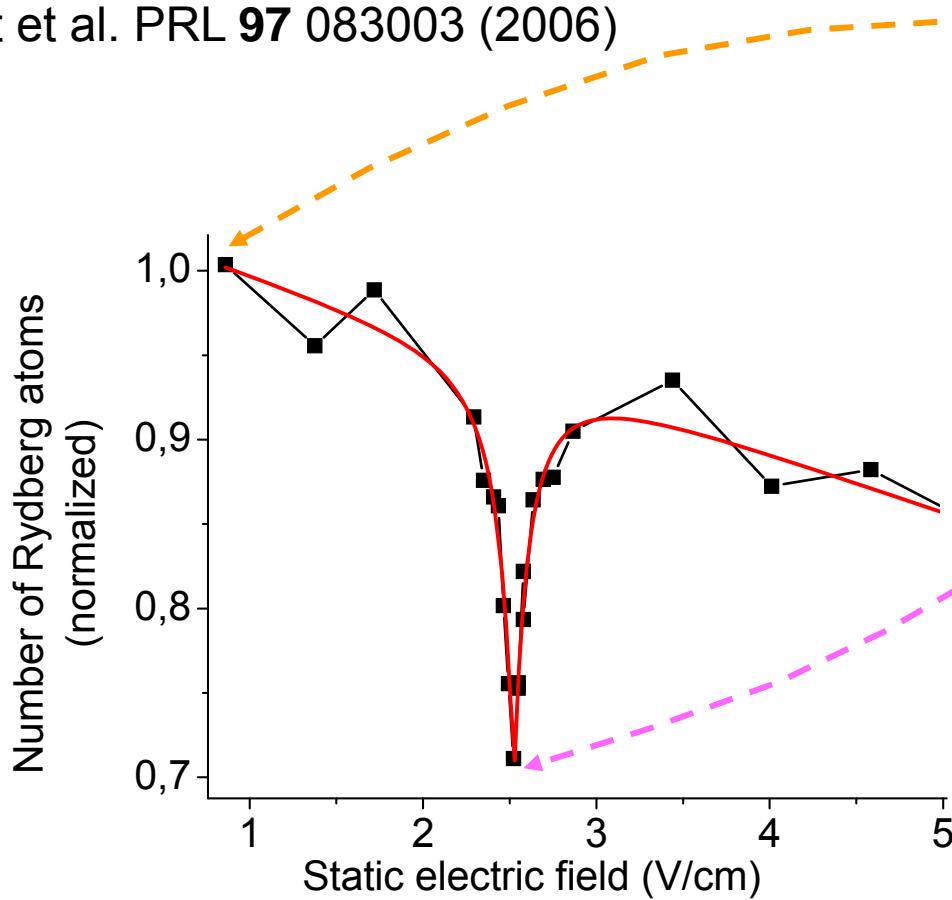


$$V_{dd} = \frac{\vec{\mu}_A \cdot \vec{\mu}_B - 3(\vec{\mu}_A \cdot \vec{n}_{AB})(\vec{\mu}_B \cdot \vec{n}_{AB})}{R_{AB}^3}$$



Dipole blockade of the high-resolution Rydberg excitation ($36p_{3/2}$)

Vogt et al. PRL 97 083003 (2006)

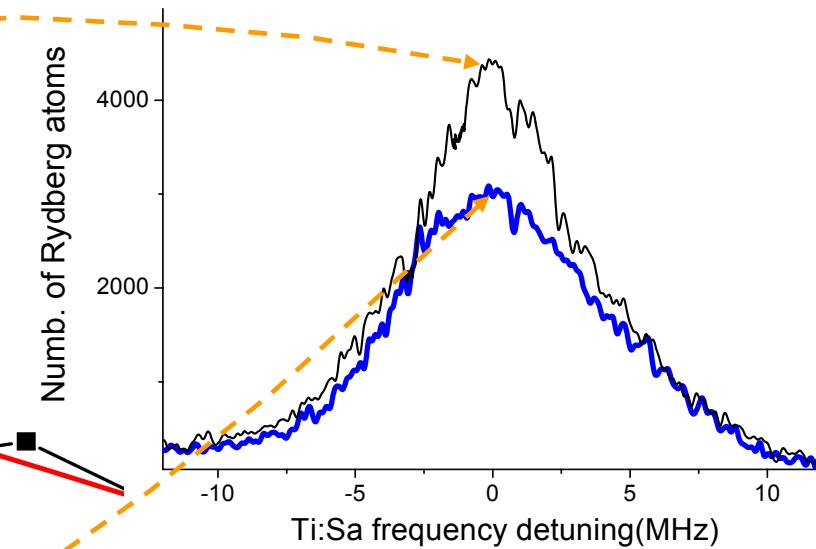
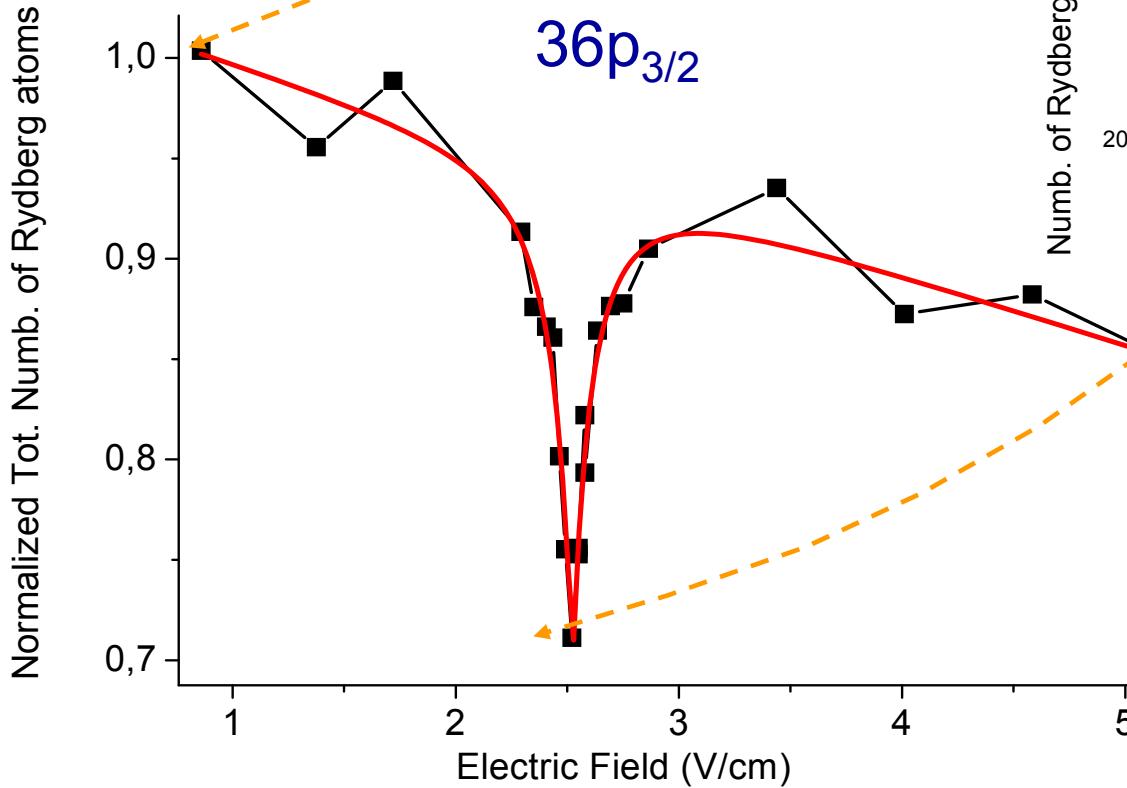


Demonstration of the dipole blockade

300ns cw laser excitation

■ Rydberg atoms excited at Förster resonance

→ Dipole blockade



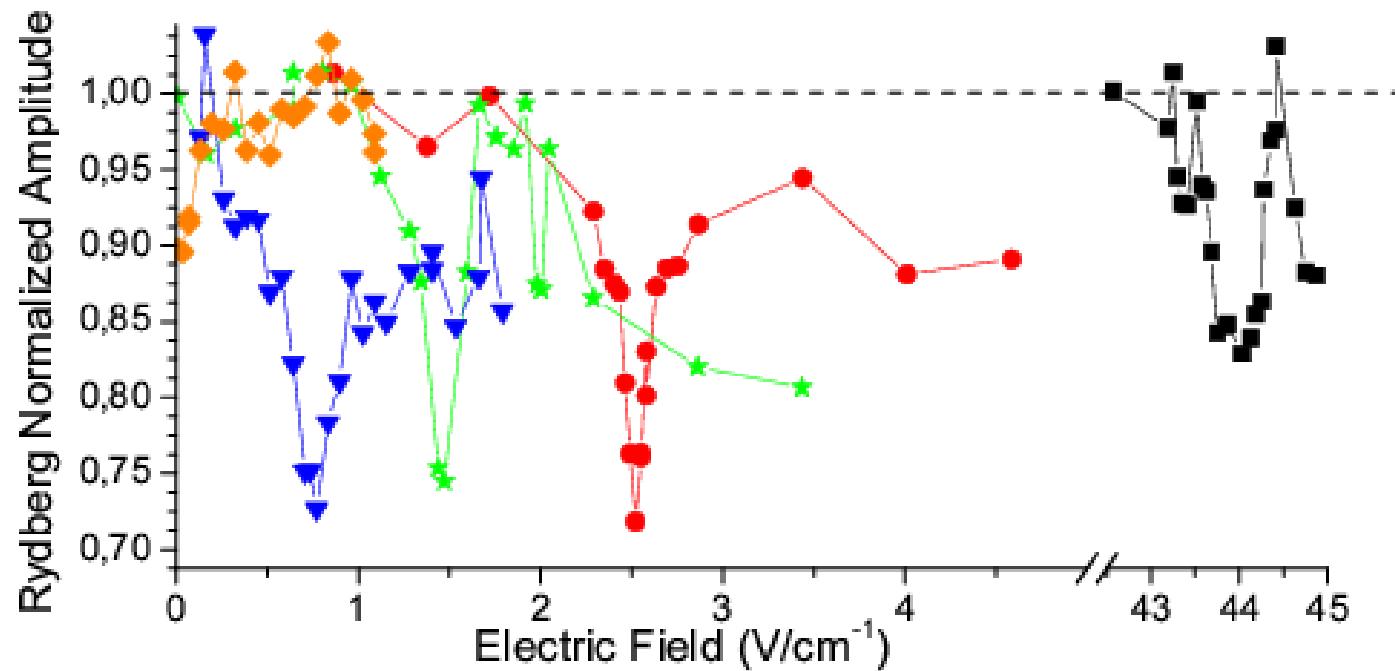
Dipole blockade from 25 to 42p

30 % for $n = 34 - 41$

$$\Delta_L \sim W \Rightarrow R_{\min} \approx 4 \mu m$$

$n = 42, 40, 38, 36$

$n = 25$

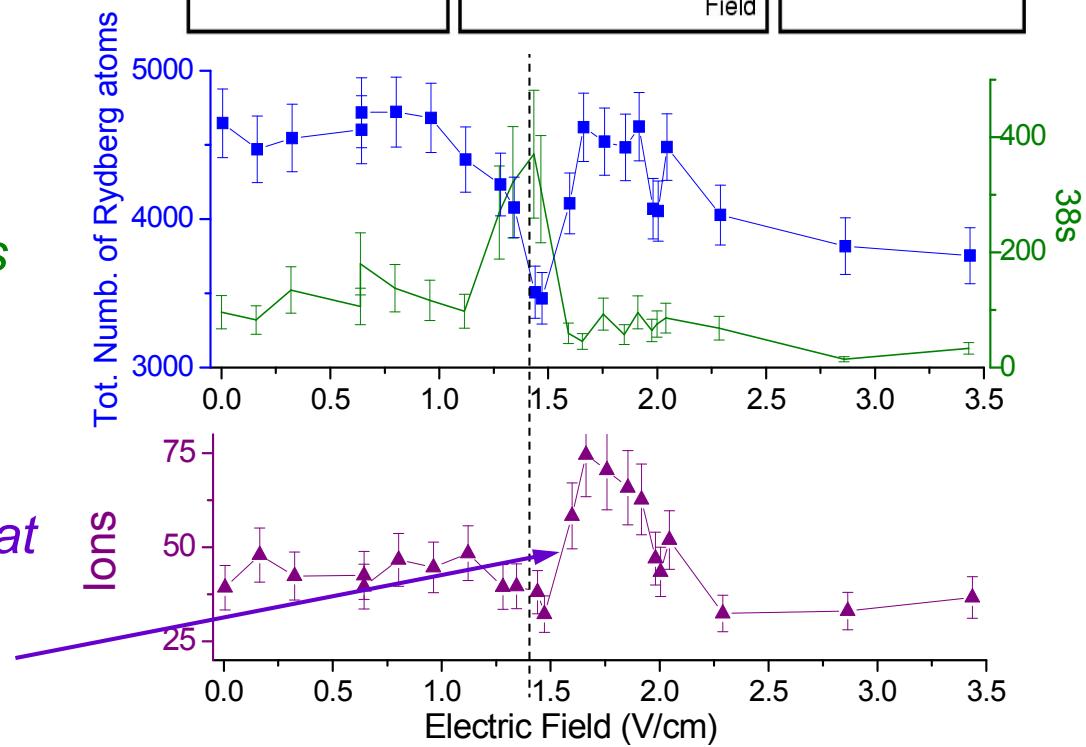
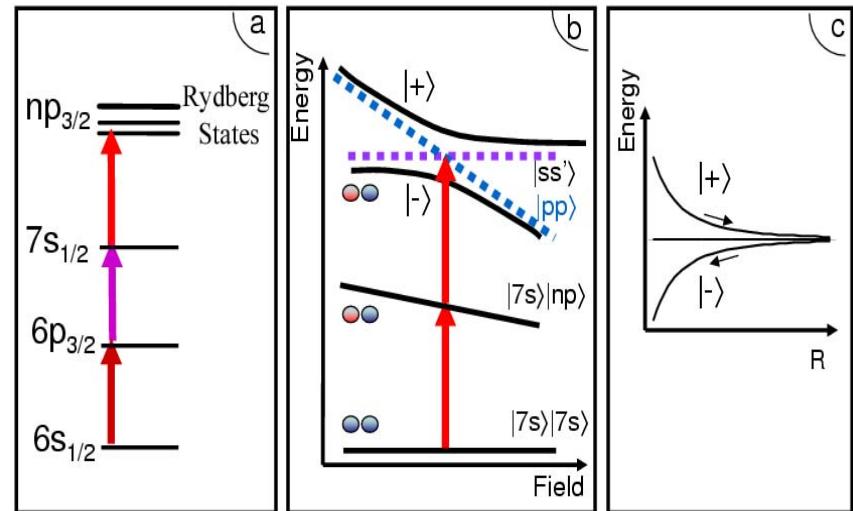


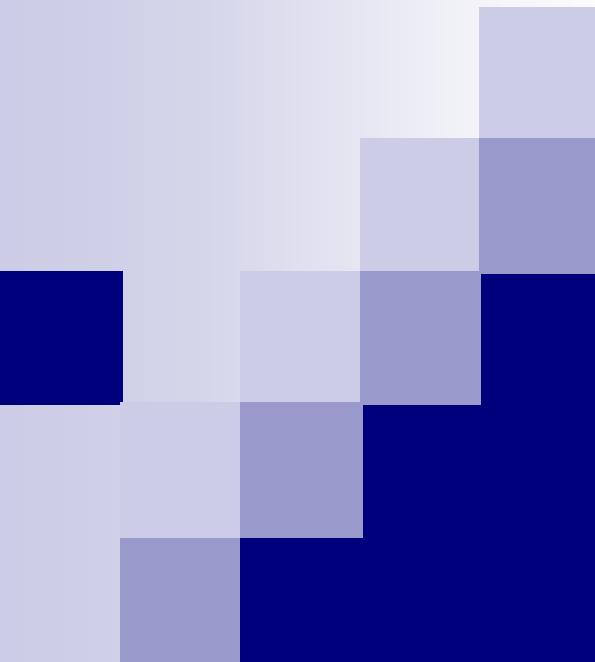
Dipole blockade

■ Dipole blockade at Förster resonance $38\text{ p}_{3/2}$

■ Transfer $p \rightarrow s$ state
 $np_{3/2} + np_{3/2} \rightarrow ns + (n+1)s$

■ Few Ions (<1%) \rightarrow no broadening of the lines.
Number of ions increases at the right of the resonance
 \rightarrow attractive force

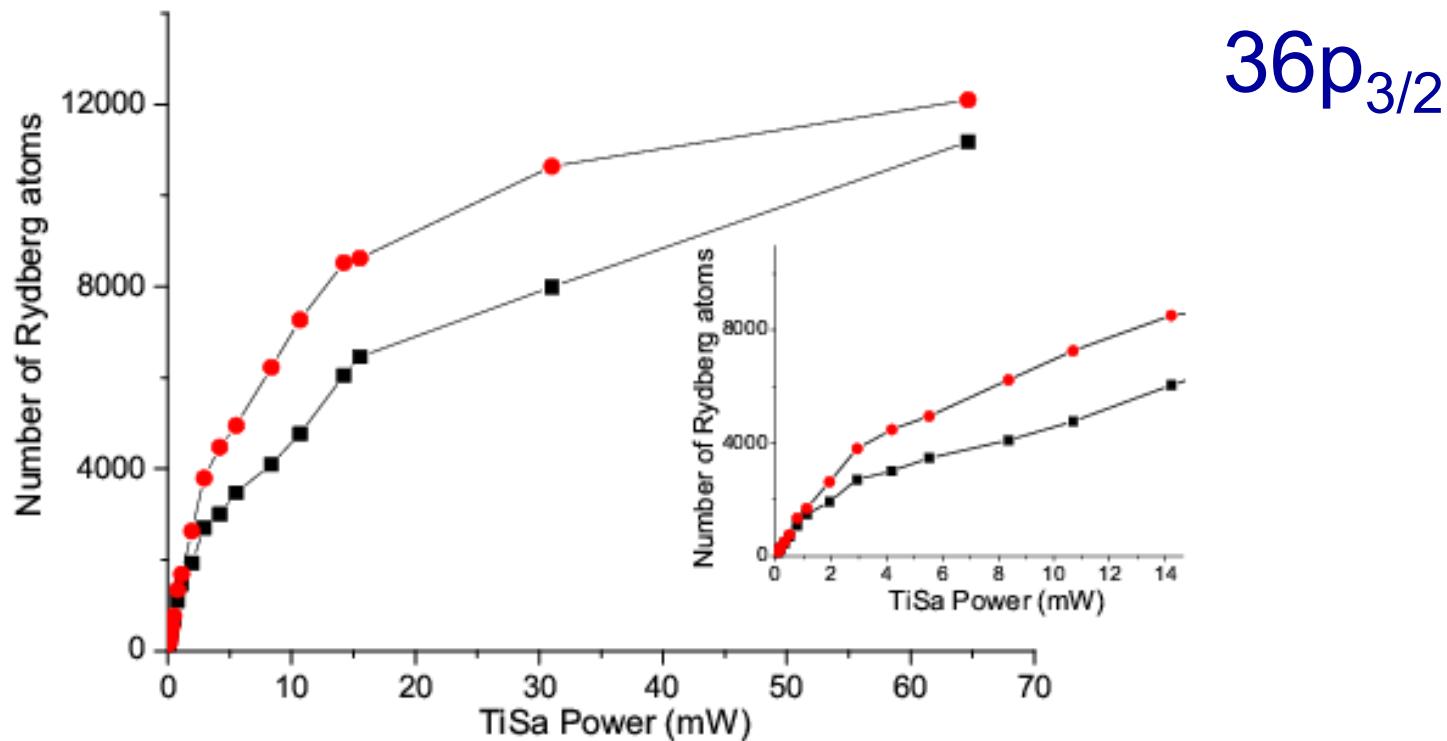




Properties of dipole blockade

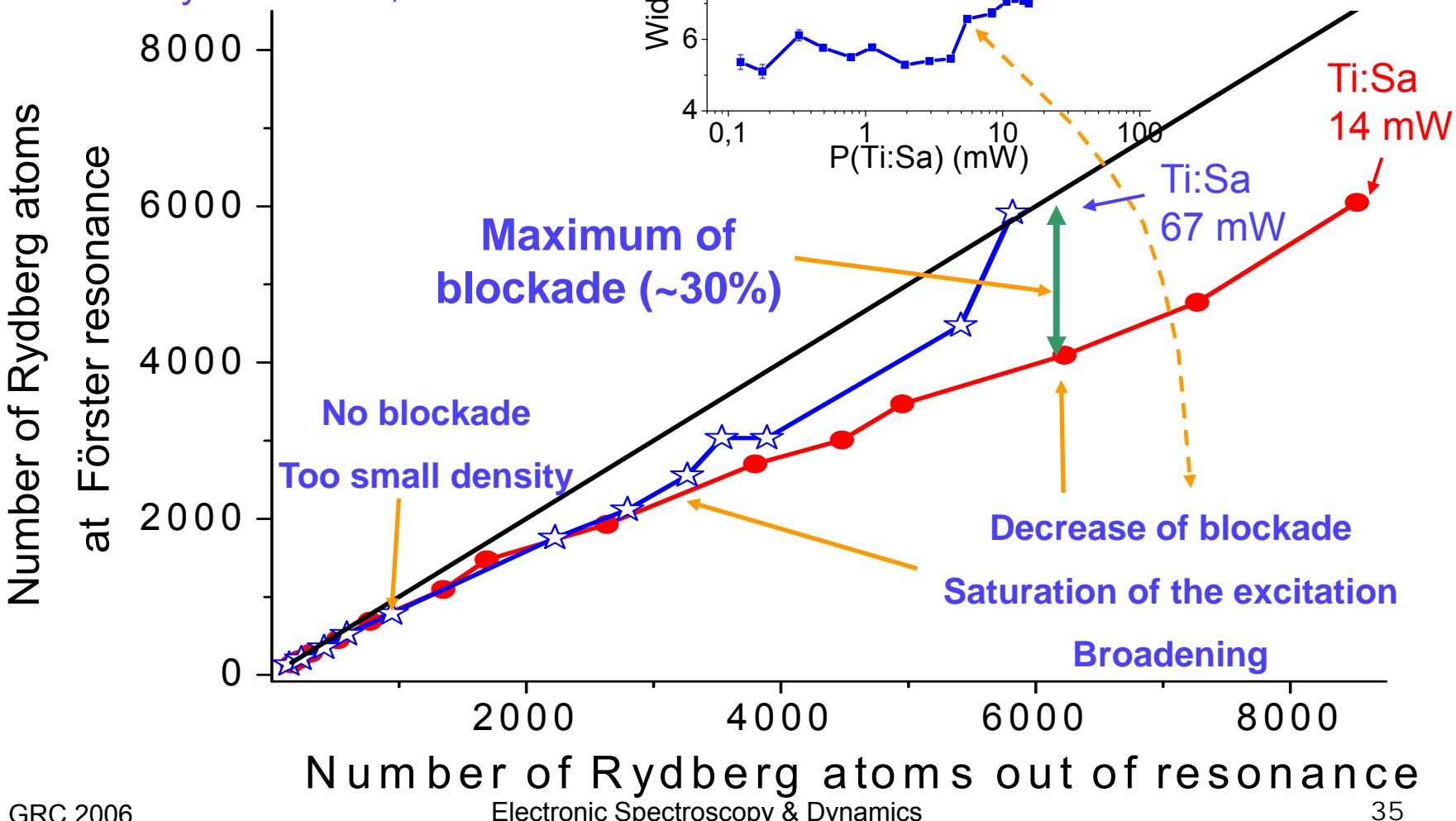
At Förster resonance

Dipole blockade and saturation of the excitation due to the “short” lifetime of 7s level



