

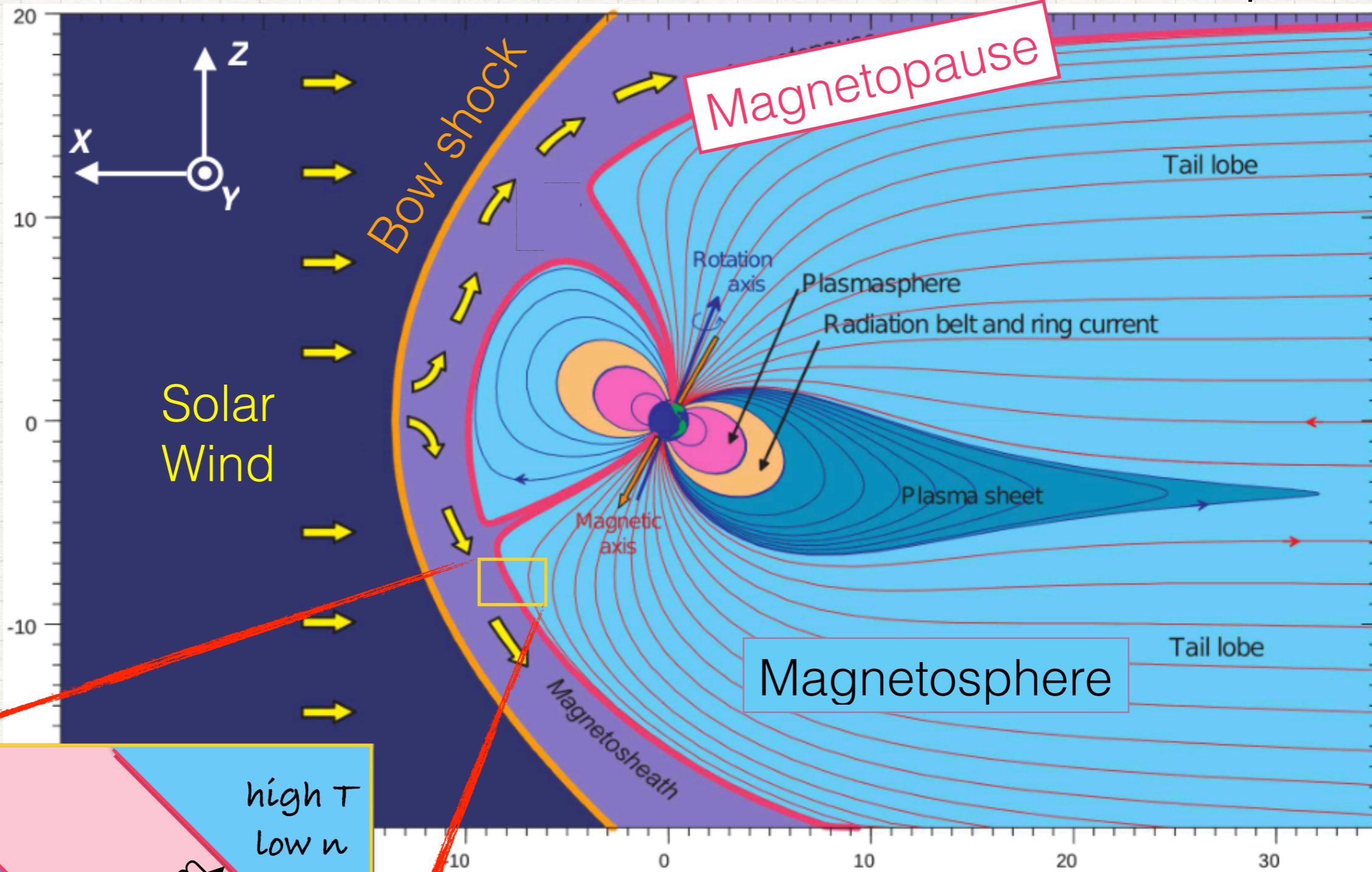
First year seminary @ UniPi



- Speaker: Roberto Manuzzo
- Working @(with): UPMC, Ecole Polytechnique (L.Rezeau, G.Belmont), UniPi (F.Califano)
- Target: Unequal temperature plasmas mixing across the Magnetopause

The Sun-Earth plasma system

$\sim 200 R_E \longrightarrow$



Magnetopause

Solar Wind

Bow shock

Magnetosphere

Tail lobe

Plasma sheet

Radiation belt and ring current

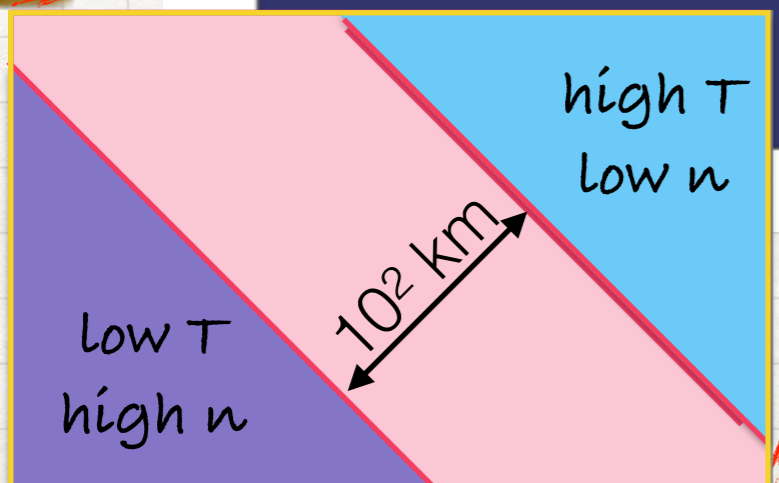
Plasmasphere

Rotation axis

Magnetic axis

Magnetosheath

Tail lobe



XZ cut of the magnetopause; Units: R_E ; Frame: GSE
Credits: P. Robert, CETP/CNRS, 1996

return

Sun not in scale

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From vlasov to single fluid... and after?

$$* f = f(\bar{\mathbf{r}}(t), \bar{\mathbf{v}}(t), t) \quad \partial_t f + \bar{\mathbf{v}} \cdot \bar{\nabla} f + \frac{\bar{\mathbf{F}}}{m} \cdot \bar{\nabla} f = (\cancel{\partial_t f})_{coll}$$

$$\langle \xi \rangle (\mathbf{r}, t) = \frac{\int \xi(\mathbf{r}, \mathbf{v}, t) f(\mathbf{r}, \mathbf{v}, t) d\mathbf{v}}{\int f(\mathbf{r}, \mathbf{v}, t) d\mathbf{v}}$$

for a single fluid collisionless plasma:

$$\xi = m\mathbf{v}^0 \quad \frac{\partial n}{\partial t} + \bar{\nabla} \cdot (n\mathbf{U}) = 0$$

$$\xi = m\mathbf{v}^1 \quad \frac{\partial(mn\mathbf{U})}{\partial t} + \bar{\nabla} \cdot (mn\mathbf{U}\mathbf{U}) - mn \langle \bar{\mathbf{F}} \rangle = 0$$

$$\xi = \frac{1}{2}m\mathbf{v}^2 \quad \frac{\partial(n\frac{1}{2}mU^2)}{\partial t} + \bar{\nabla} \cdot (n\frac{1}{2}mU^2\mathbf{U}) - n \langle \bar{\mathbf{F}} \cdot \mathbf{U} \rangle = 0$$

Problem: only one fluid! No energy exchanges are even defined...

Solution: find the way to perform a self-consistent evolution of 2 plasma fluids involving energy exchanges between hot and cold ions and electrons...

return

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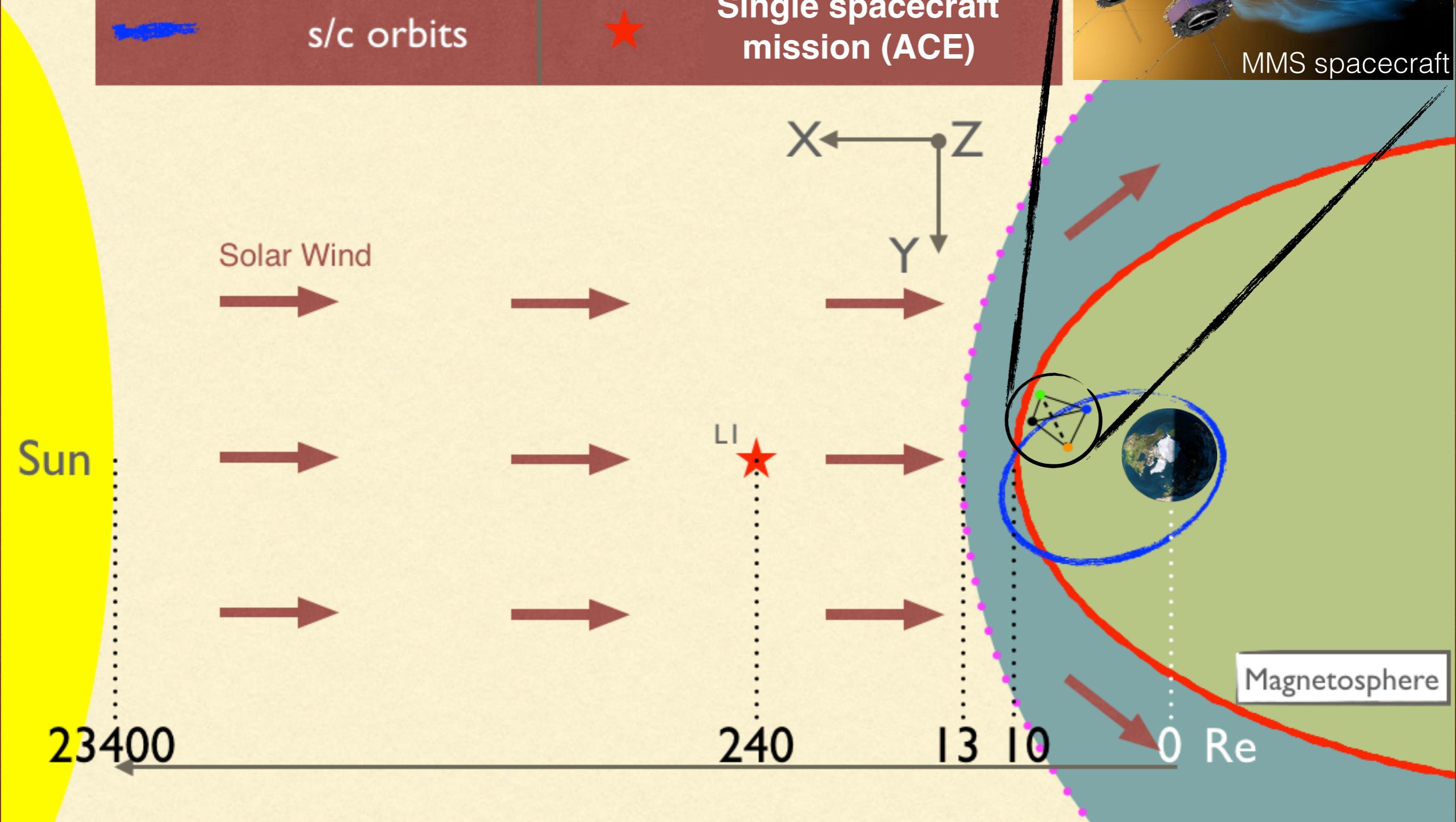
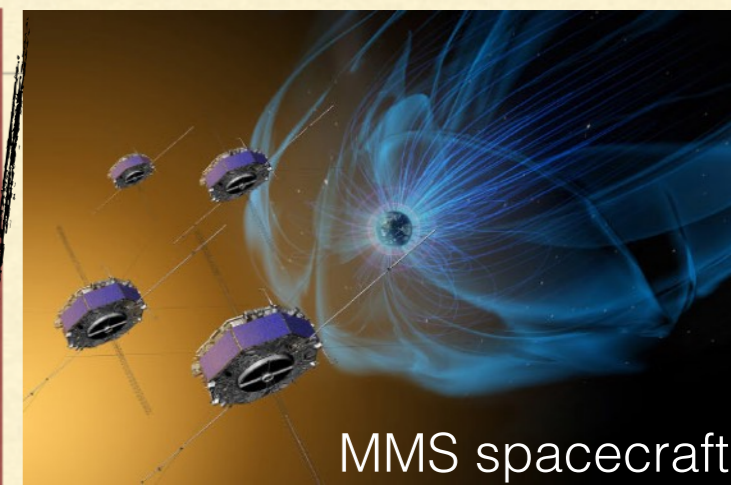
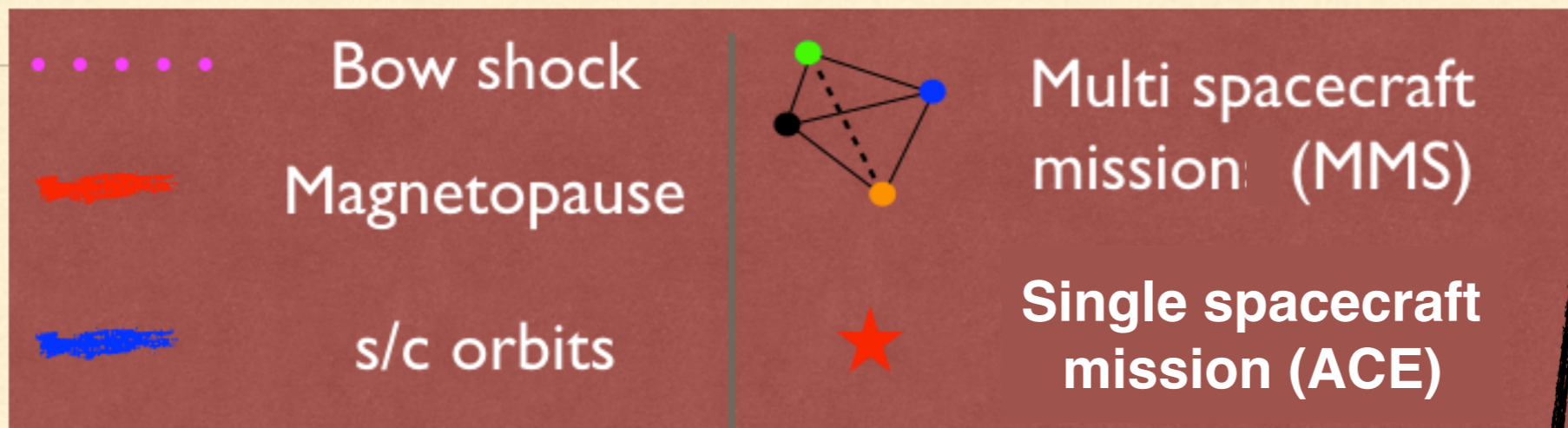
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How do we probe the magnetopause?