Density effect in the blockade $36p_{3/2}$

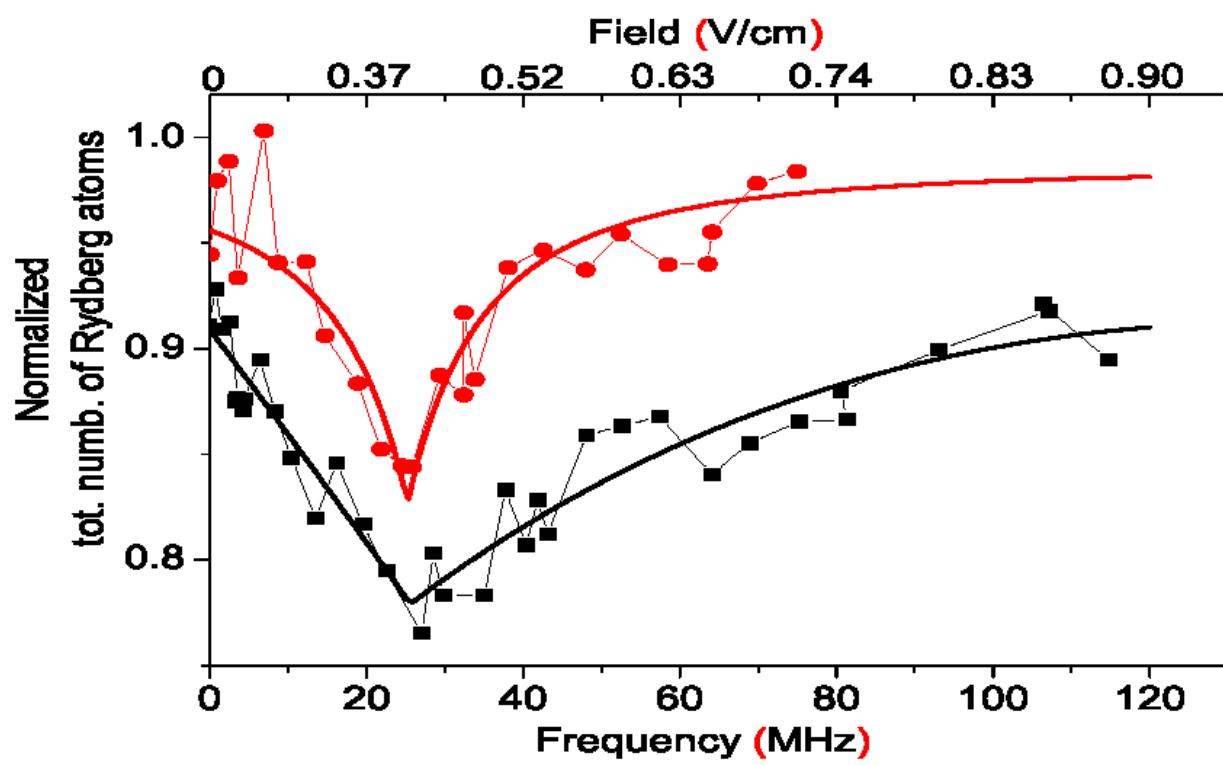
- Density of 7s level
- $D = 8 \cdot 10^9 \text{ cm}^{-3}$
- Density of 7s level, D/3



Resonance in field

10 times larger than laser ones.

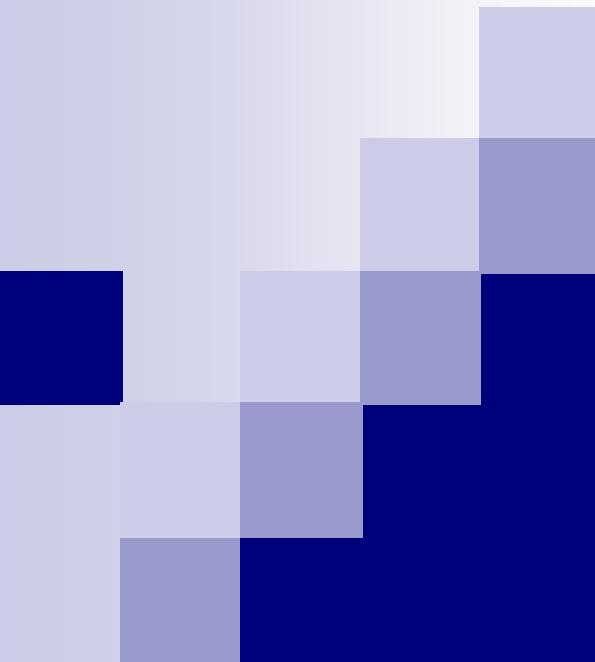
Similar as pulsed excitation: Many-body effects



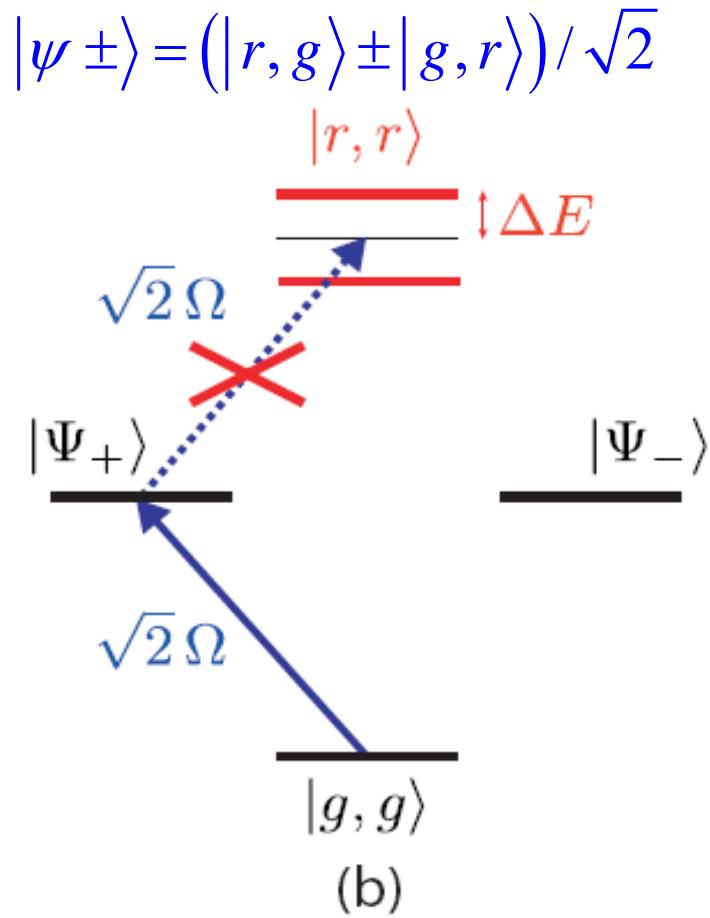
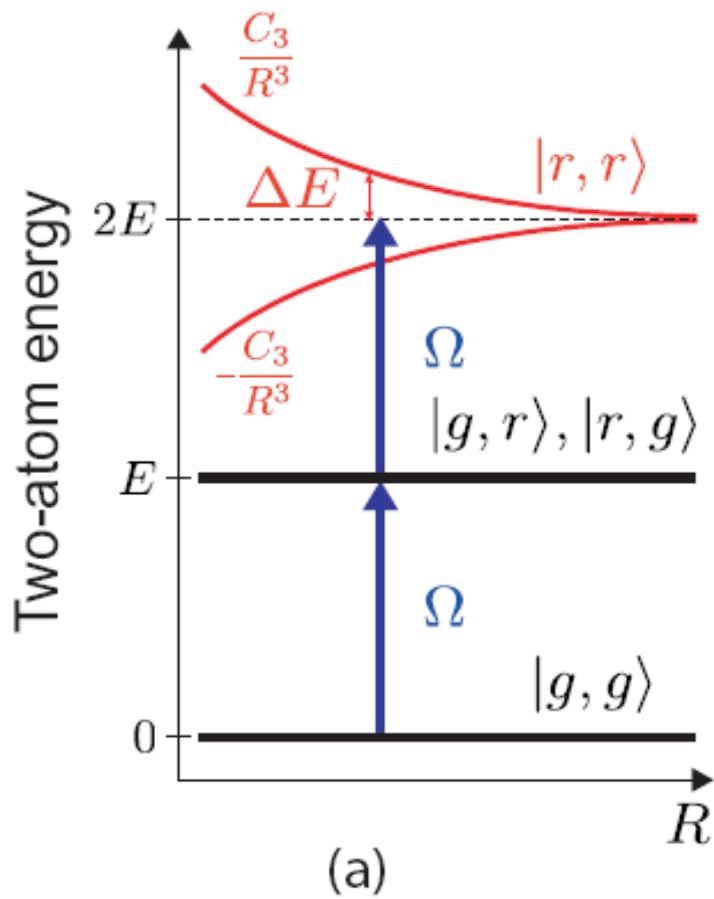
$41\text{p}_{3/2}$

3000 Rydberg
atoms

5000

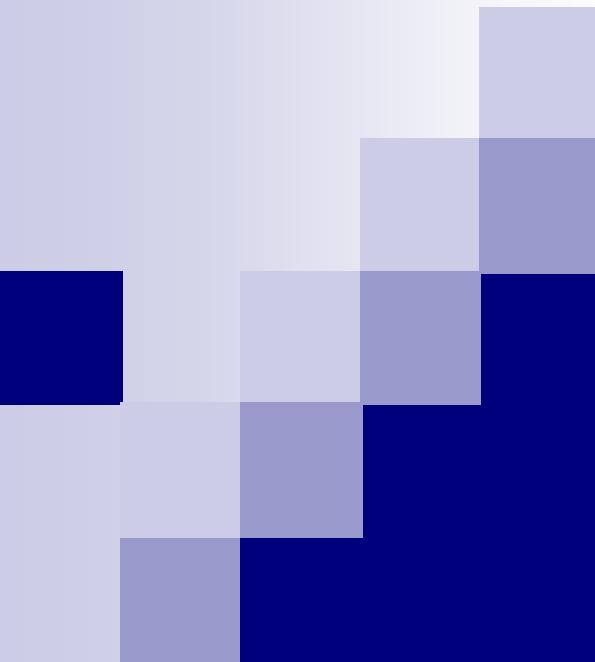


Conclusion and frontiers



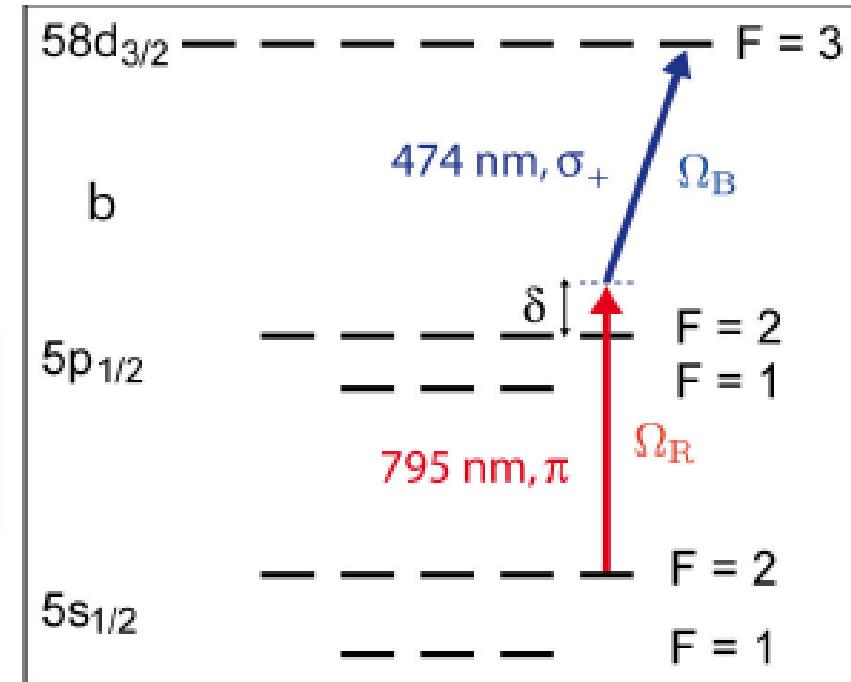
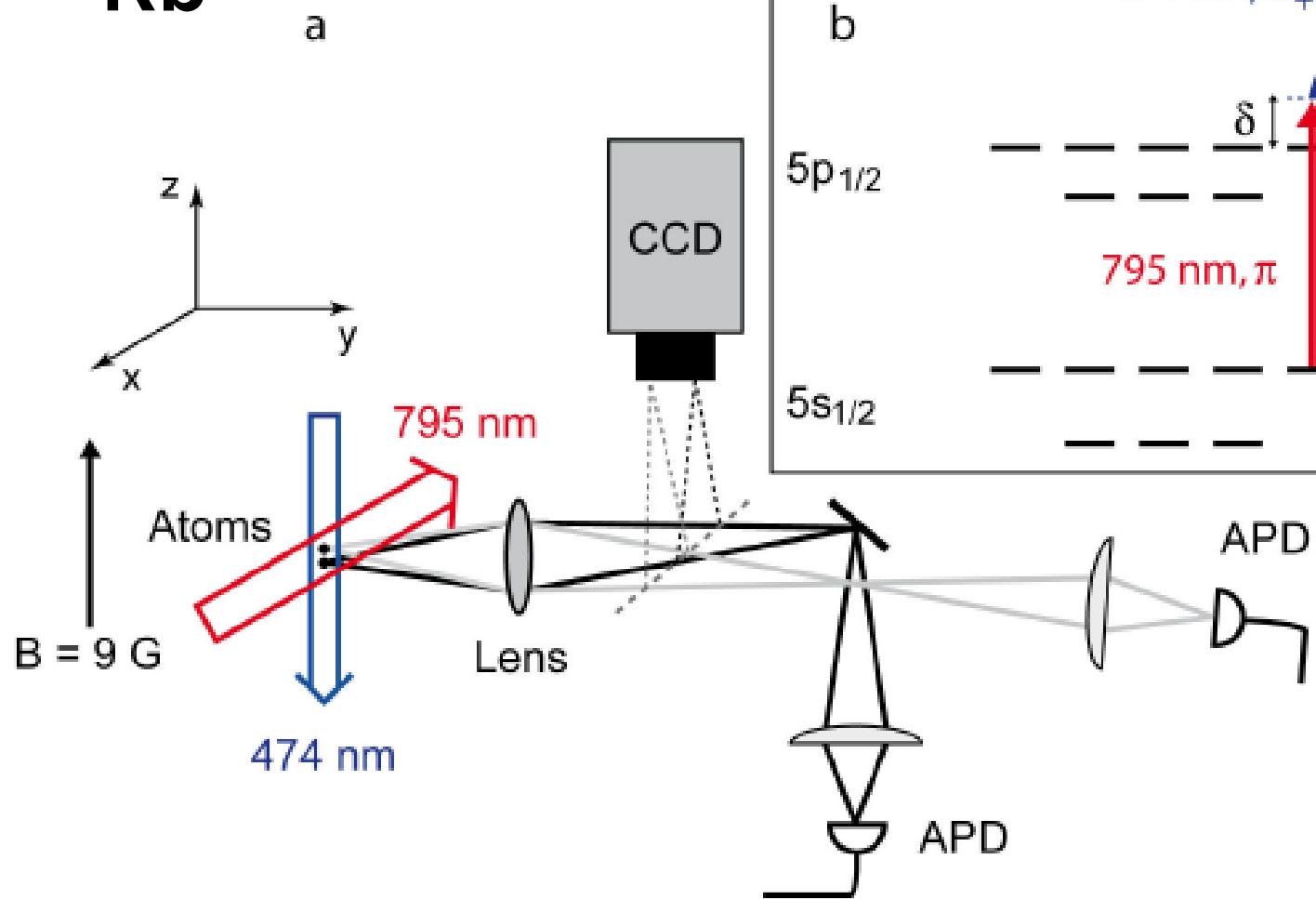
Dipole blockade at Förster resonance

The case of two atoms: conditional excitation (a) or collective excitation (b)



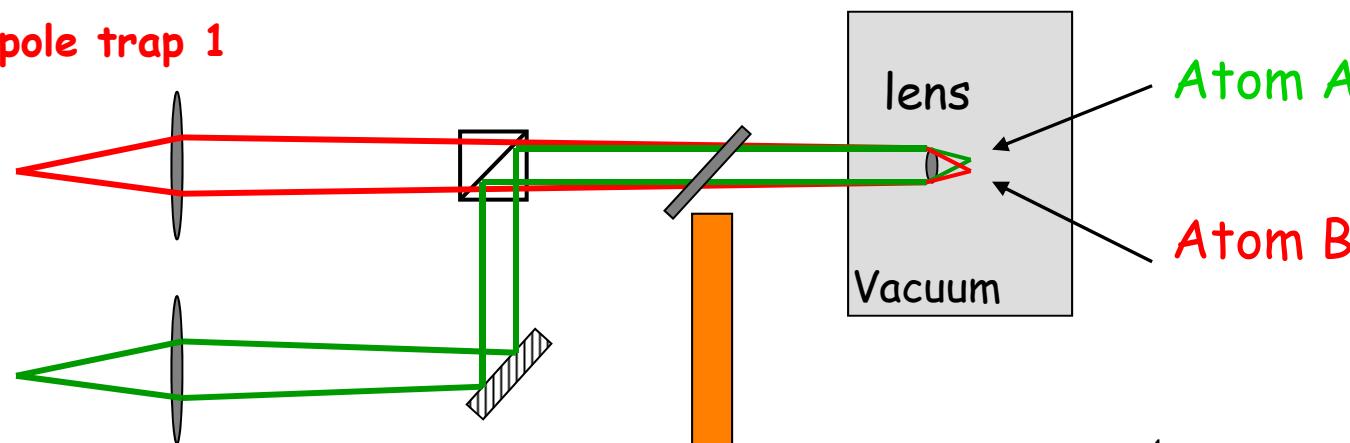
Collective excitation in the dipole blockade regime

Rb

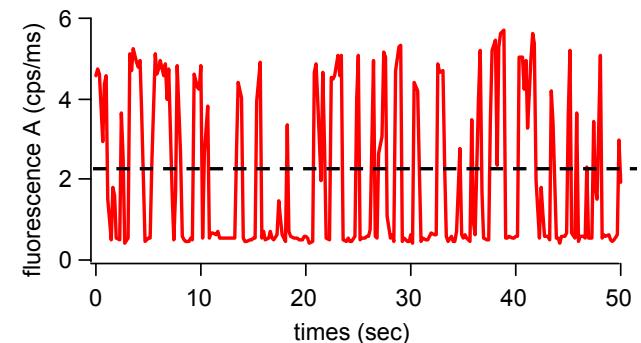
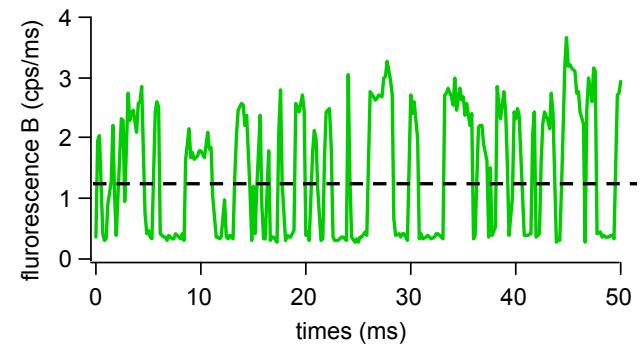
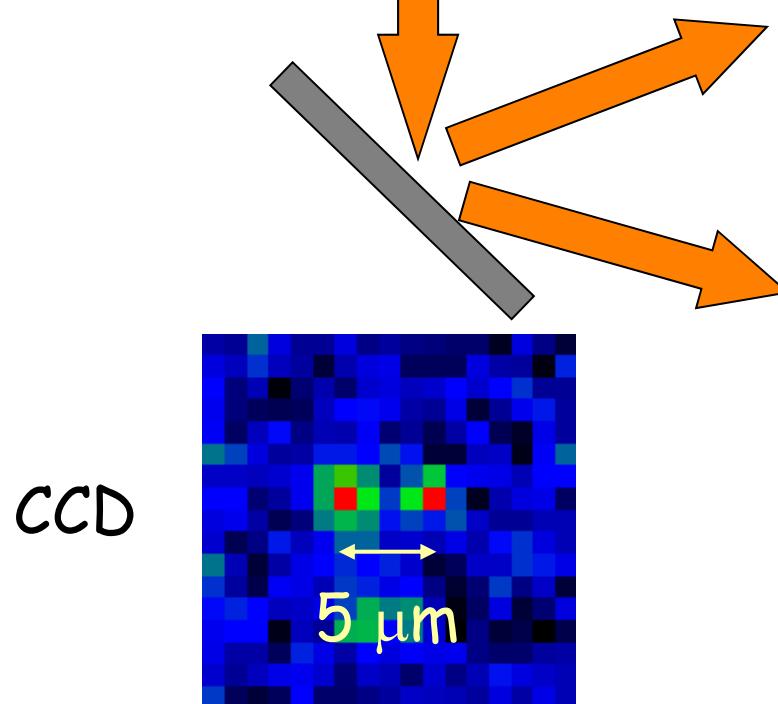


Detecting and "heralding" two single trapped atoms

Dipole trap 1



Dipole trap 2



Experimental protocol

1. Trap 2 atoms in 2 tweezers and optically pump them
2. Excite the two atoms
3. Measure if they are still trapped after the excitation

Repeat 100 times

Atom A : 0, 1, 0, 1, 0, 0, 0, 1, 1, ...