Sun

Solar Wind

L1

X Z

Y

Magnetosphere

23400

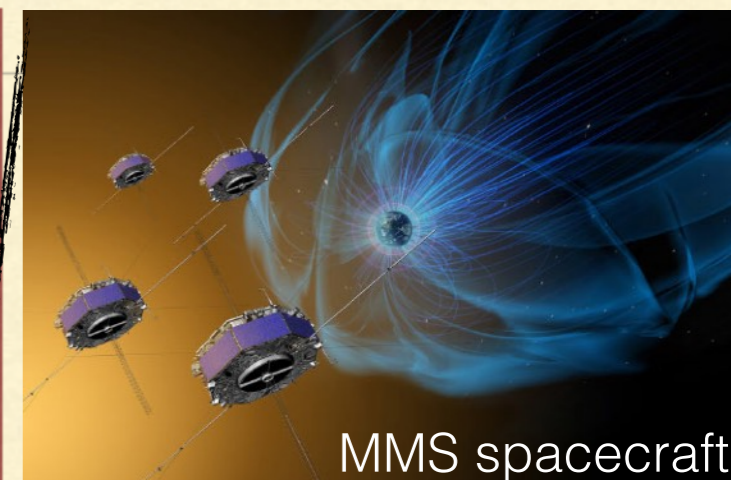
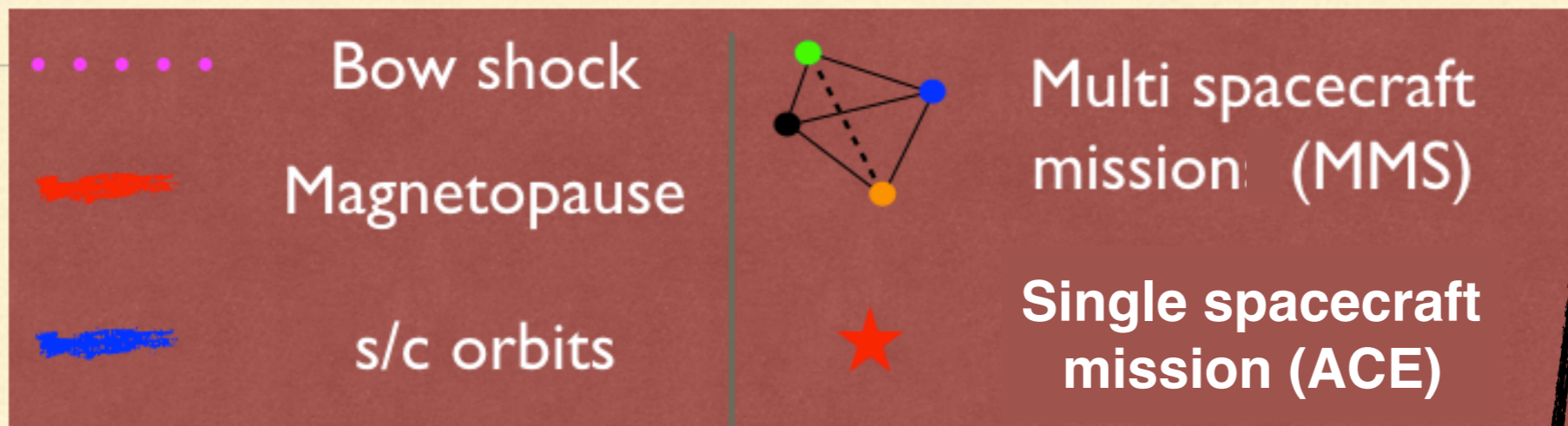
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How do we probe the magnetopause?