Atom B : 0, 1, 1, 1, 0, 0, 1, 1, 0, ...

Experimental protocol

1. Trap 2 atoms in 2 tweezers and optically pump them
2. Excite the two atoms
3. Measure if they are still trapped after the excitation

Repeat 100 times

Atom A : $[0, 1, 0, 1, 0, 0, 0, 1, 1, \dots]$
Atom B : $[0, 1, 1, 1, 0, 0, 1, 1, 0, \dots]$

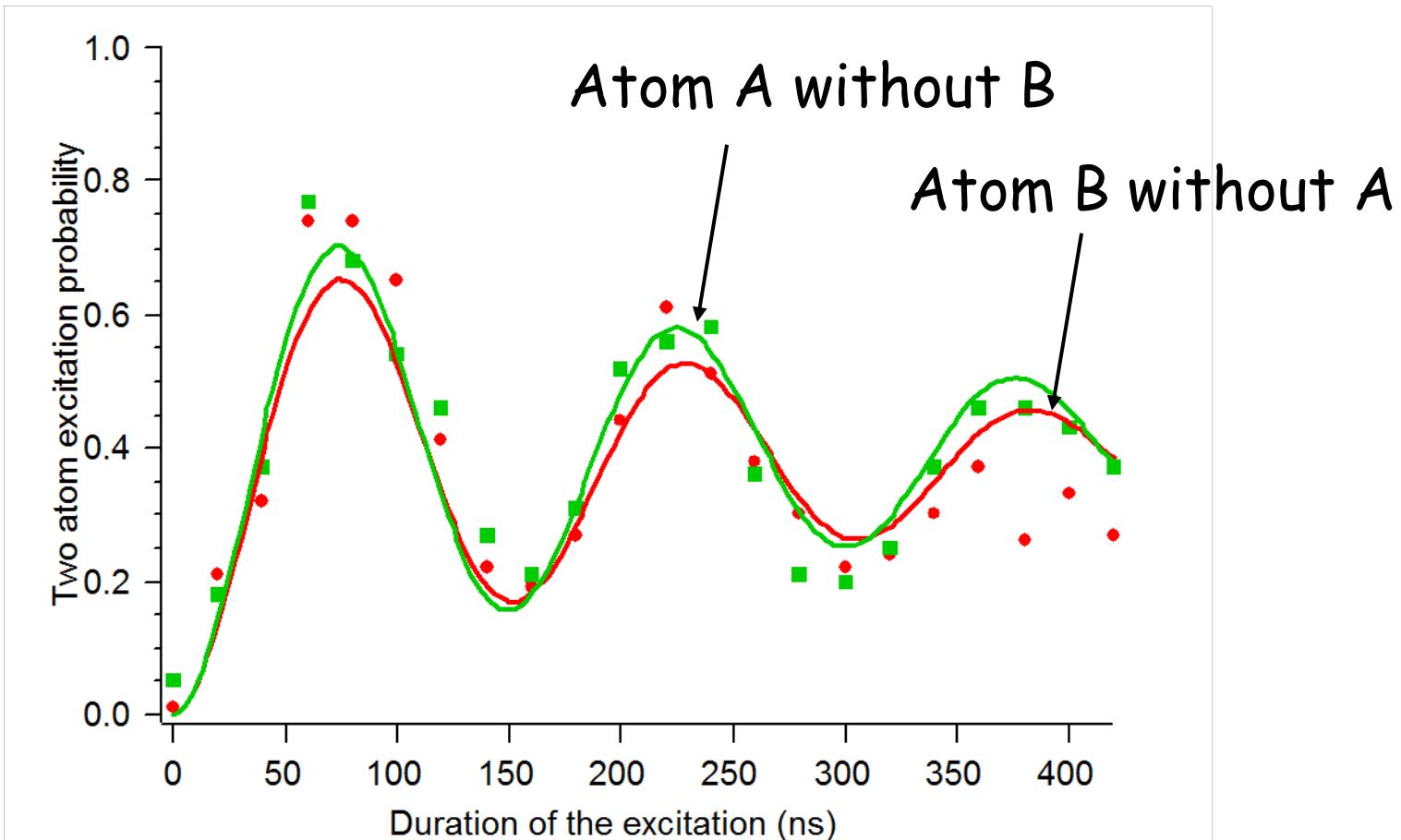
Extract

P to excite no Rydberg's

P of exciting two Rydberg's simultaneously

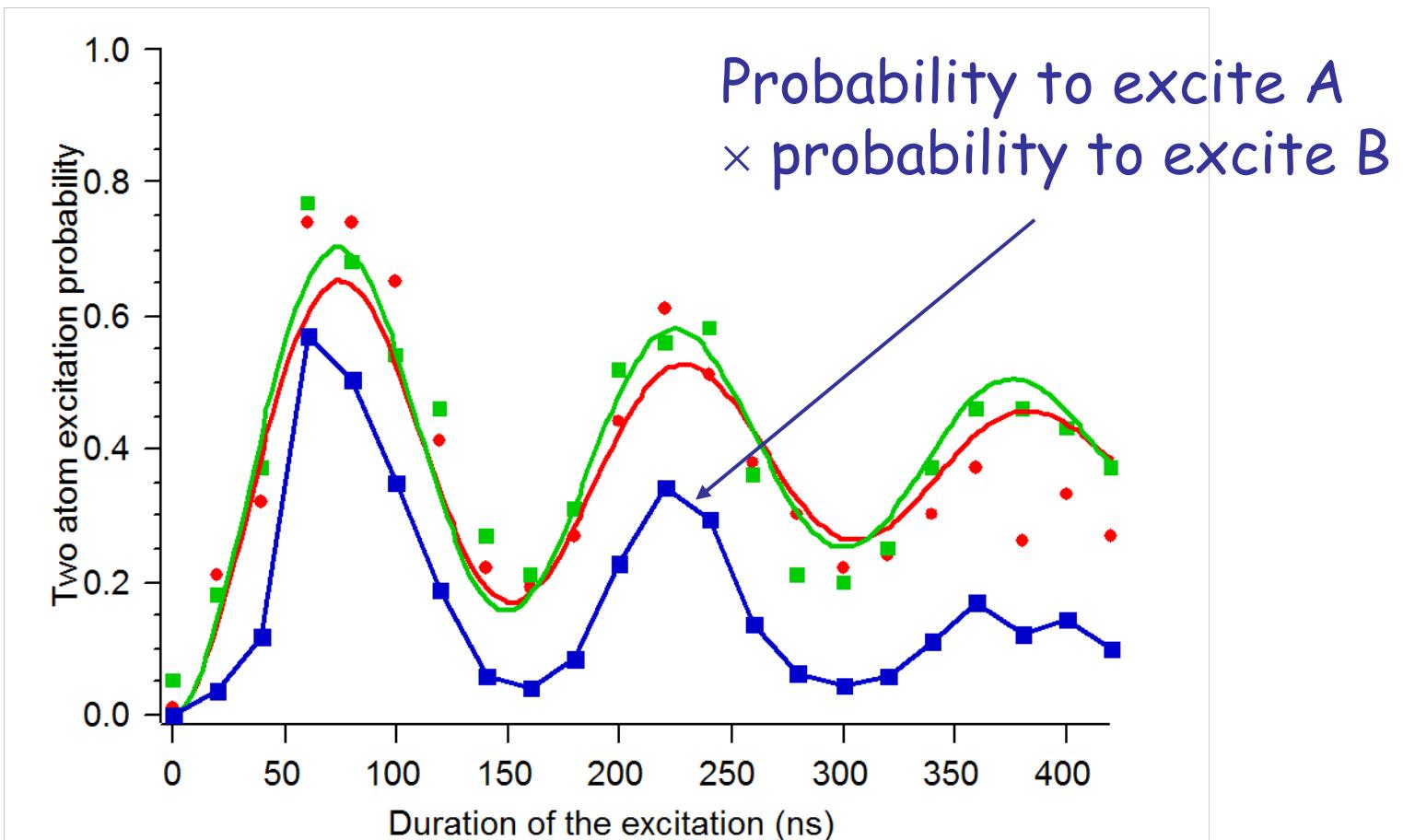
P to excite only one Rydberg

Excitation of two atoms at $R = 18 \mu\text{m}$

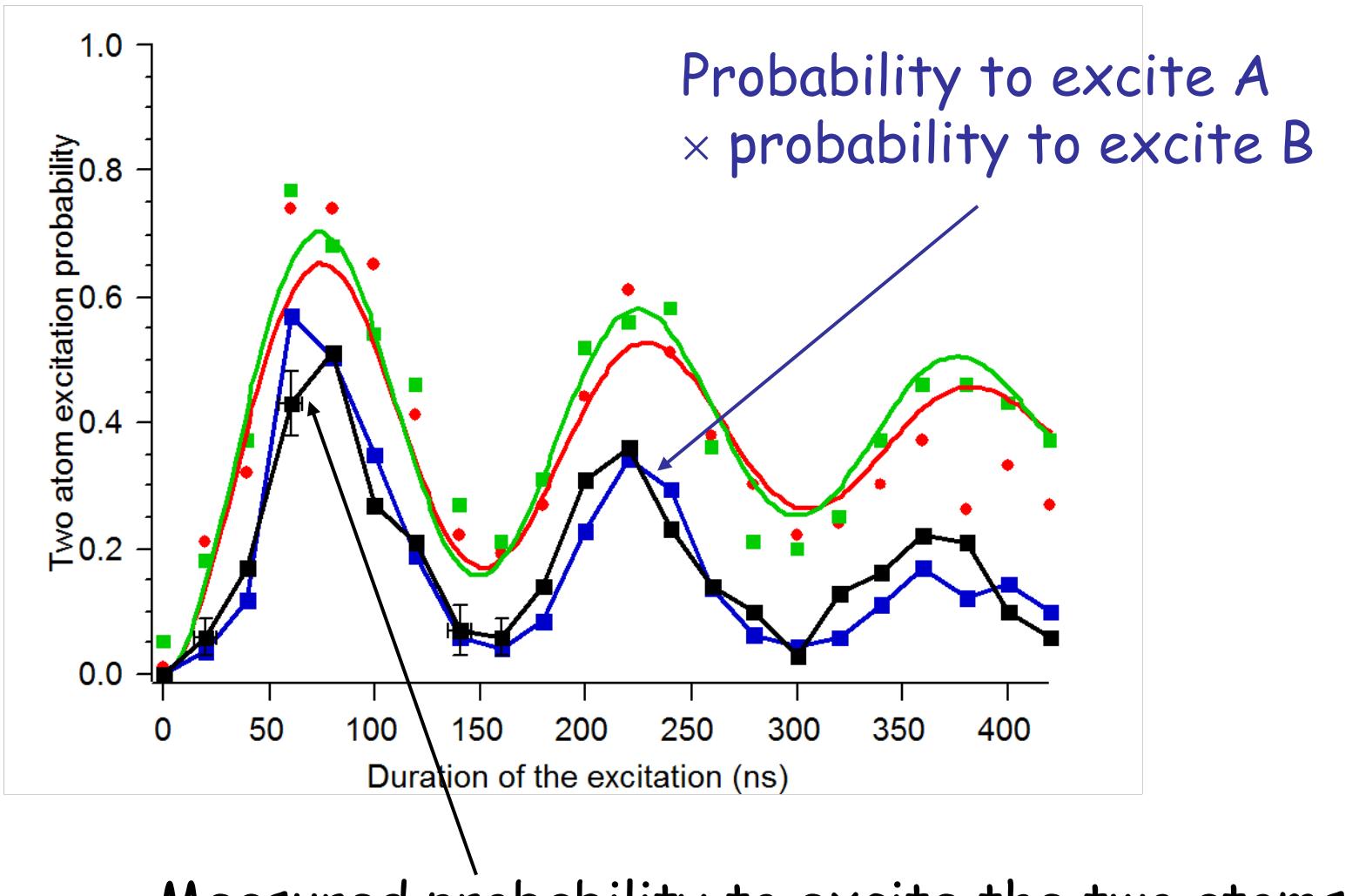


Single atom Rabi oscillation
between ground and Rydberg state

Excitation of two atoms at $R = 18 \mu\text{m}$

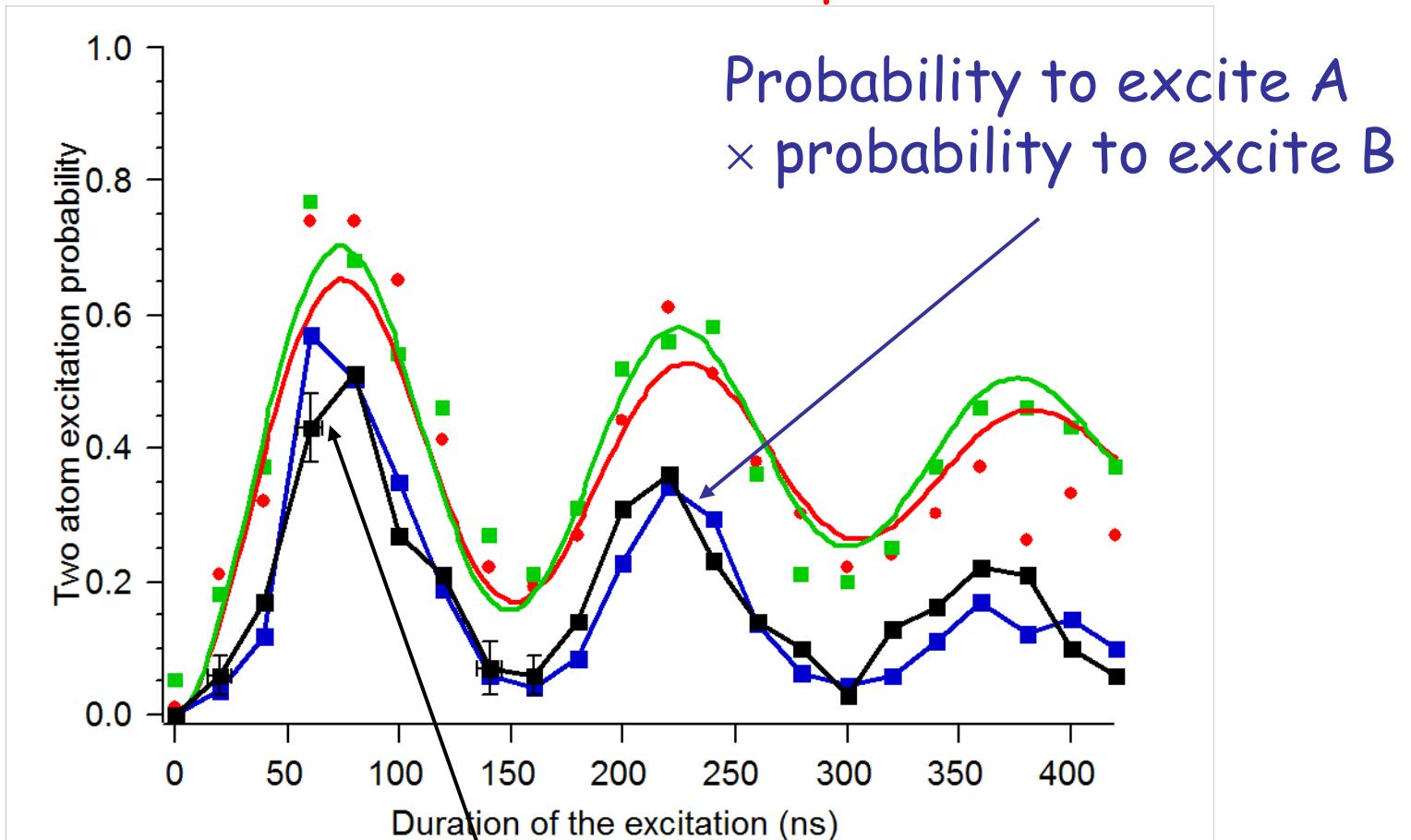


Excitation of two atoms at $R = 18 \mu\text{m}$



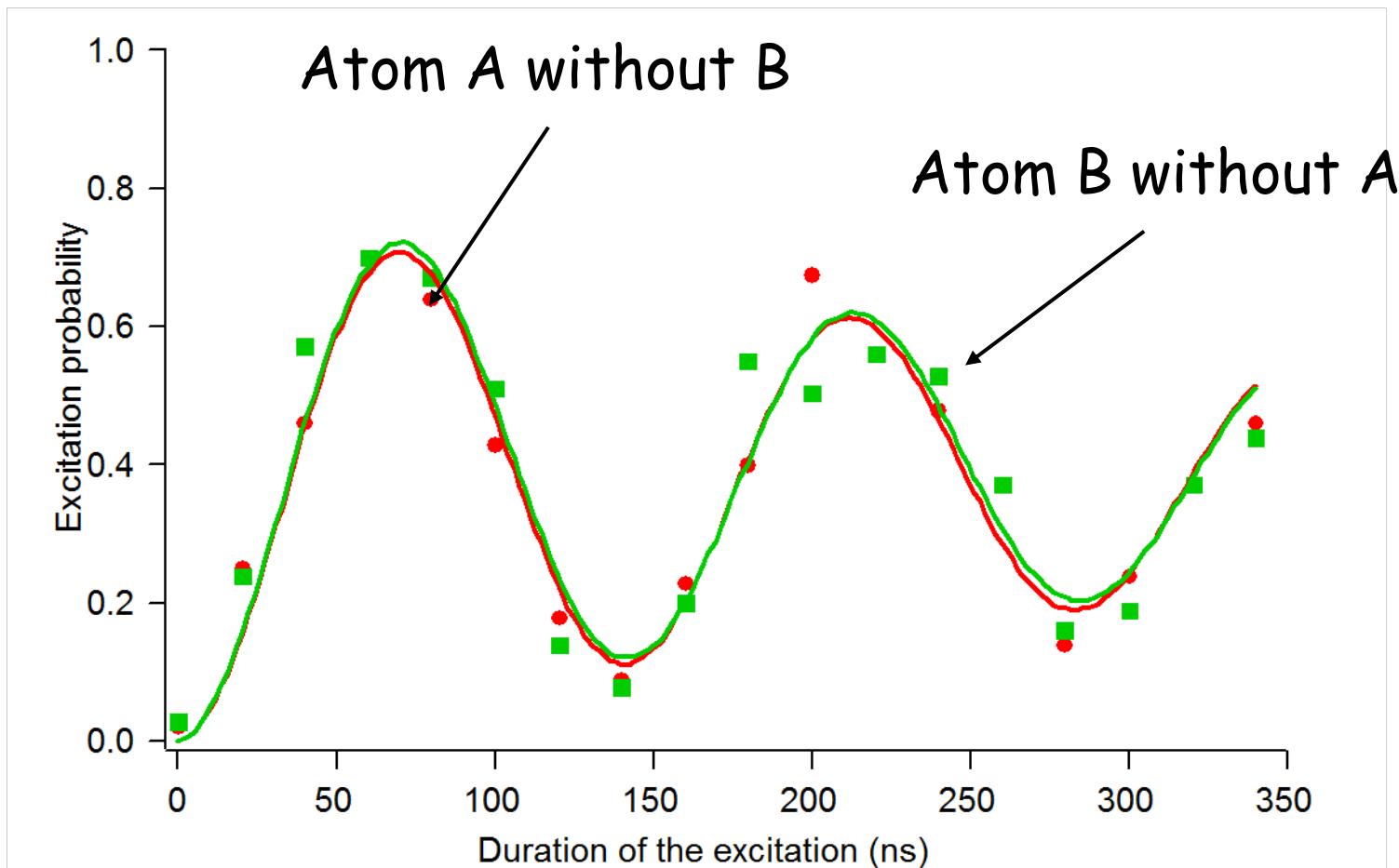
Excitation of two atoms at $R = 18 \mu\text{m}$

The atoms are « independent »

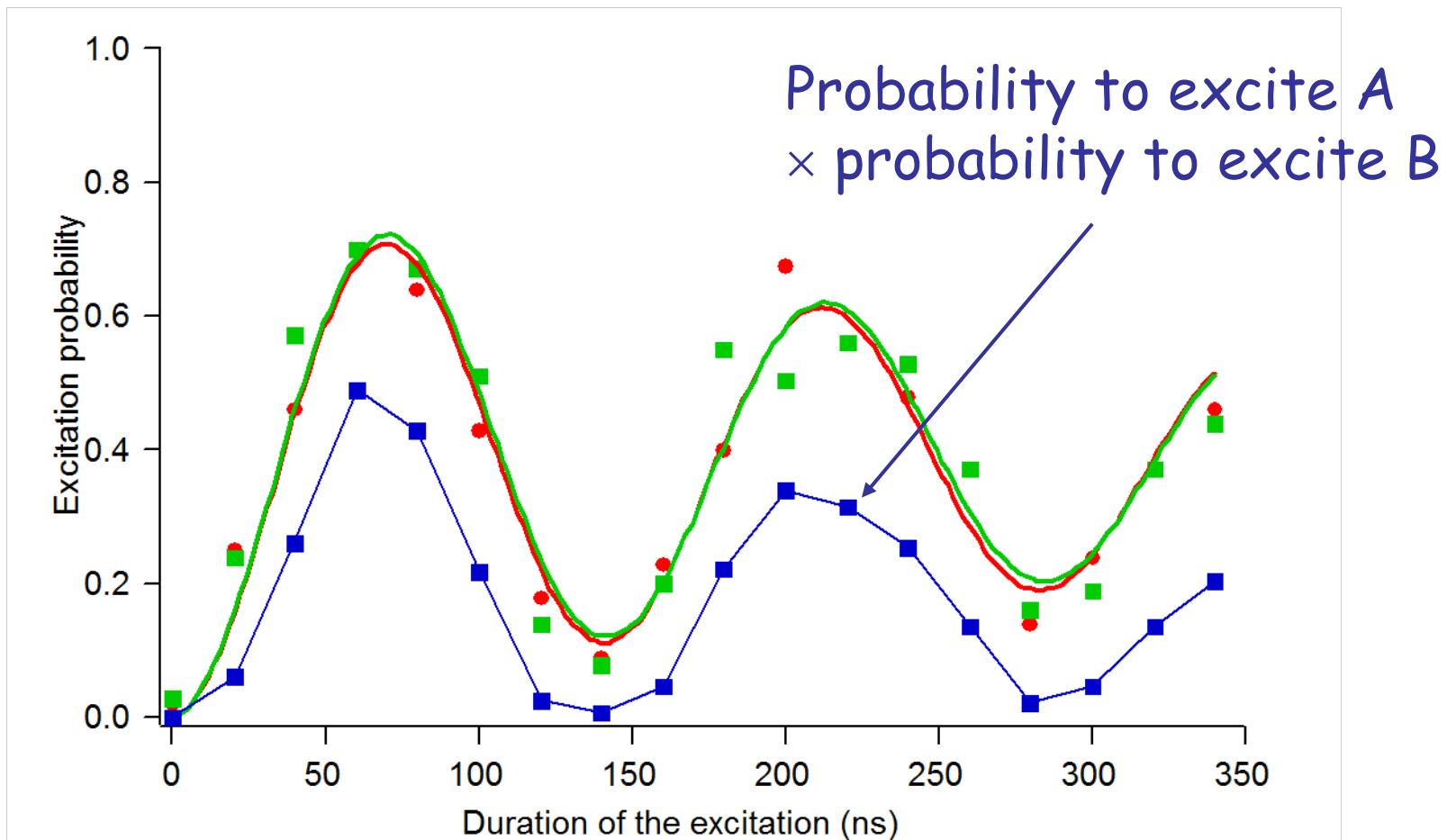


Measured probability to excite the two atoms

Excitation of two atoms at $R = 3.6 \mu\text{m}$

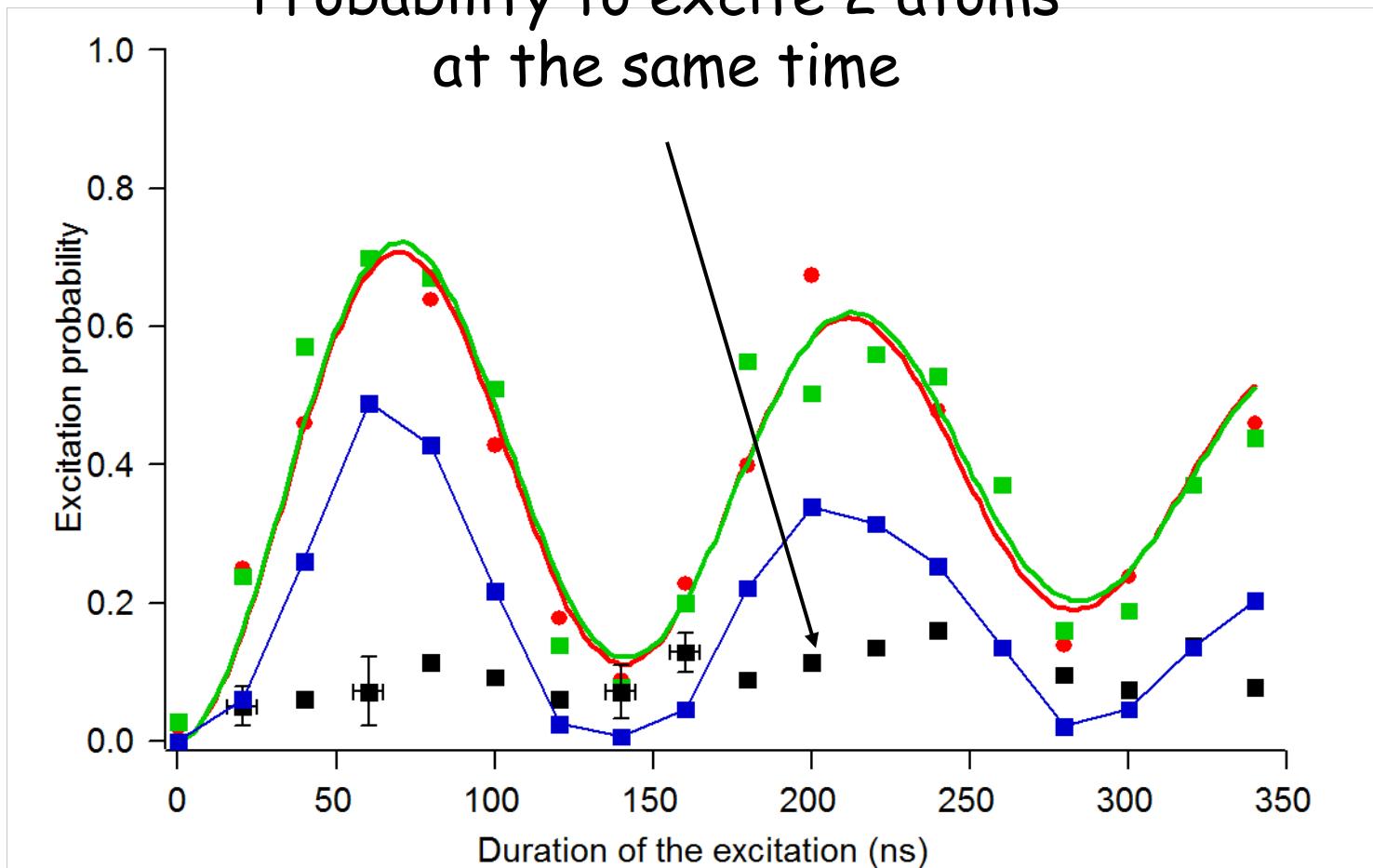


Excitation of two atoms at $R = 3.6 \mu\text{m}$



Excitation of two atoms at $R = 3.6 \mu\text{m}$

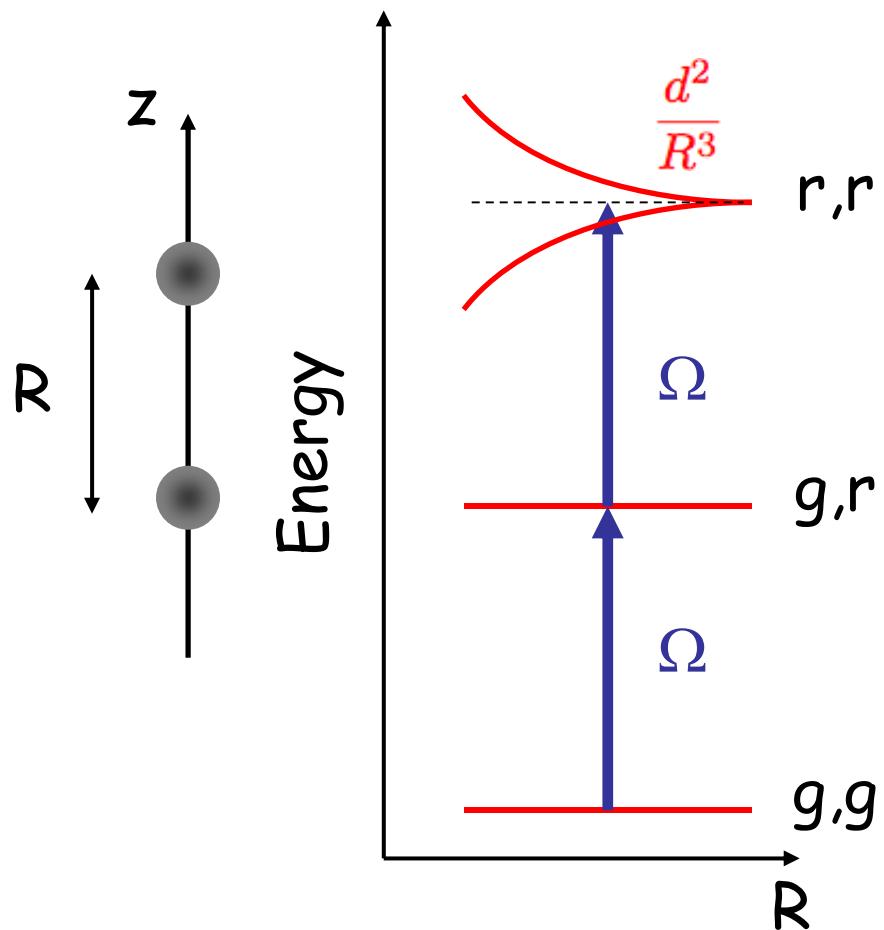
Probability to excite 2 atoms
at the same time



« Blockade » range

Two atoms excited to
 $|58d_{3/2} : M_J = 3/2\rangle$

$\Delta = 7 \text{ MHz}$



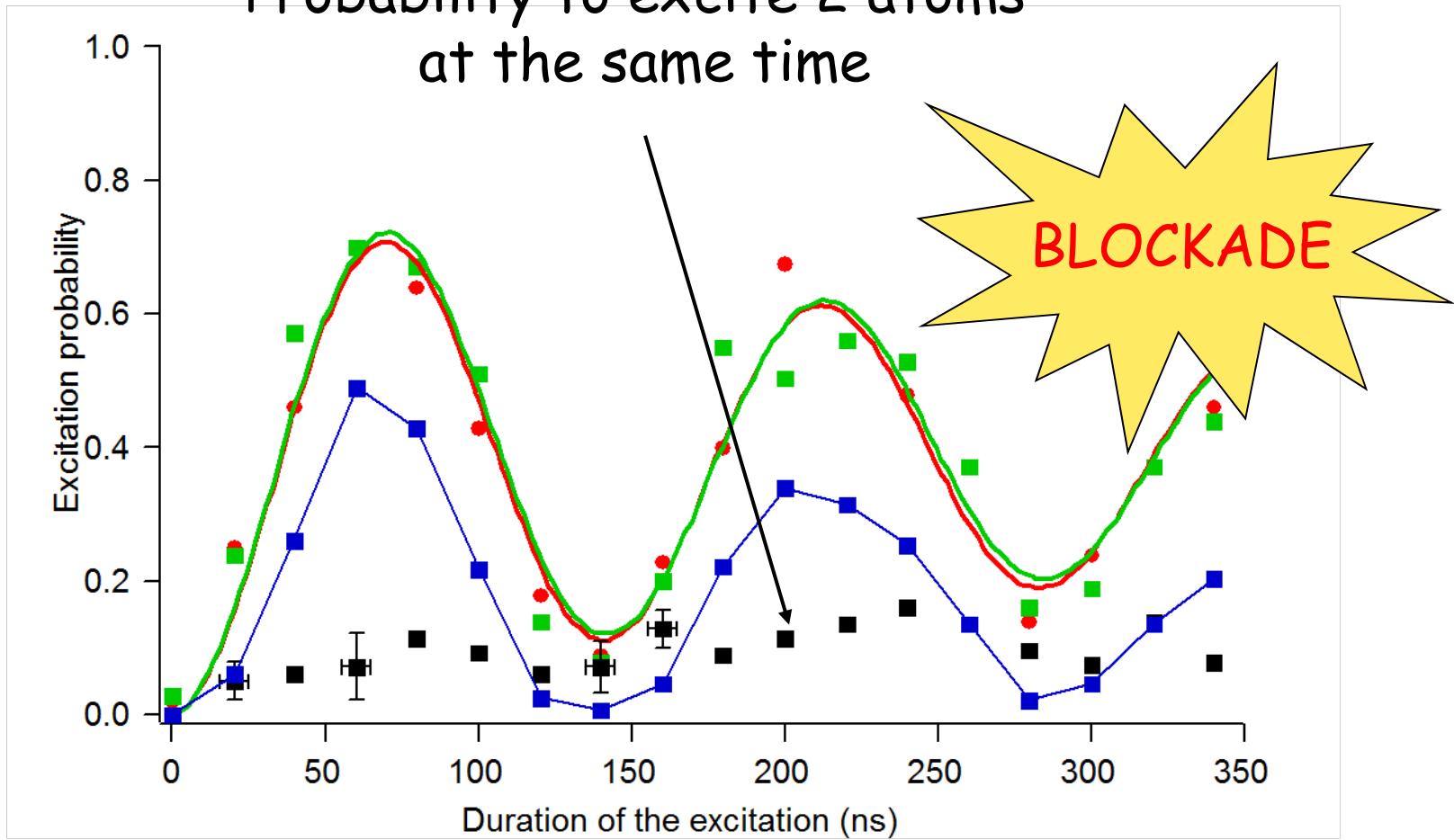
Blockade stops when

$$\hbar\Omega \approx \frac{d^2}{R^3}$$

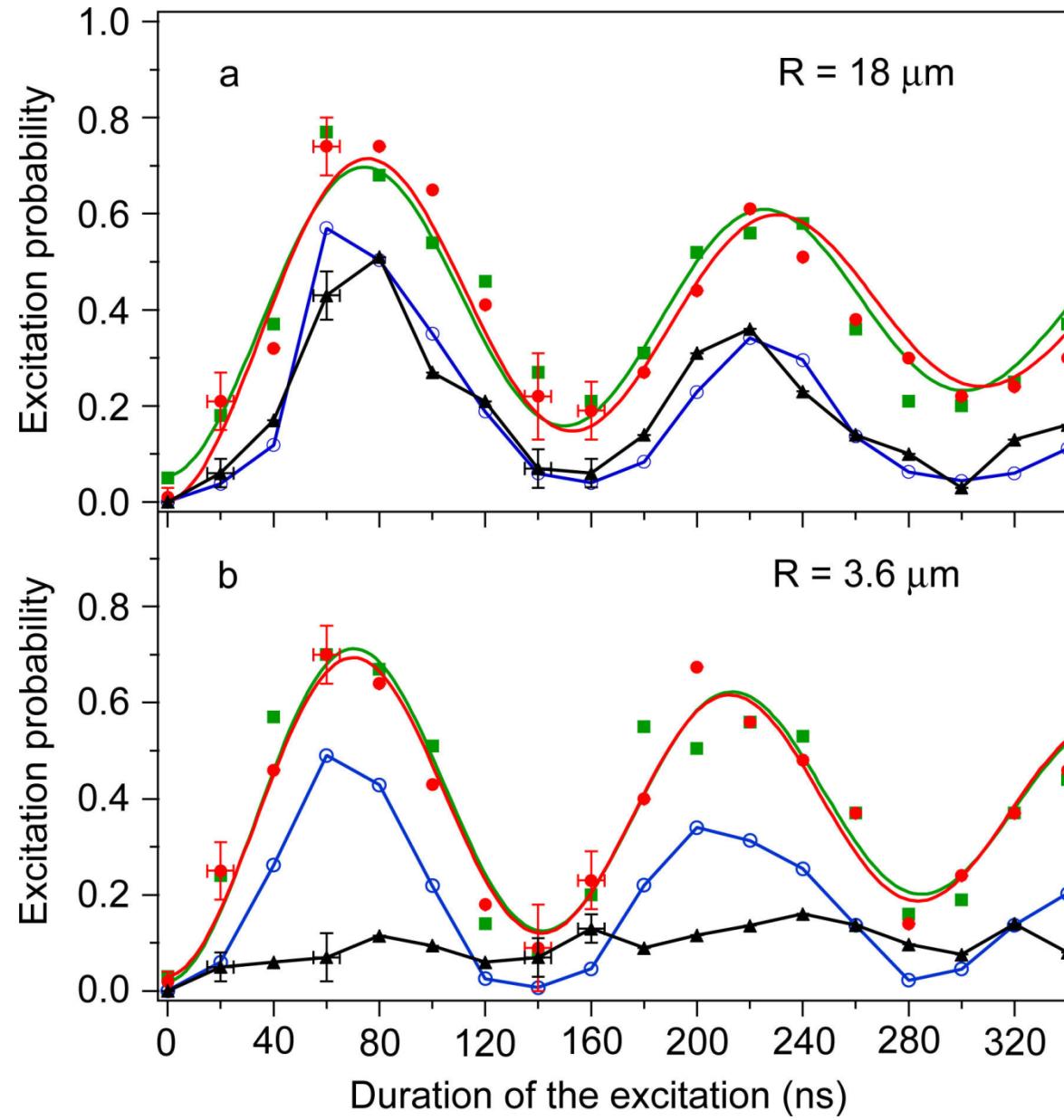
$$\begin{aligned}\Omega &= 2\pi \times 7 \text{ MHz} \\ \Rightarrow R_{\max} &= 8 \mu\text{m}\end{aligned}$$