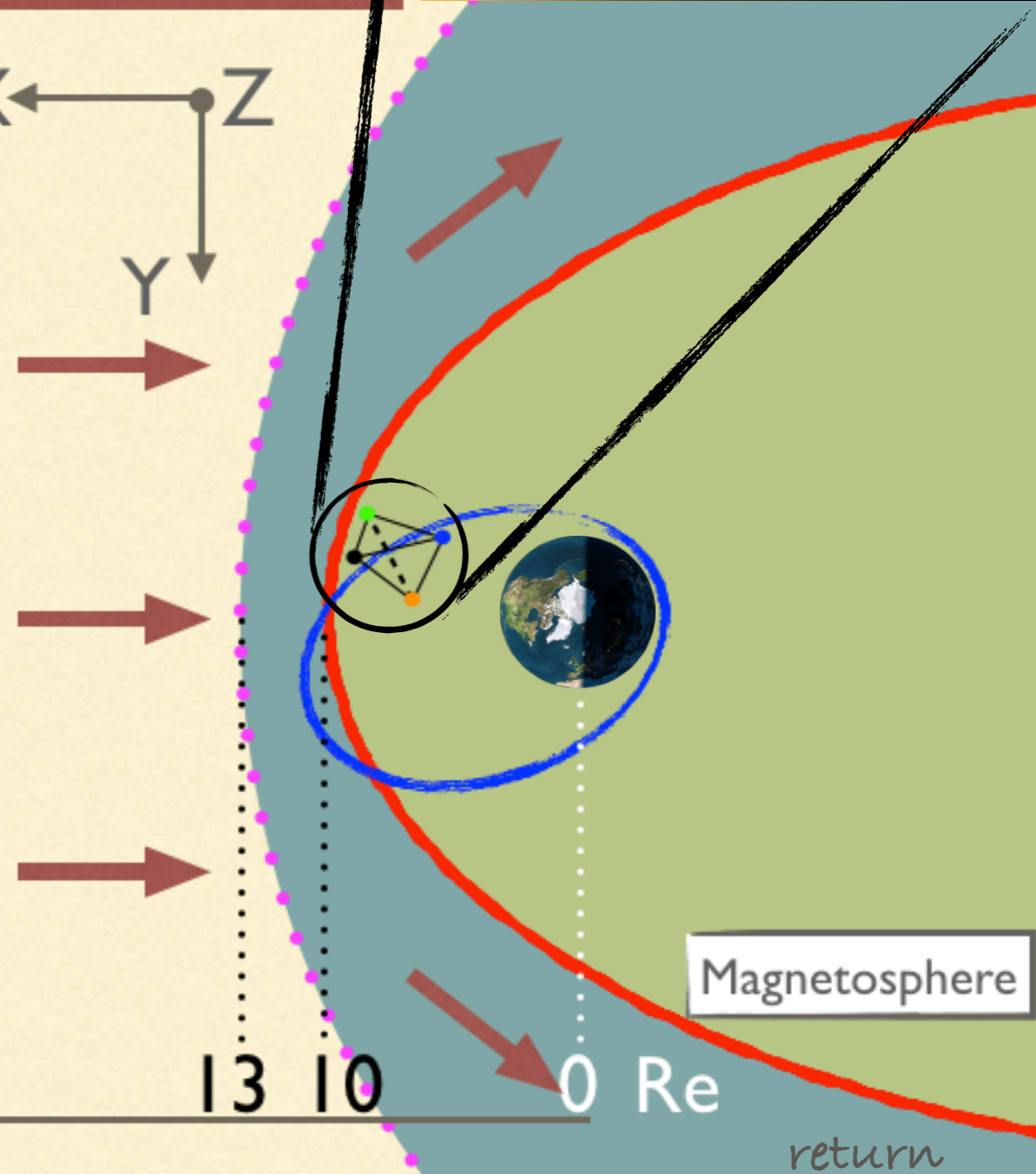
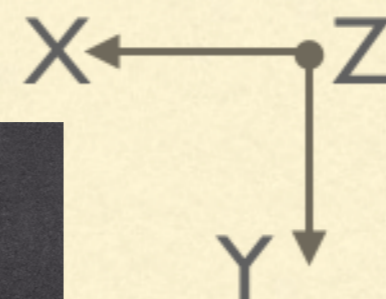
* WHAT MMS MEASURES (AND HOW)?