Excitation of two atoms at $R = 3.6 \mu\text{m}$

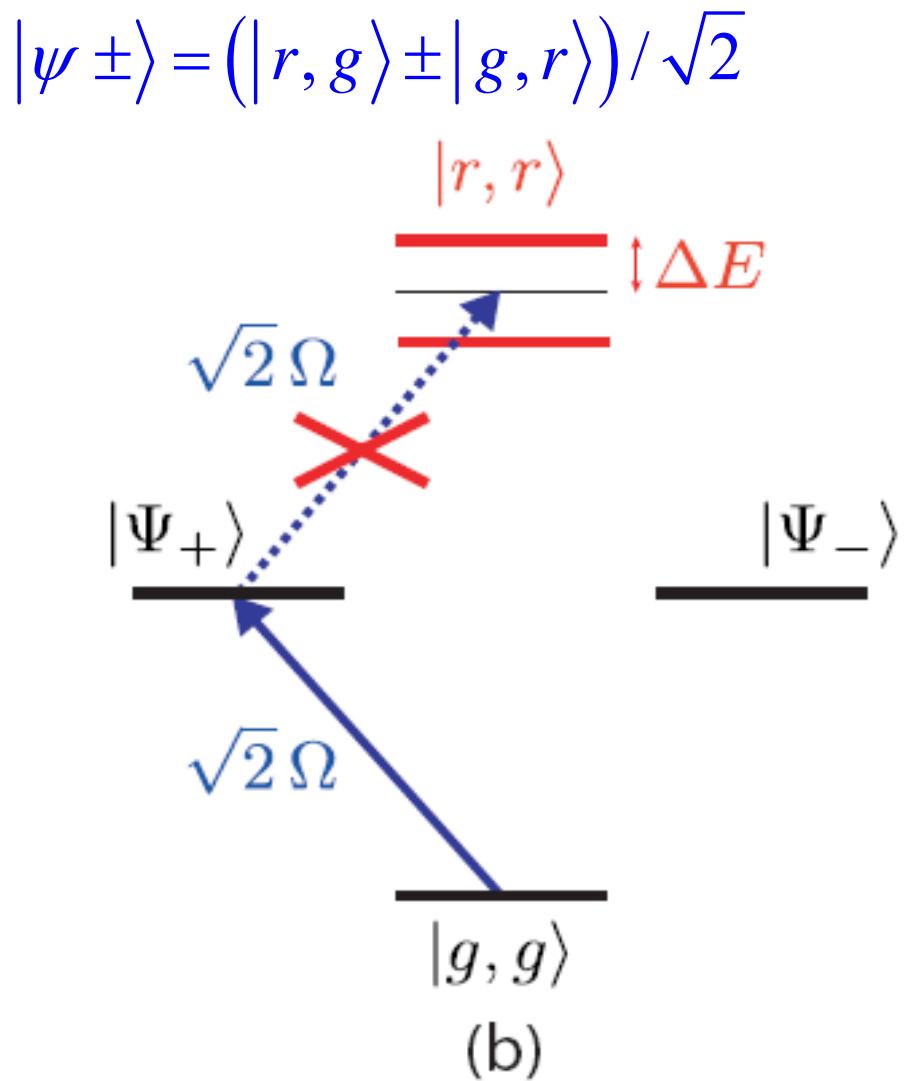
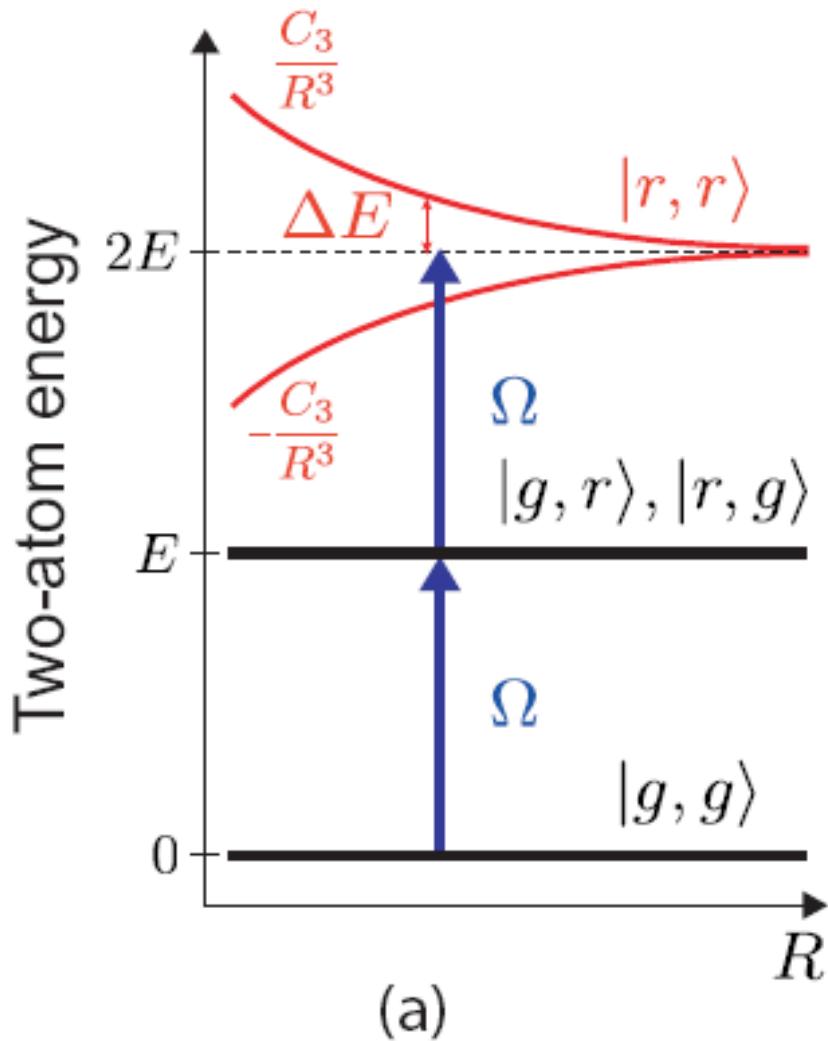
Probability to excite 2 atoms
at the same time



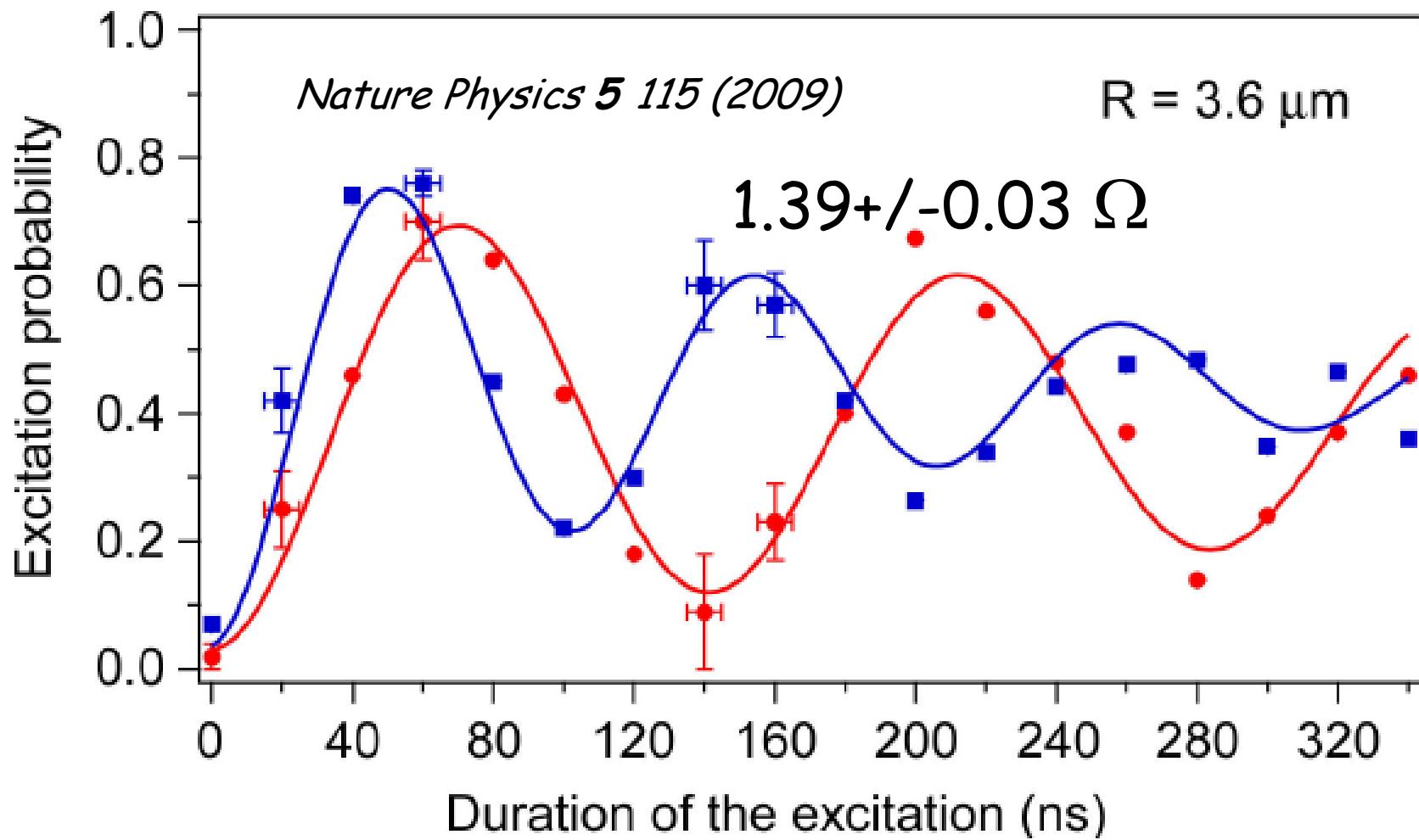
« Observation of collective excitation of two individual atoms in the Rydberg blockade regime », A. Gaëtan, Y. Miroshnychenko, T. Wilk, A. Chotia, M. Viteau, D. Comparat, P. Pillet, A. Browaeys, and P. Grangier, *Nature Physics* 5, 115 (2009).



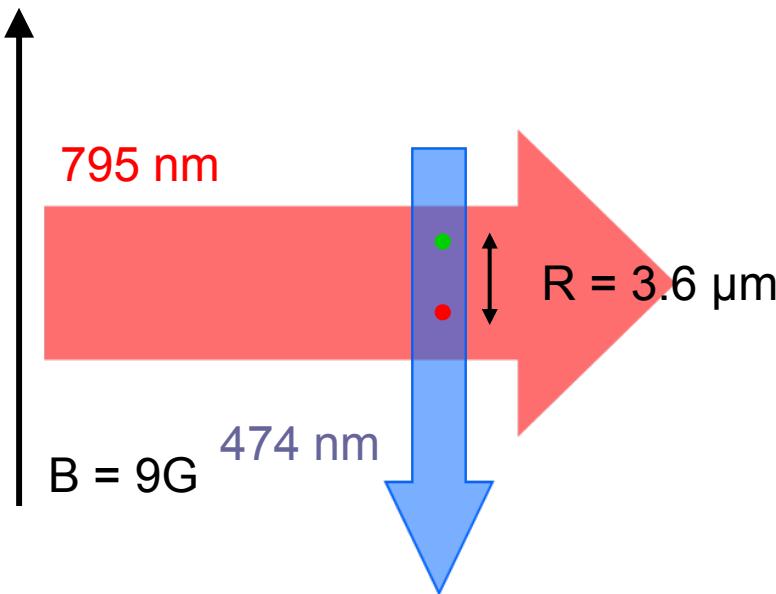
Rb : Förster résonance ($58d_{3/2}$, $58d_{3/2}$) et ($60p_{1/2}$, $56f_{5/2}$)



Collective excitation: Alpha Gaëtan, Yevhen Miroshnychenko,
Tatjana Wilk, Amodsen Chotia, Matthieu Viteau, Daniel Comparat,
Pierre Pillet, Antoine Browaeys and Philippe Grangier

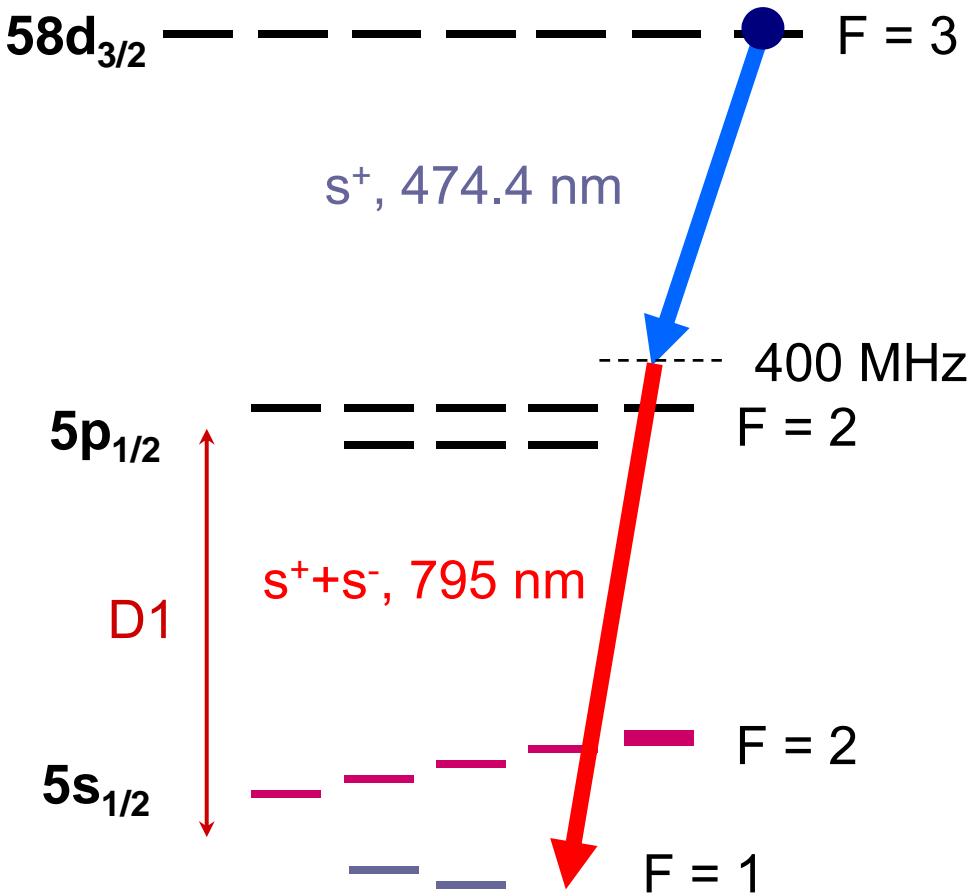


To prepare a quantum bit

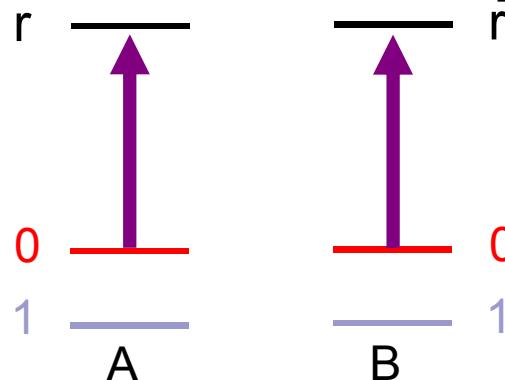


$$\frac{1}{\sqrt{2}}(|r, 1\rangle + |1, r\rangle)$$

$$\rightarrow |\psi_B\rangle = \frac{1}{\sqrt{2}}(|1, 0\rangle + |0, 1\rangle)$$



Scalable quantum gate



$|1\ 1\rangle$
 $|0\ 1\rangle$
 $|1\ 0\rangle$
 $|0\ 0\rangle$

Phase



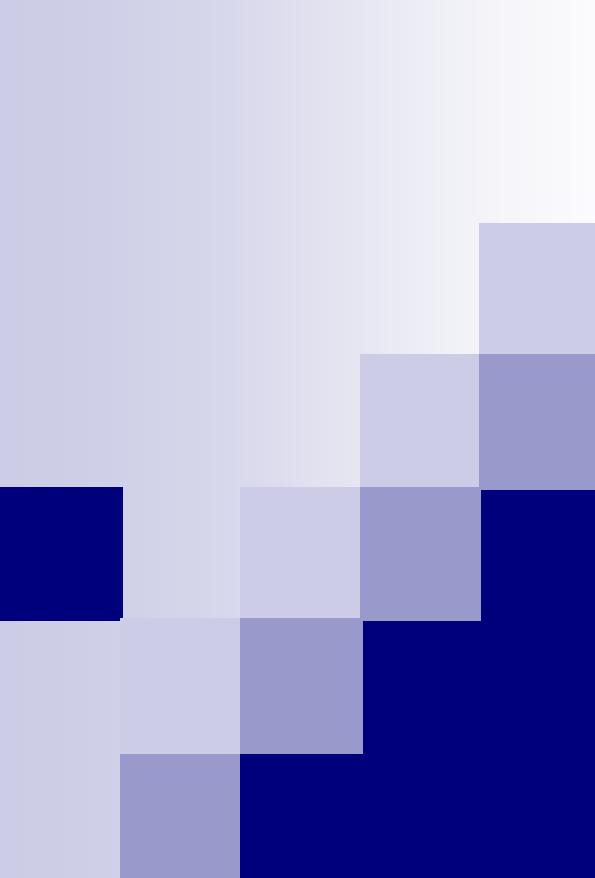
$|1\ 1\rangle$
 $-|0\ 1\rangle$
 $-|1\ 0\rangle$
 $-|0\ 0\rangle$

π - excitation on A
 2π - excitation on B
 π - excitation on A

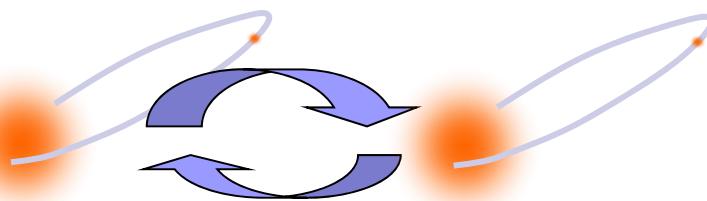
Blockade

- * Requires « addressability ». Very fast gate
- * Can (easily ?) be turned into a CNOT gate

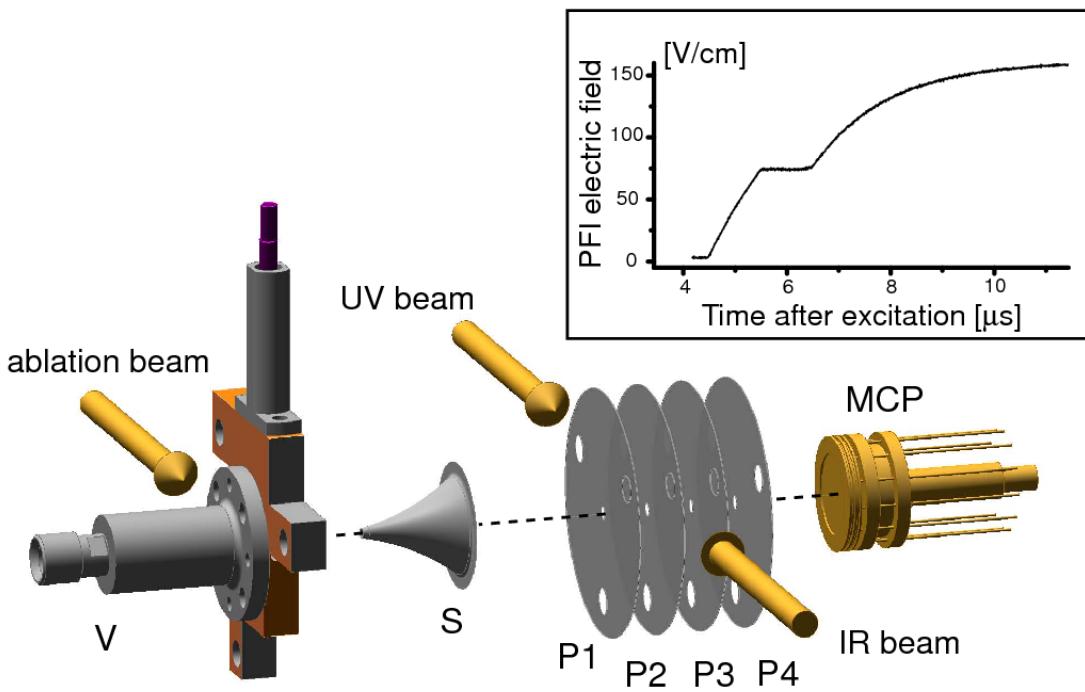
Work in progress... (U. Wisconsin, Institut d'Optique)



Foster resonance: Collisions, Landau-Zener transitions, or Interactions



Experiments with a Na supersonic beam

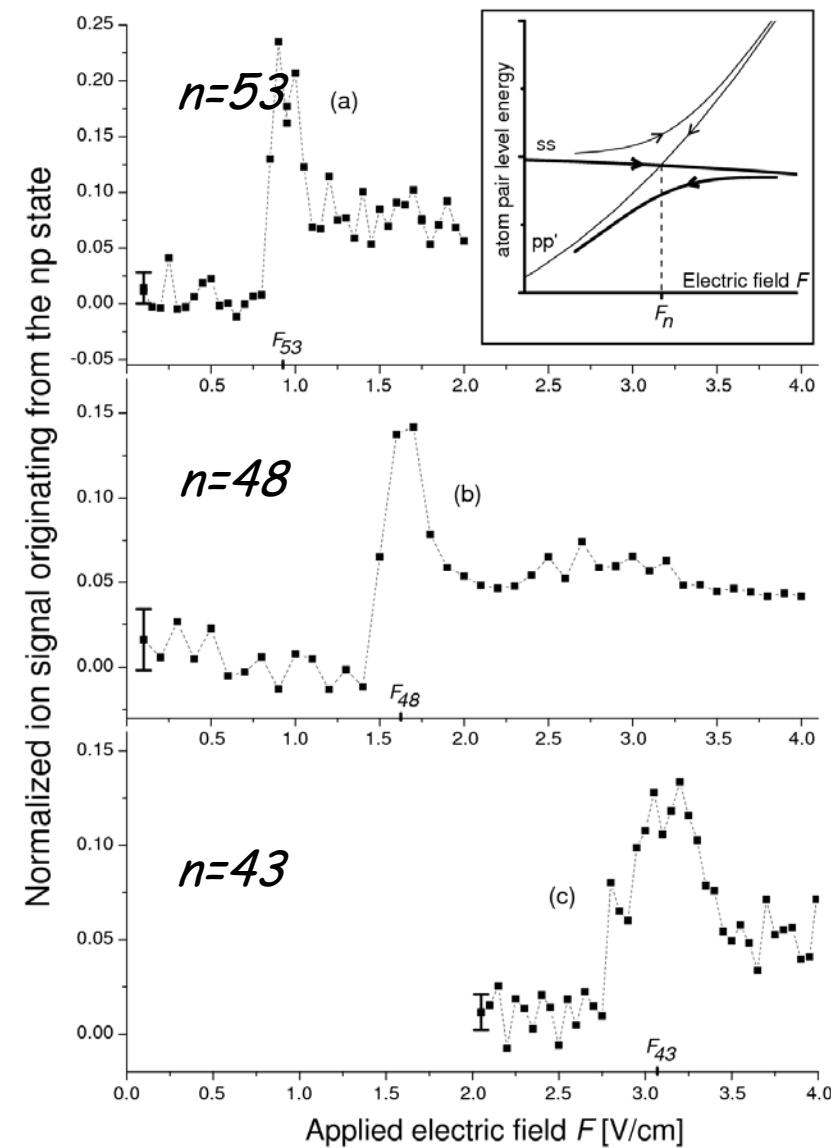
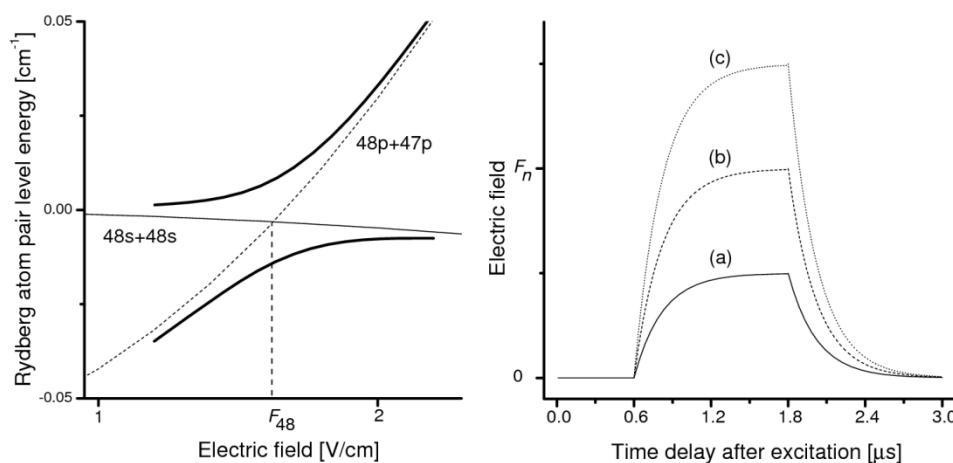