• FIELDS

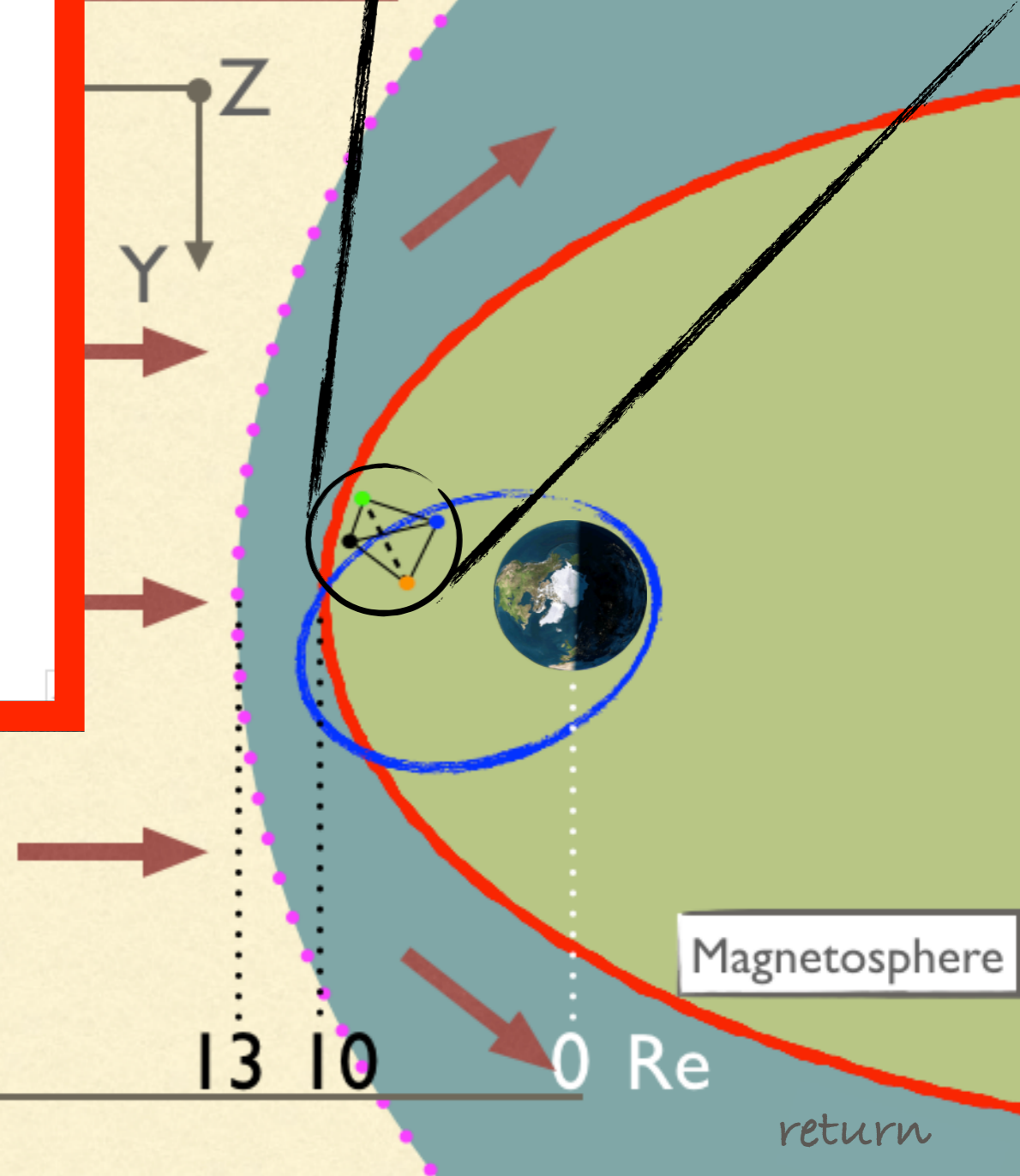
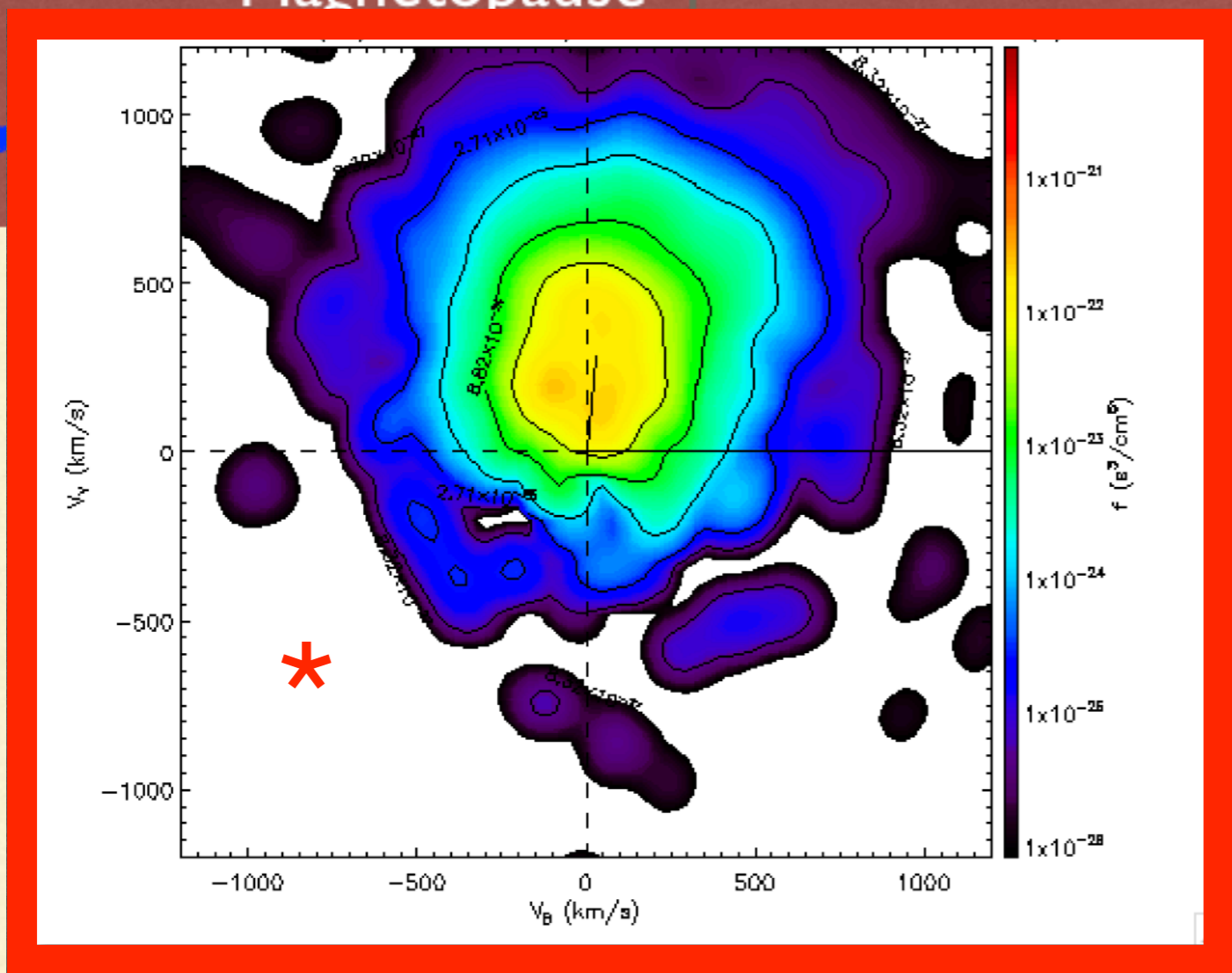
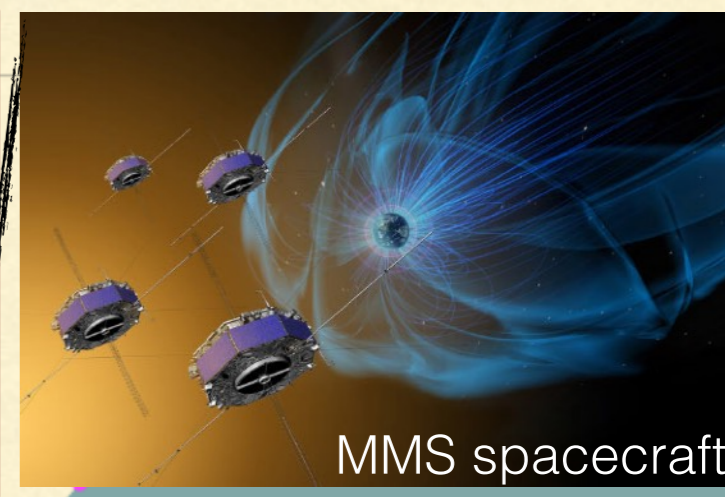
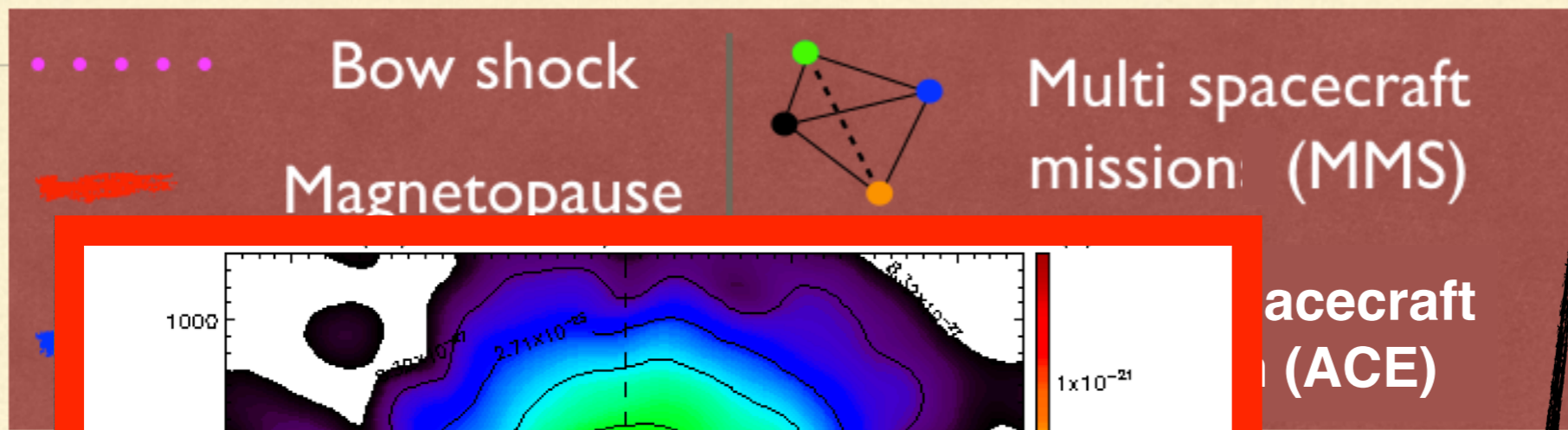
	E	B
Survey	DC, ~S/s	16 S/s
Burst	100 kS/s	128 S/s

• PARTICLES 3D3V DISTRIBUTION FUNCTIONS

- Ions => 150 S/s
- Electrons => 30 S/s



How do we probe the magnetopause?