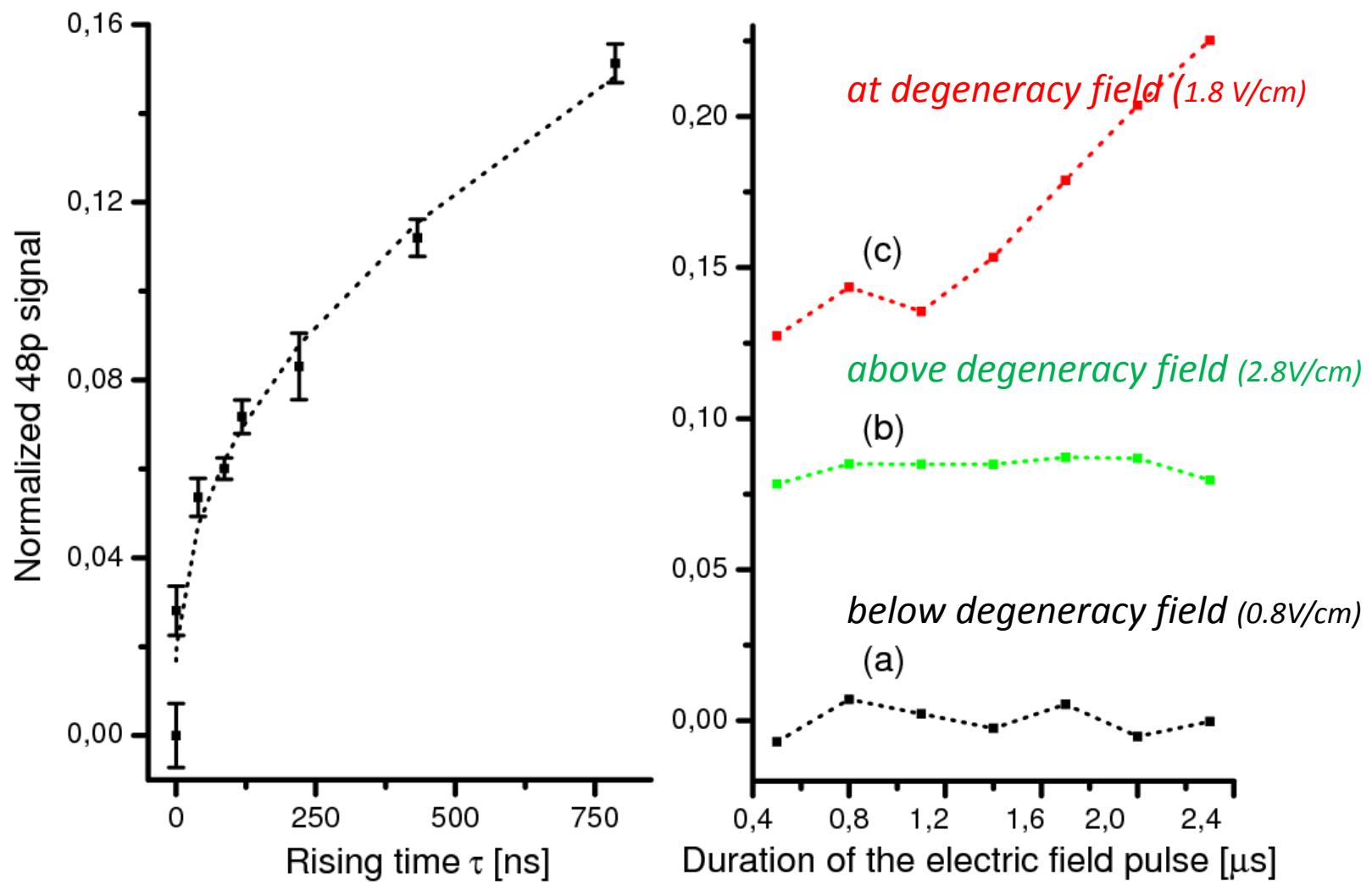
$$\langle v \rangle = 1900 \text{ m/s}$$
$$T_{\text{trans}} = 1 \text{ K}$$

Excitation
 $3s \rightarrow 4p_{3/2} \rightarrow ns$

Föster resonance
 $ns + ns \rightarrow np + (n-1)p$

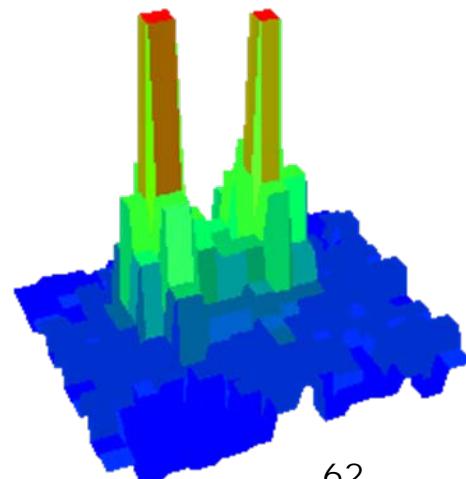
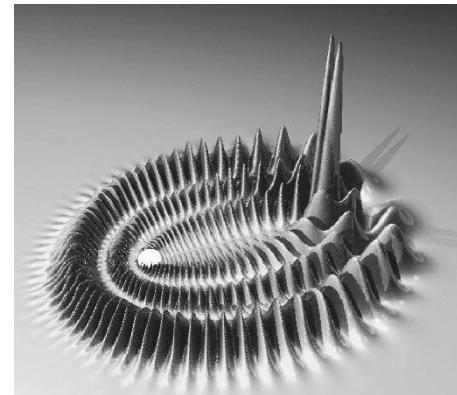
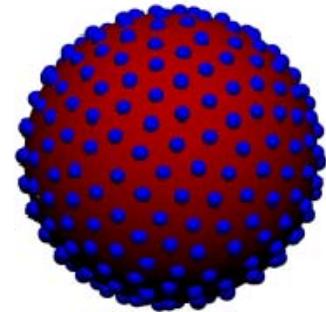
Landau-Zener transitions at Föster resonance





Perspectives and conclusion

- A very rich physics
-
- Penning ionization, control of the interatomic forces, evolution towards an ultracold plasmas, highly correlated plasmas...
- Application of dipole blockade for quantum gates : P. Gangrier, A. Browaeys *et al.* entanglement of two atoms with a fidelity of 75 %
- Landau-Zener transitions: selection of pairs, few-body effects
- Stark-Rydberg decelerator of supersonic beams
- ...



Frontier between cold Rydberg gases and ultracold plasmas

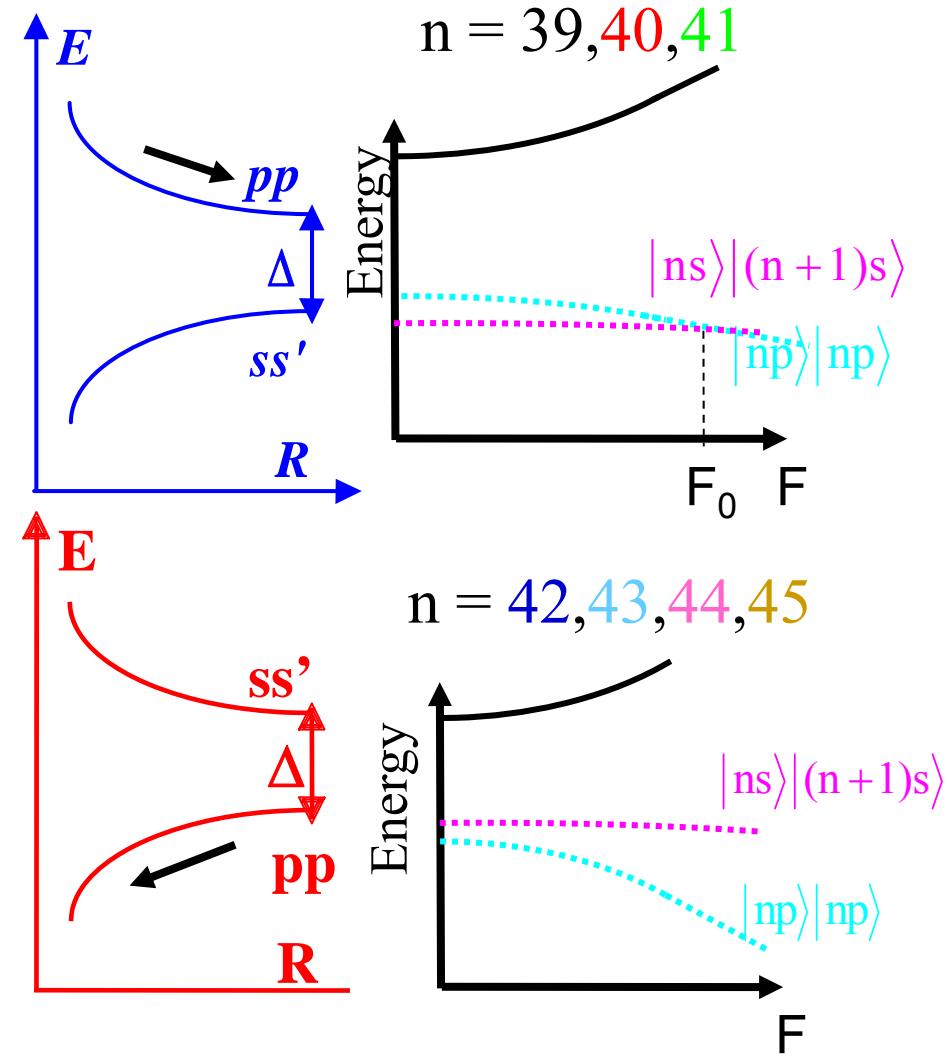
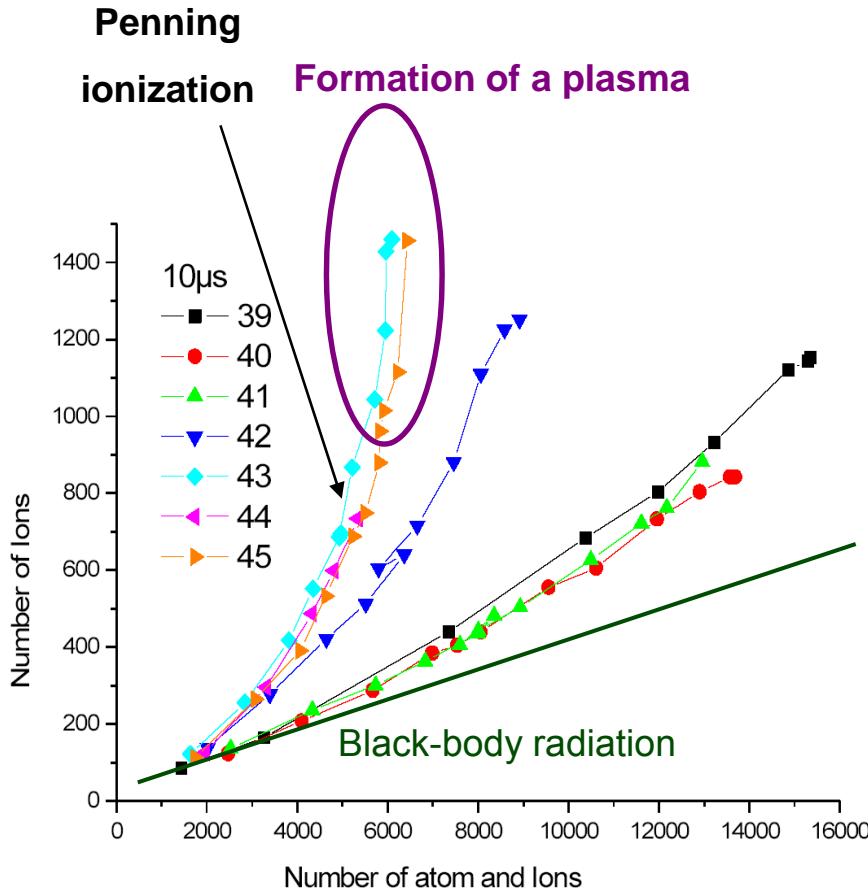
Limit of the frozen Rydberg gas picture
Dipole forces

Penning ionization



Dipole-dipole collisions (after $10\mu s$)

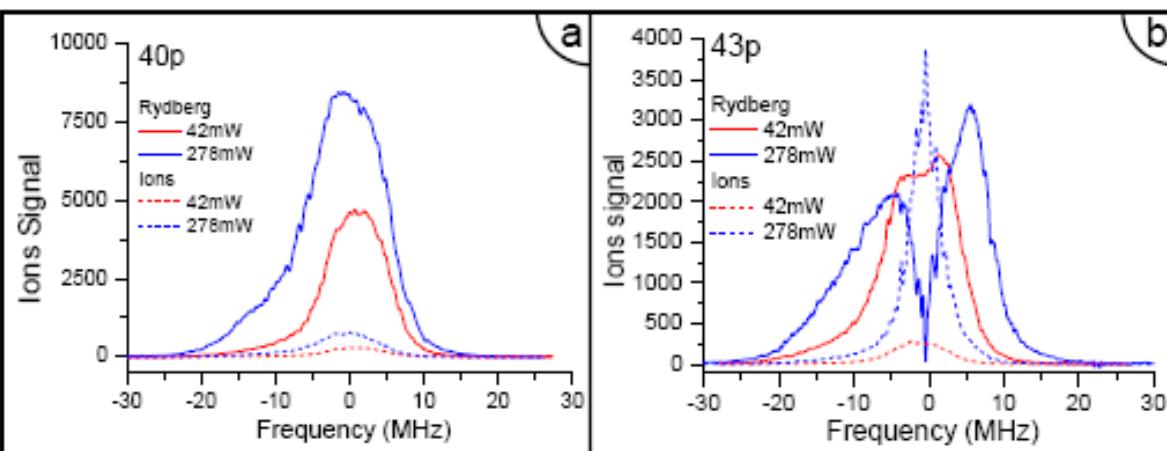
- Excitation of $np_{3/2}$ at zero field ($F = 0V/cm$)
van der Waals or second order dipole-dipole coupling



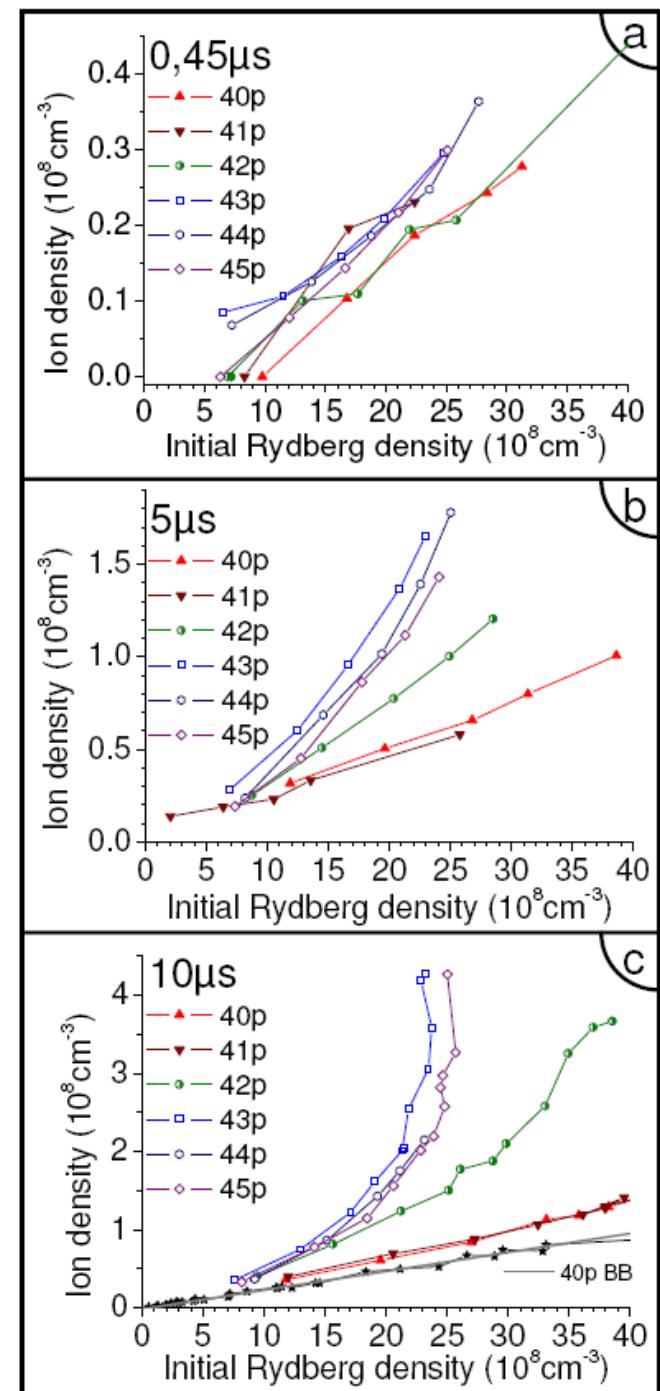


From 40p to 43p: Spectacular change in the behavior of the Rydberg gas

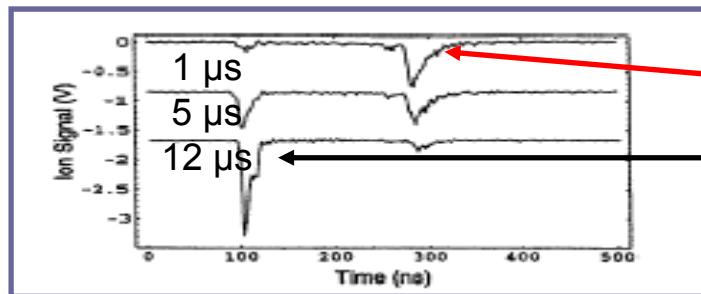
Viteau et al. PRA 78 040704(R) (2008)



For 43p: The pairs of close atoms collide to form an ion space charge which can trap the electrons, leading to avalanche ionization up to the formation of an ultracold plasma



Spontaneous evolution of a Rydberg atomic gas into an ultracold plasma

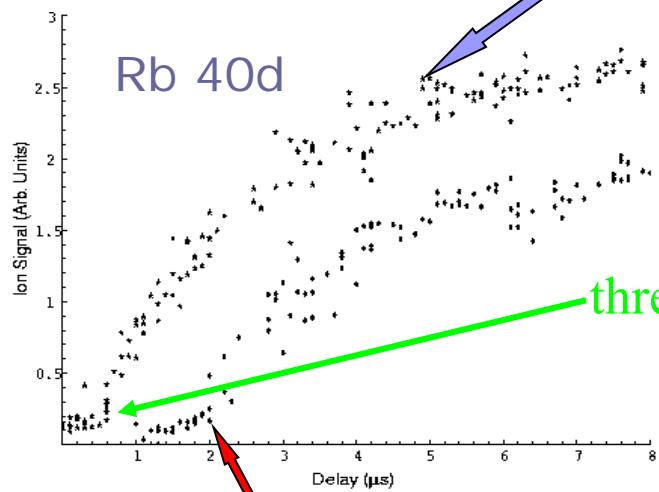


- Two signals
 - Rydberg atoms
 - Ions

PRL 85 4466 (2000)