- PARTICLES 3D3V DISTRIBUTION FUNCTIONS
 - Ions $\Rightarrow 150$ S/s
 - Electrons $\Rightarrow 30$ S/s

Sun

23400

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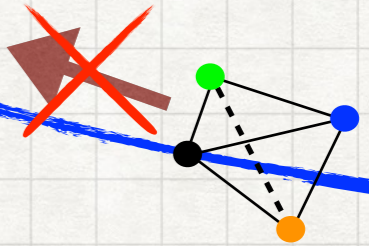
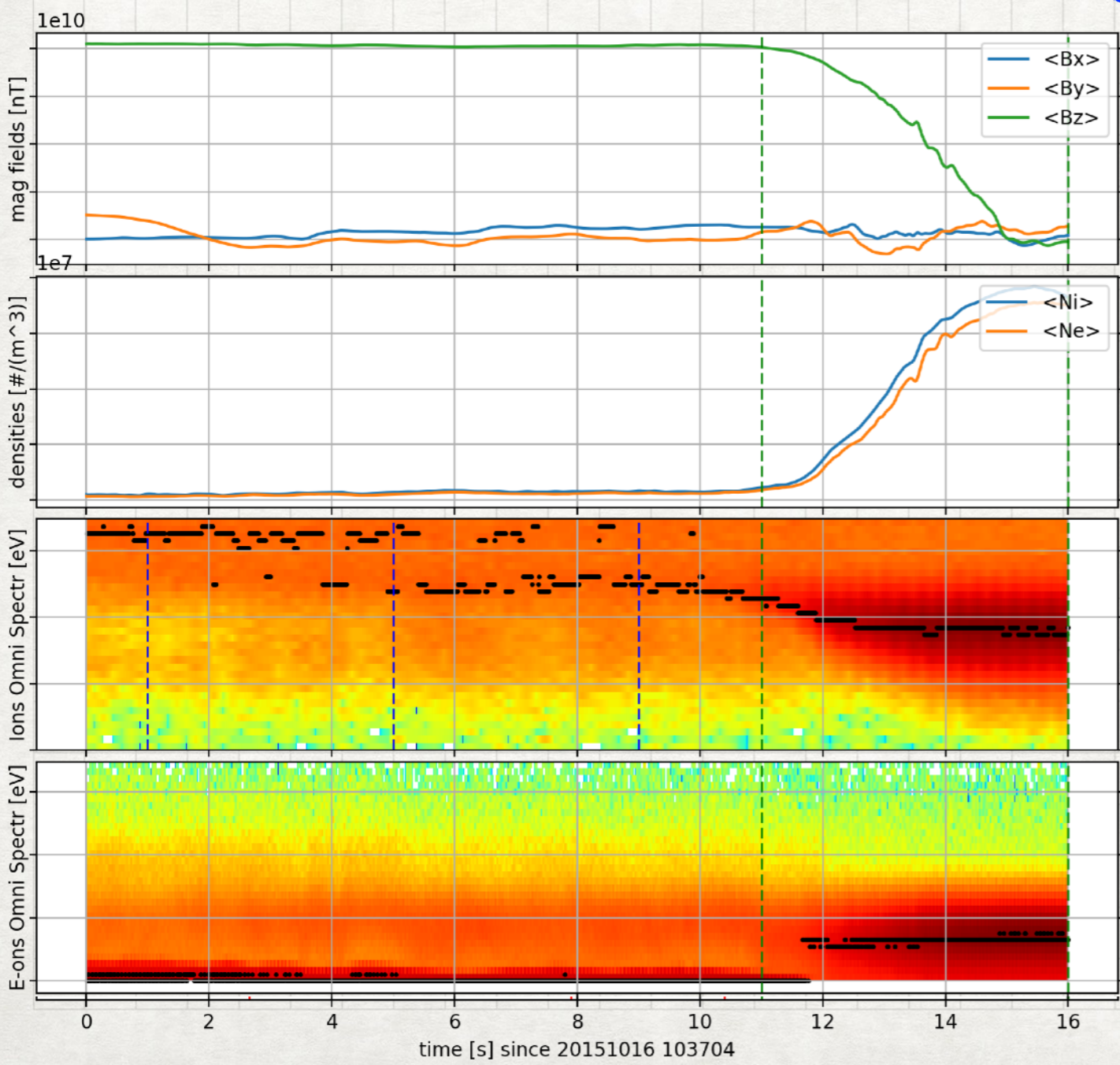
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Solar Wind 