Ion detection

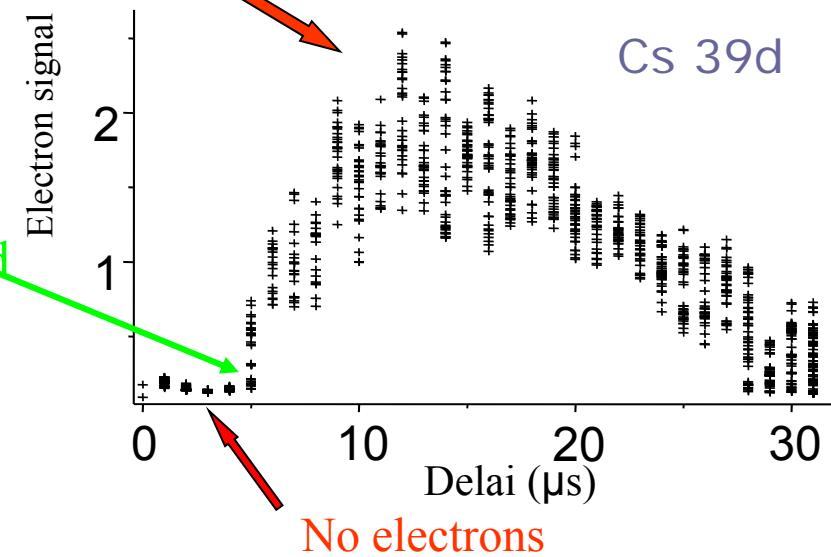
3.3 et 2.4 10^5 atoms



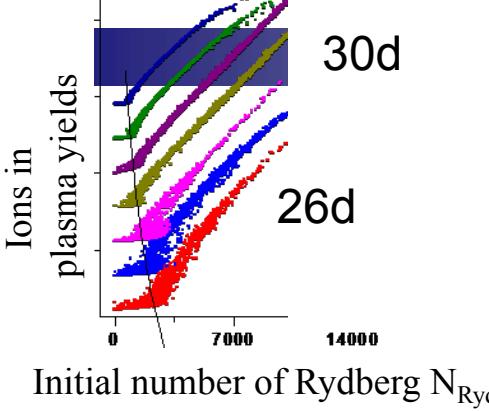
A few ions

Electron detection

Cs 39d



No electrons



Scenario

1) Ionization and ignition

Blackbody radiation

Collisions between hot and cold atoms

Collisions between cold Rydberg atoms

2) Avalanche ionization

Electrons trapped by the space charge

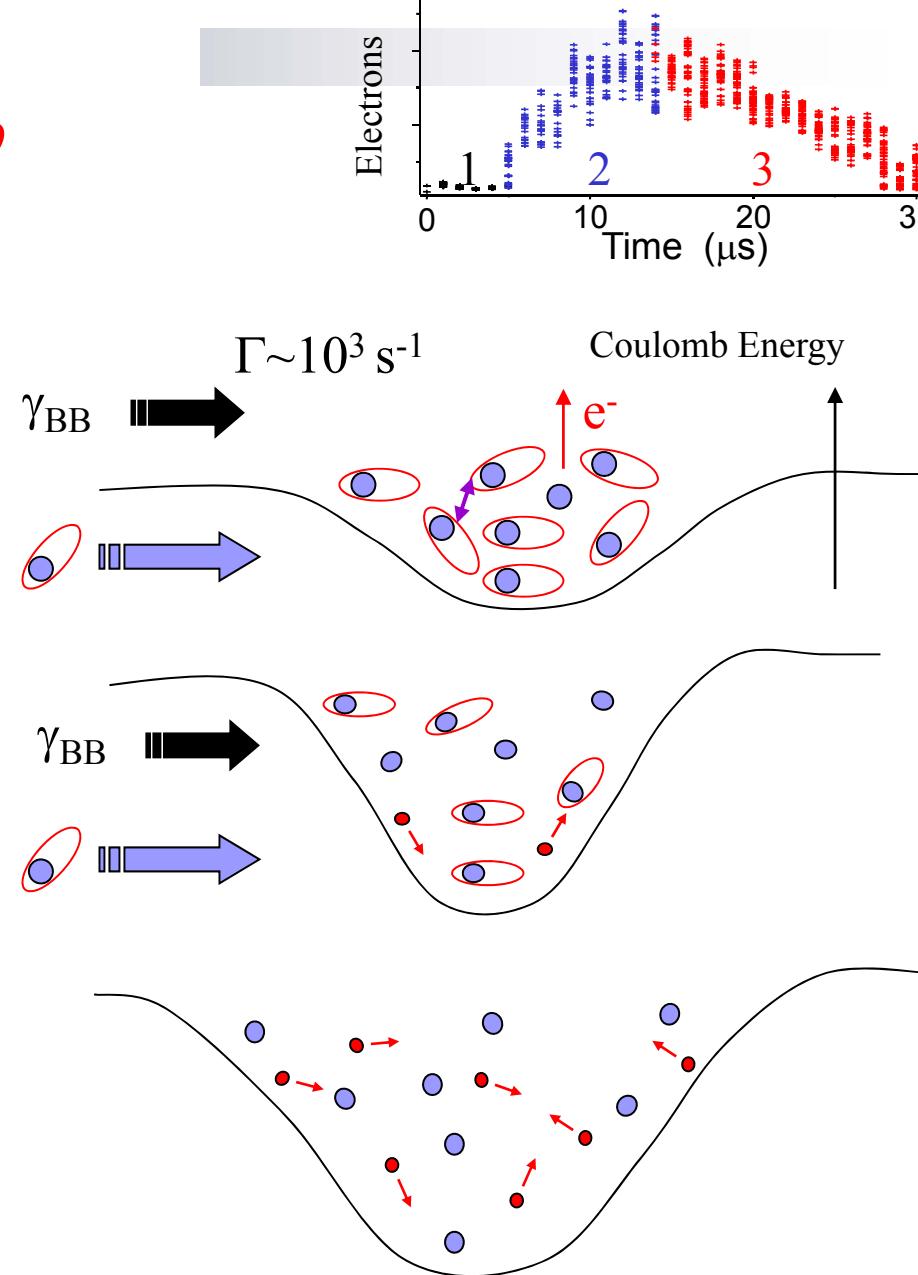
Collisions electrons – Rydberg atoms:
ionization , super-elastic collisions

3) Expansion

Electron pressure + Coulomb explosion

3-body recombination (heating)

Evaporation of electrons



Plasma parameters

$$E_{\text{cin}} \sim k_B T_e \quad E_{\text{pot}} \sim e^2/a$$

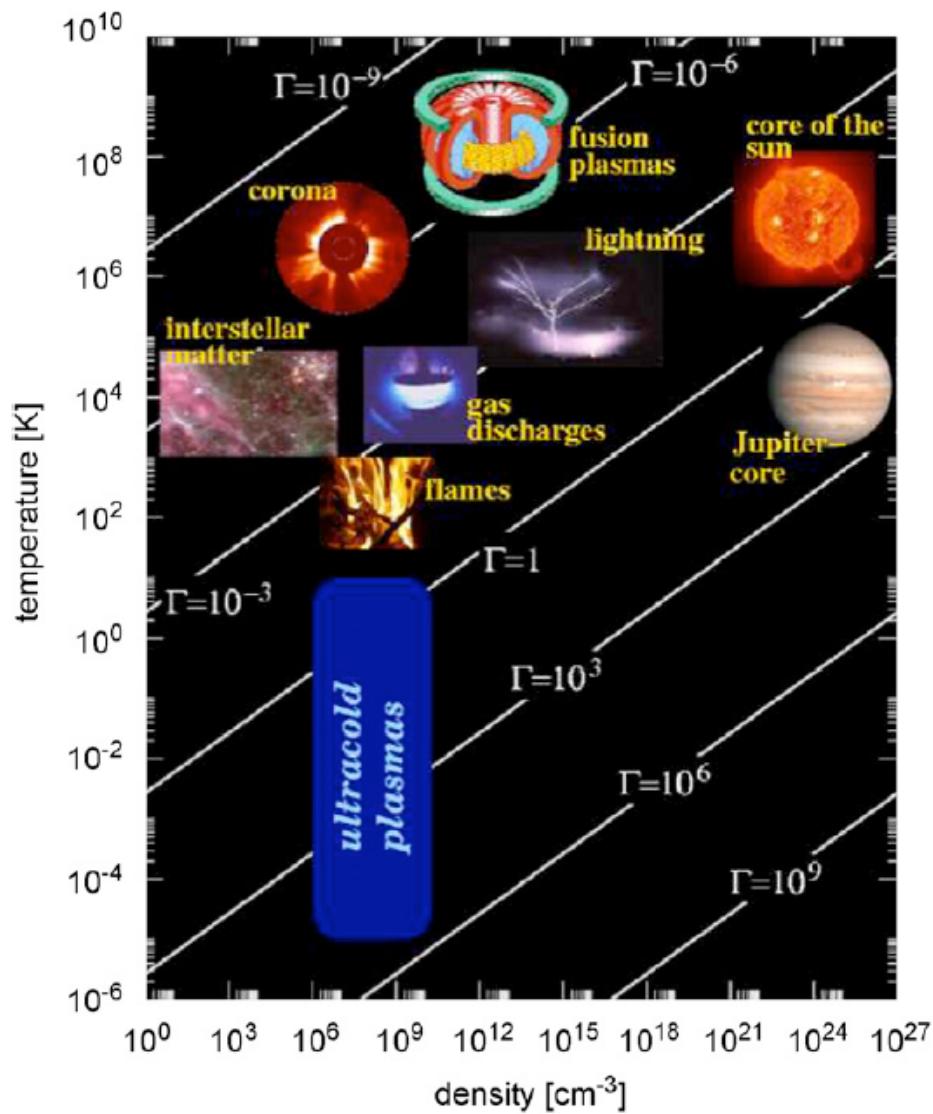
$$(e^2 = q_e^2 / 4\pi\epsilon_0) \\ a = (4\pi n_e / 3)^{-1/3}$$

$$\Gamma = E_{\text{pot}} / E_{\text{cin}}$$

$$\Gamma < 1 ; n_e \lambda_{\text{Debye}}^3 > 1$$

$$\lambda_{\text{Debye}} = (\epsilon_0 k_B T_e / e^2 n_e)^{1/2}$$

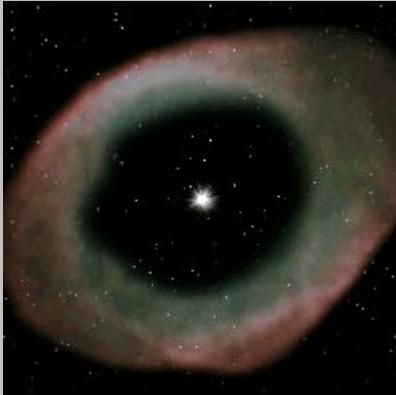
Plasmas



Correlated plasmas $\Gamma \geq 1$

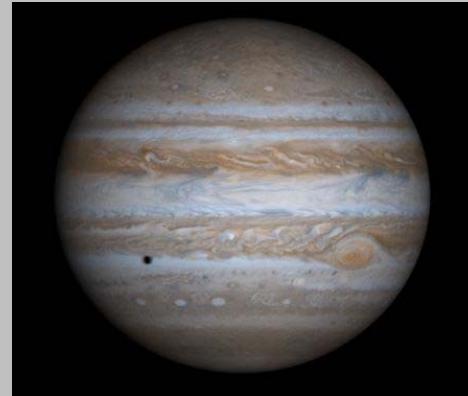
White dwarfs:

$T \sim 10^7 \text{ K}$, $n \sim 10^{40} \text{ m}^{-3}$,
 $\Gamma_{\text{ion}} \sim 300$

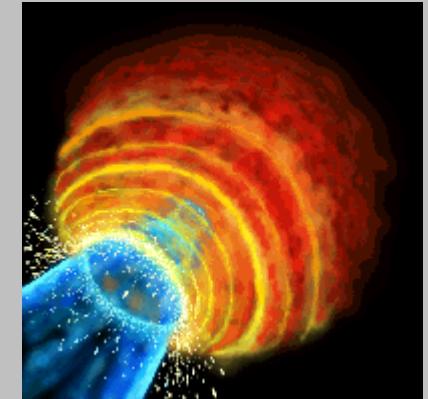


Brown dwarfs:

$T \sim 10^4 \text{ K}$, $n \sim 10^{30} \text{ m}^{-3}$
 $\Gamma \sim 20$



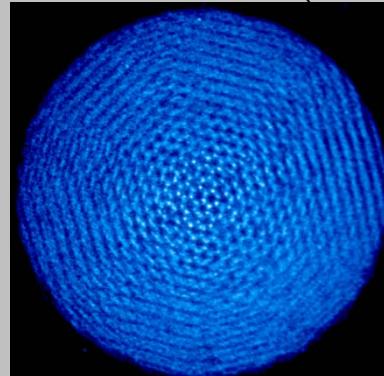
Laser plasmas (ps):
 $T \sim 10^4 \text{ K}$, $n \sim 10^{30} \text{ m}^{-3}$
 $\Gamma \sim 20$



$\Gamma \geq 172$ Coulomb crystal

Non neutral plasma

Coulomb cluster (EBIT)



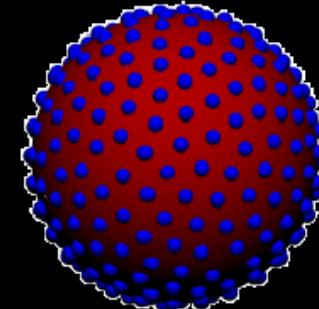
$\Gamma \geq 1$ Ultra-cold plasmas

$n_e \sim n_i \sim 10^{16} \text{ m}^{-3}$

$T_e \sim T_i \sim 100 \mu\text{K}$

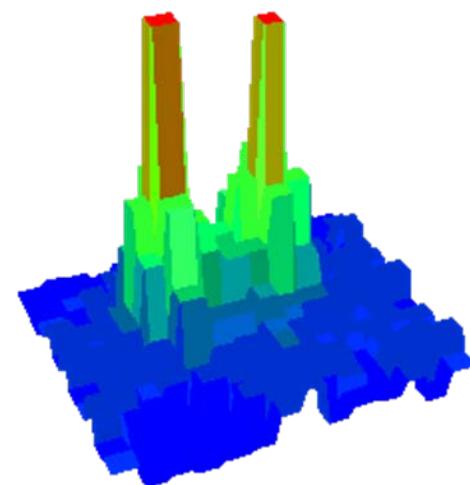
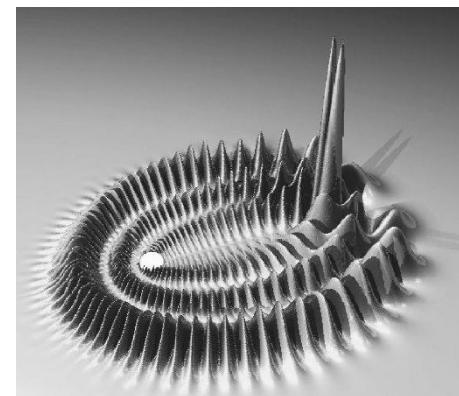
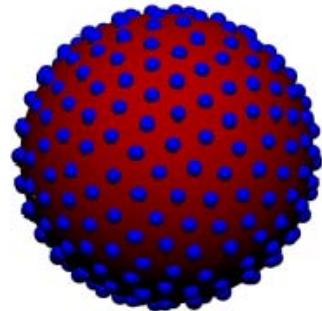


Cs



Perspectives and conclusion

- A very rich physics: cold Rydberg atoms as quantum simulators, cold Rydberg matter?
-
- Penning ionization, control of the interatomic forces, evolution towards an ultracold plasmas, highly correlated plasmas..., heating processes
- Application of dipole blockade for quantum gates : P. Gangrier, A. Browaeys *et al.* entanglement of two atoms with a fidelity of 75 % (quantum engineering)
- Rydberg photoassociation of cold atoms
- Landau-Zener transitions: few-body effects
- Stark-Rydberg decelerator of supersonic beams
- Rydberg excitation of quantum gases
- ...



Cold Rydberg atoms / Ultracold plasmas

Thibault Vogt

Matthieu Viteau

Amodsen Chotia

Jianming Zhao

Nicolas Saquet

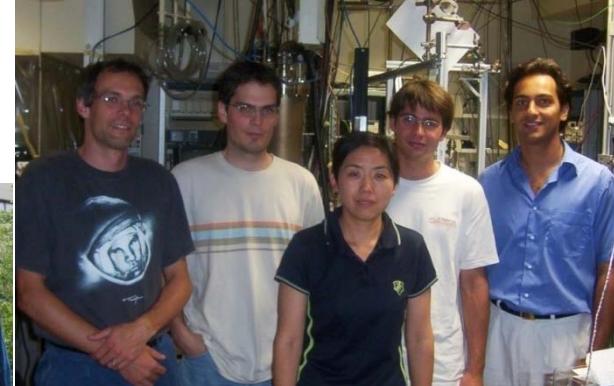
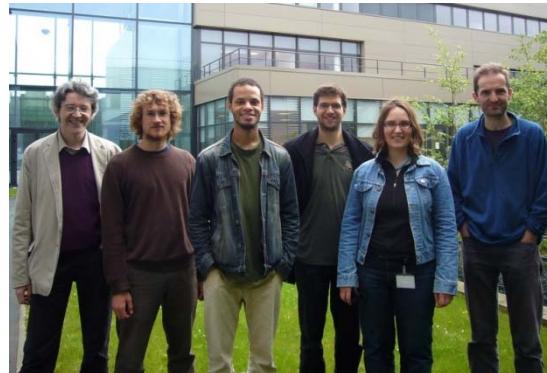
Anne Cournol

Jérôme Beugnon

Daniel Comparat

Nicolas Vanhaecke

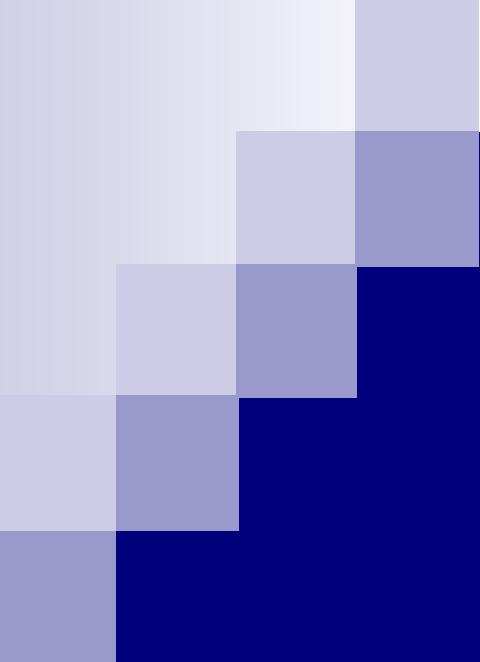
Pierre Pillet



**Collaboration on ultracold plasmas with
Thomas F. Gallagher, University of Virginia
and Ducan Tate, Colby College**

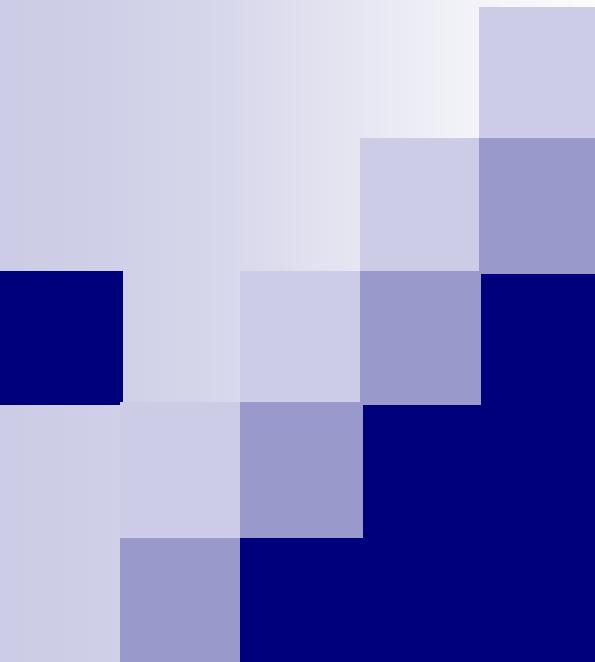
**Collaboration on collective excitation of a
pair of atoms in the dipole blockade regime
with Philippe Grangier, Antoine Browaeys
et al., Institut d'Optique**





The end

Thank you for your attention

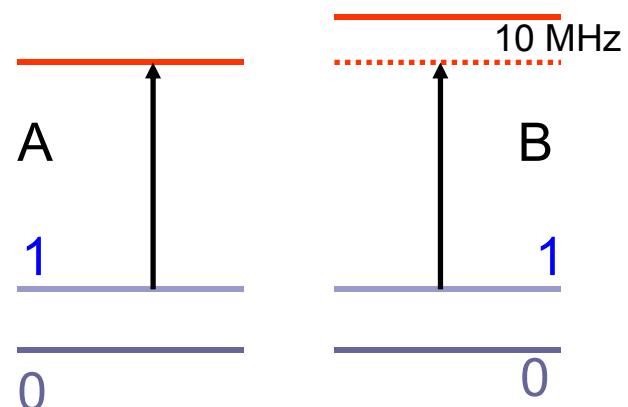


Dipole blockade of the Rydberg excitation

Application: quantum
information

Dipole blockade and quantum information

- Rydberg atoms, nl , are giant atoms (n^2 a.u.) and have huge polarizabilities
- Two atoms: Long-range dipole-dipole interaction shifts the Rydberg energy from its isolated value
- and prevents the excitation of the second atom in narrow bandwidth excitation:
Dipole blockade
-
- Application for scalable quantum logic gates



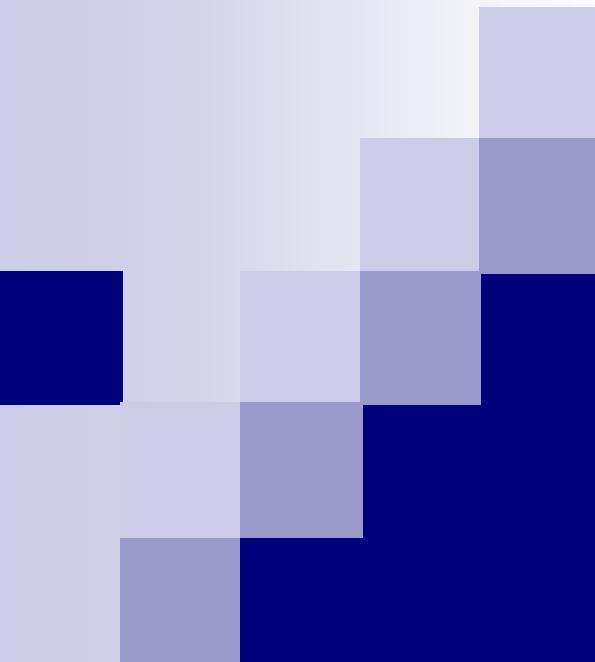
| | Phase Gate | 1) π pulse atom A | | | | 2) 2π pulse atom B | | | | 3) π pulse atom A | | | |
|---------------------------------------|--|-----------------------|--------------|--------------|--------------|------------------------|--------------|---------------|---------------|-----------------------|---------------|---------------|--|
| Jaksch et al., PRL 85 2208 (2000) | $ 0\rangle \otimes 0\rangle \rightarrow + 0\rangle \otimes 0\rangle$ | | | | | | | | | | | | |
| | $ 0\rangle \otimes 1\rangle \rightarrow - 0\rangle \otimes 1\rangle$ | | | | | | | | | | | | |
| Lukin et al., PRL 87 037901 (2001) | $ 1\rangle \otimes 0\rangle \rightarrow - 1\rangle \otimes 0\rangle$ | $ 00\rangle$ | $ 00\rangle$ | $ 00\rangle$ | $ 00\rangle$ | $ 01\rangle$ | $ 01\rangle$ | $- 01\rangle$ | $- 01\rangle$ | $ R0\rangle$ | $ R0\rangle$ | $- 10\rangle$ | |
| | $ 1\rangle \otimes 1\rangle \rightarrow - 1\rangle \otimes 1\rangle$ | $ 10\rangle$ | $ R0\rangle$ | $ R0\rangle$ | $ R0\rangle$ | $ 11\rangle$ | $ R1\rangle$ | $ R1\rangle$ | $ R1\rangle$ | $ R1\rangle$ | $- 11\rangle$ | | |



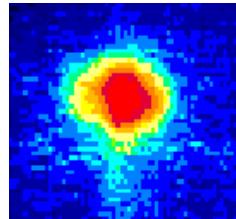
Dipole Blockade in a mesoscopic Rydberg n /ensemble?

- In zero electric field, no permanent electric dipole: no interaction? no blockade?
- By adding an electric field, Rydberg atoms acquire a permanent dipole: control of dipole blockade
- Förster resonances: to control and to have a strong dipole-dipole interaction
- Need high-resolution laser excitation ($\Delta\nu_L$).
Need to have motionless atoms: cold atoms
$$\Delta\nu_L \sim W \approx \mu_1\mu_2 / R^3$$
- To avoid the line-broadening due to saturation
- To limit the ionization processes

Evolution toward an ultracold plasma (Robison *et al.*, PRL85, 1408 (2000)) LAC-Charlottesville.

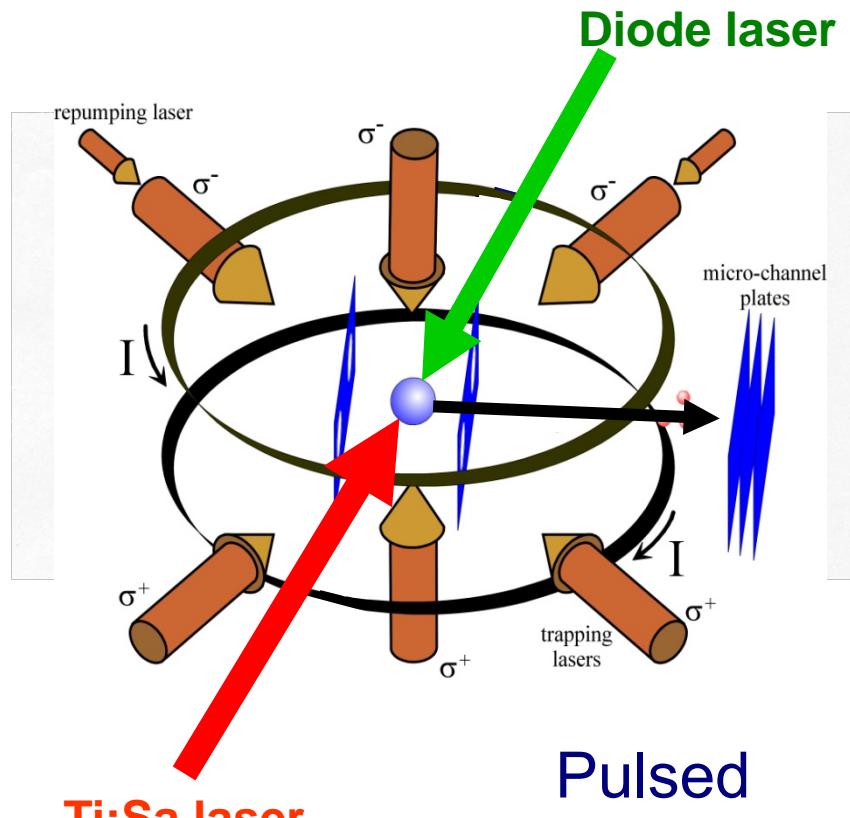


Cold Rydberg atoms at a Förster resonance

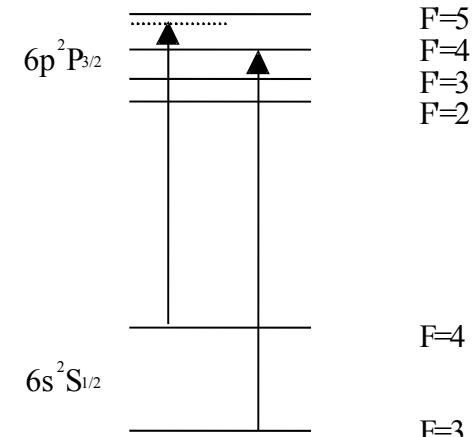


Experimental setup

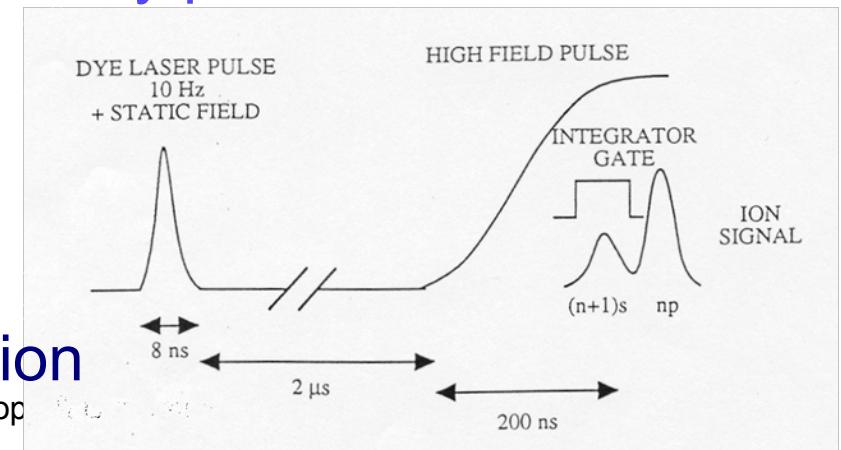
Cs vapor loaded MOT



Cs



Selective ionization
by pulsed electric field

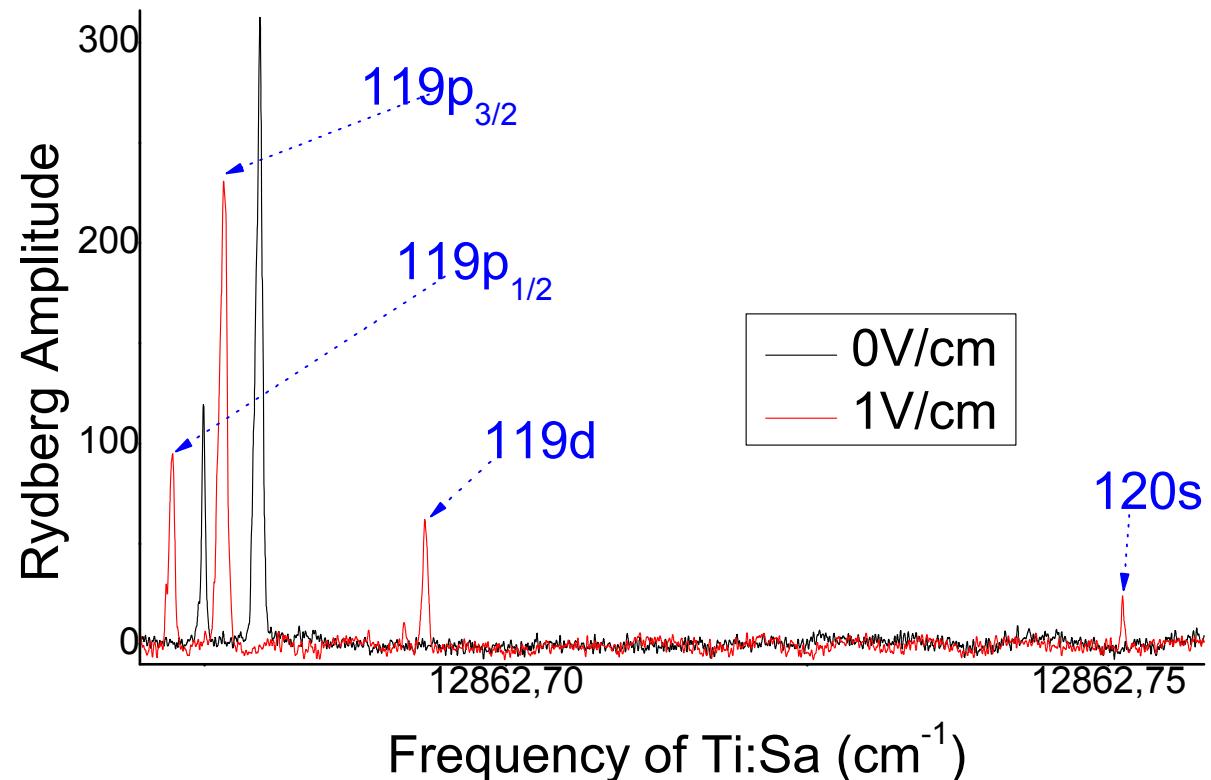
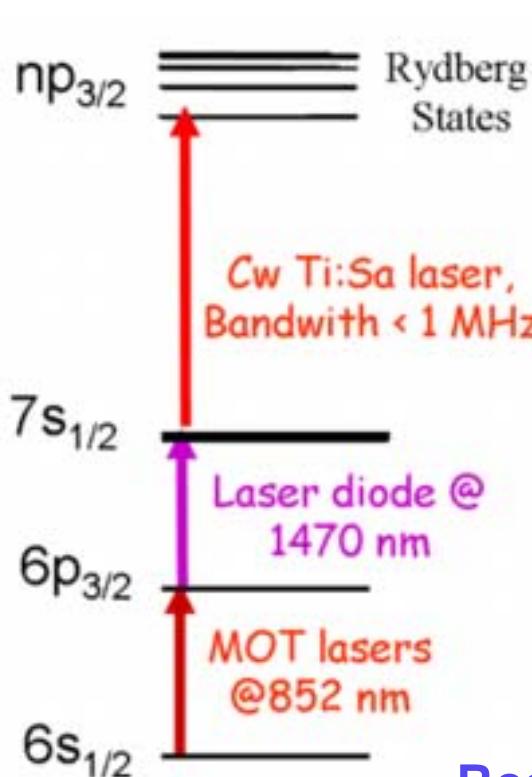


Pulsed
or cw excitation

Electronic Spectroscop

High-resolution laser-excitation of an ensemble of Rydberg atoms

$n = 25 - 130$



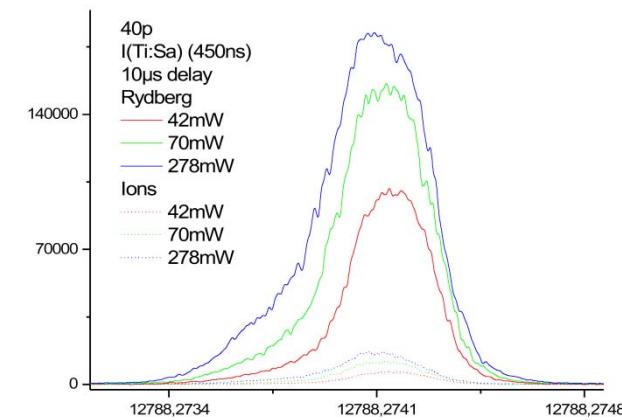
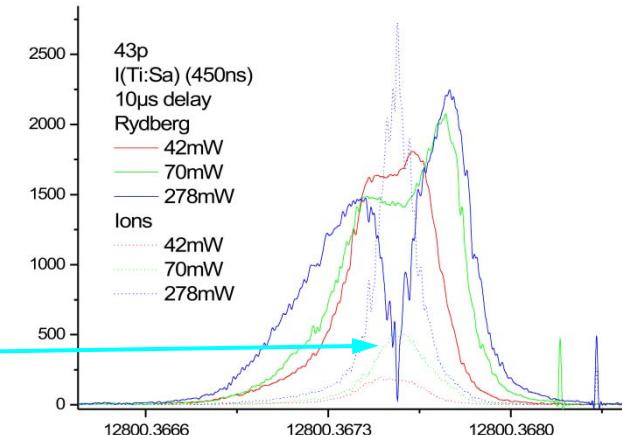
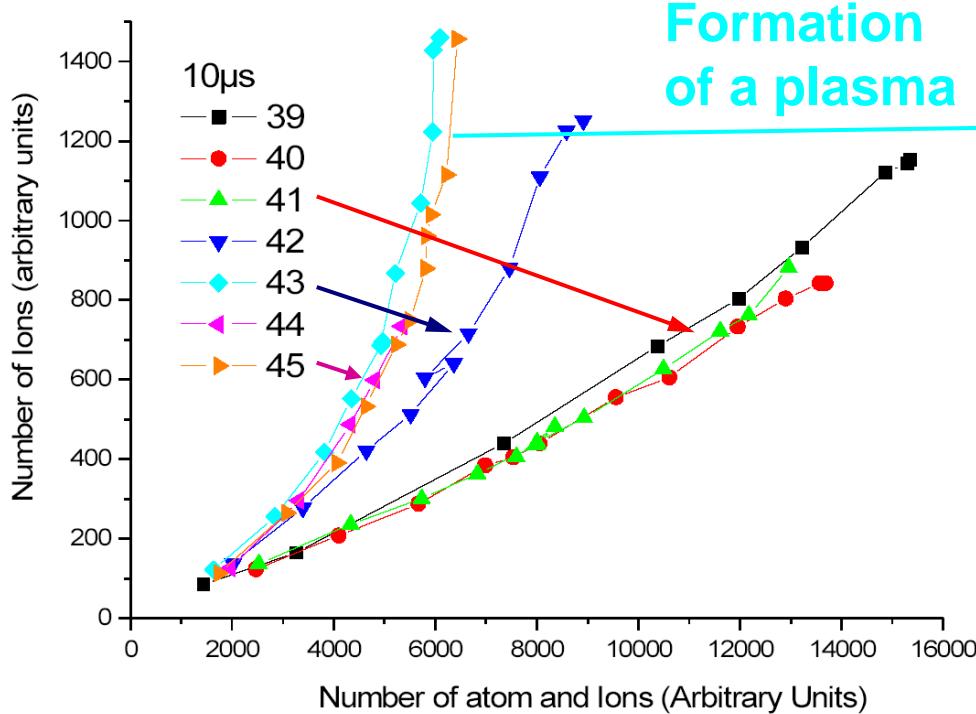
Resolution limited by the lifetime of $7s$ level: 56.5 ns:
 $\Delta\nu_L = 5 - 6 \text{ MHz}$. Duration of the excitation: $\tau = 300 \text{ ns}$

Cold collisions between cold Rydberg atoms and ionization (in zero field)

(excitation duration 10 μ s)



$$n' \ll n$$



Dipole gas / Rydberg atomic gas

- Quasi-resonance

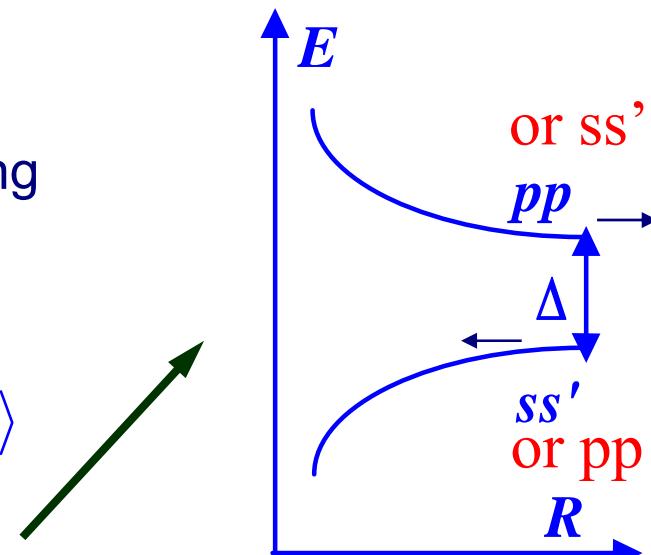
$$2 \times E(np) \sim E(ns) + E((n+1)s)$$

Second order dipole-dipole coupling

$$V \approx \frac{W^2}{\Delta} \text{ avec } W \approx \frac{\mu\mu'}{R_{AB}^3}$$

$$\mu = \langle np | \mu | ns \rangle, \quad \mu' = \langle np | \mu | (n+1)s \rangle$$

$$\Delta = 2E_{np} - (E_{(n+1)s} + E_{ns})$$

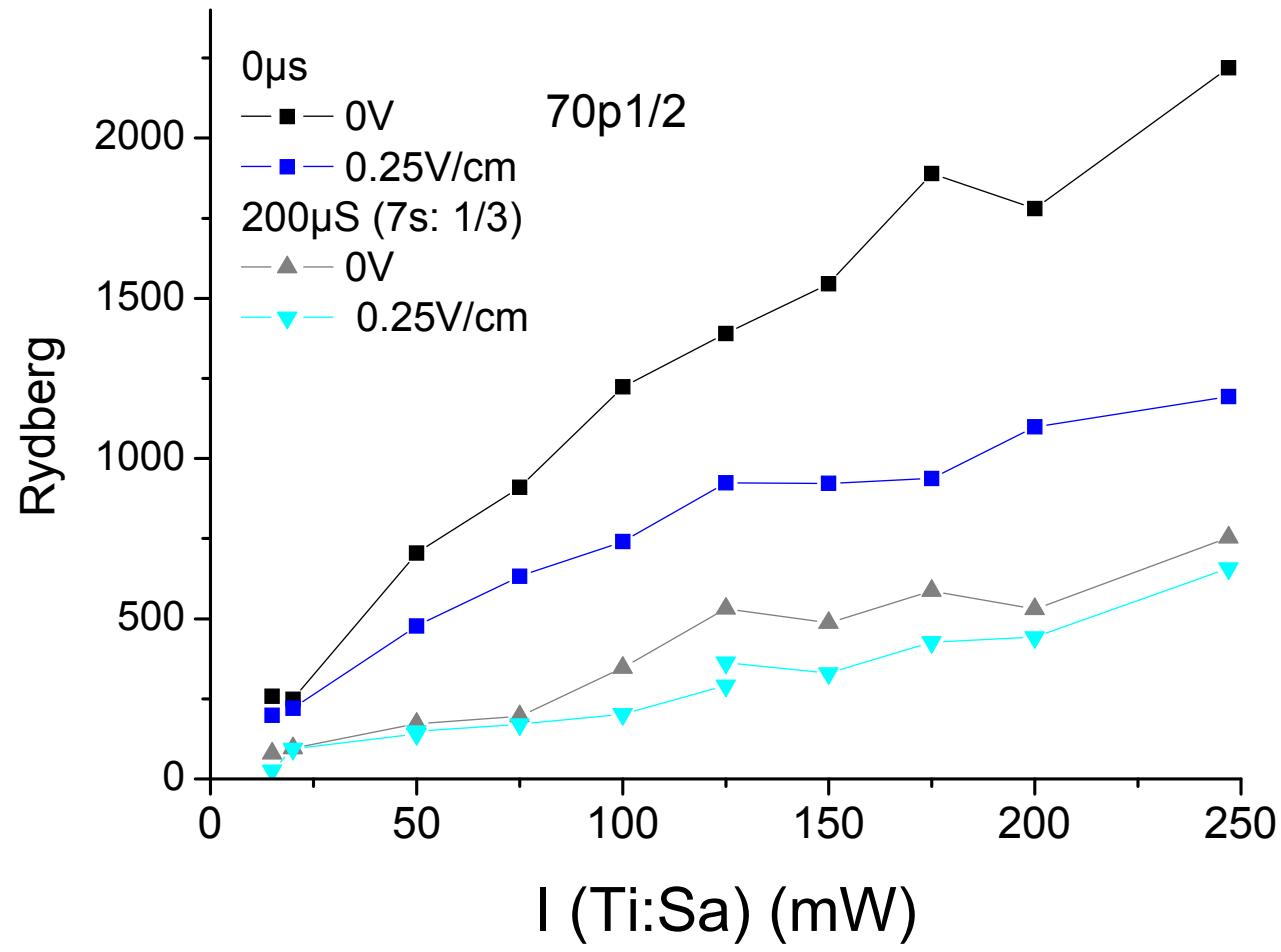


- n < 42:*** $2 \times E(np) > E(ns) + E((n+1)s)$, which corresponds to a weak repulsive force between close Rydberg atoms. The slow ionization is the result of blackbody radiation (ionization, BR assisted collisions)
- n > 42:*** $2 \times E(np) < E(ns) + E((n+1)s)$, which corresponds to an attractive force leading to Penning ionization, then to the *evolution of an ultracold plasma* (not the subject) ~ **Dipole gas**.



New schemes: Dipole blockade controled by electric field Dipole-dipole interaction due $p - d$ mixing

In progress



Conclusion

- Examples of dipole – dipole interaction
- Demonstration of the dipole blockade for Förster resonances
T. Vogt, M. Viteau, J. Zhao, A. Chotia, D. Comparat and P. Pillet, PRL 97, 083003 (2006)
- Quantum gate: collaboration with the group of Philippe Grangier
- A singly excited collective state
- Rydberg photoassociation (trilobite state)...
- Development of a Stark decelerator for Rydberg atoms or molecules (Nicolas Vanhaecke, Christian Jungen,... LAC)