MAGNETOSHEATH

MAGNETOSPHERE

MAGNETOPAUSE



return

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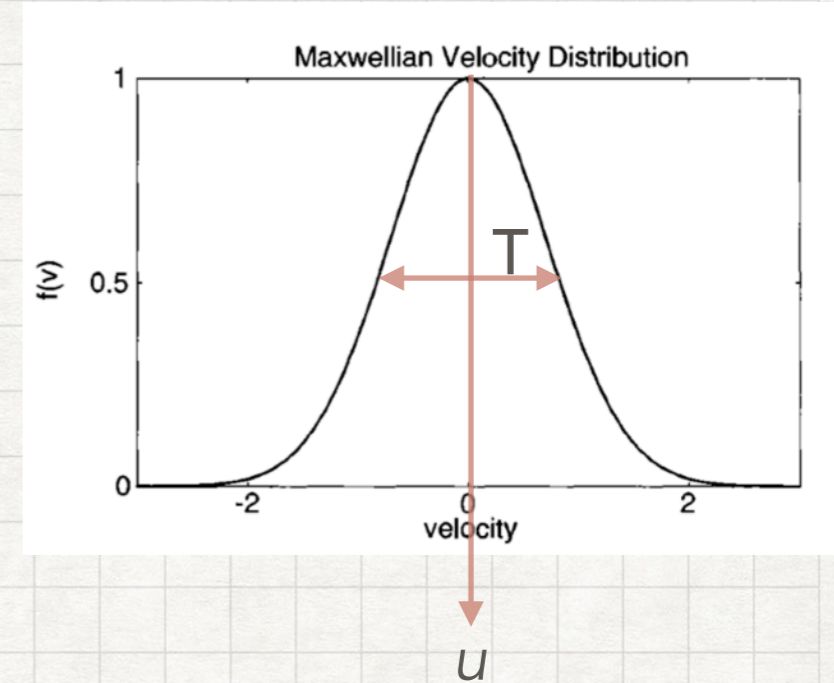


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 - Hermite analysis of 3V distribution function

How to discover several species in one distribution function?

-) Reminder: the physical meaning of a distribution function in a 1V phase space:

$$* f_{MB}(v) = n \left(\frac{m}{2\pi kT} \right)^{3/2} \text{Exp} \left(-\frac{m(v-u)^2}{2kT} \right)$$



-) 1V Hermite transform representation Servidio[2017]:

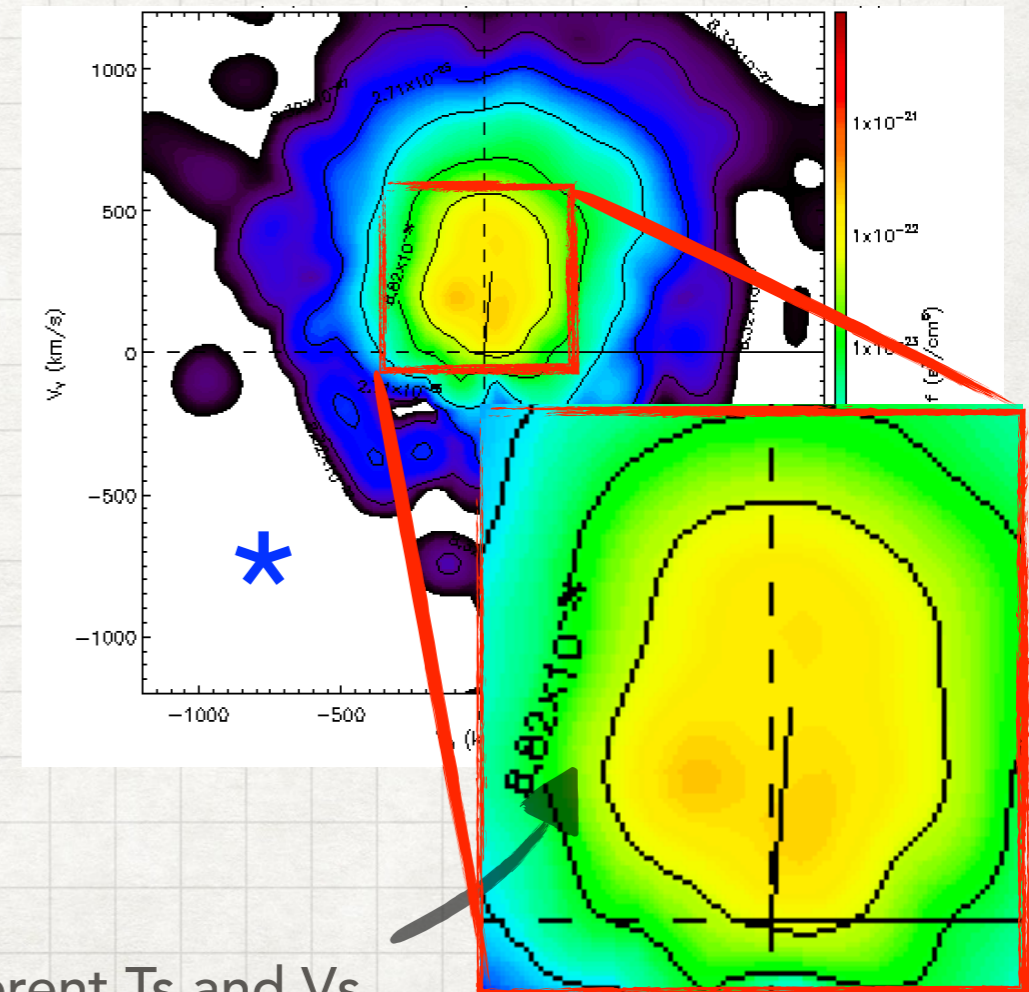
$$\begin{cases} f_{\mathbf{v}} = \sum_m f_m \psi_m(\mathbf{v}) \\ \int_{-\infty}^{\infty} \psi_m \psi_l = \delta_{ml} \\ \psi_m(v) = \frac{H\left(\frac{v-u}{v_{th}}\right)}{\sqrt{2^m m!} \sqrt{\pi} v_{th}} \exp\left(-\frac{m(v-u)^2}{2v_{th}^2}\right) \\ H_m(v) = (-1)^m e^{v^2} \frac{d^m}{dv^m} e^{-v^2} \end{cases}$$

N.B. : $\psi_{m=0}(v) \propto F_{MB}$

-) idea: apply the HTR to the 3V distr. func.:

$$\psi_m(\mathbf{v}) = \psi(m_x, v_x) \psi(m_y, v_y) \psi(m_z, v_z)$$

allowing for the presence of different species having different Ts and Vs...



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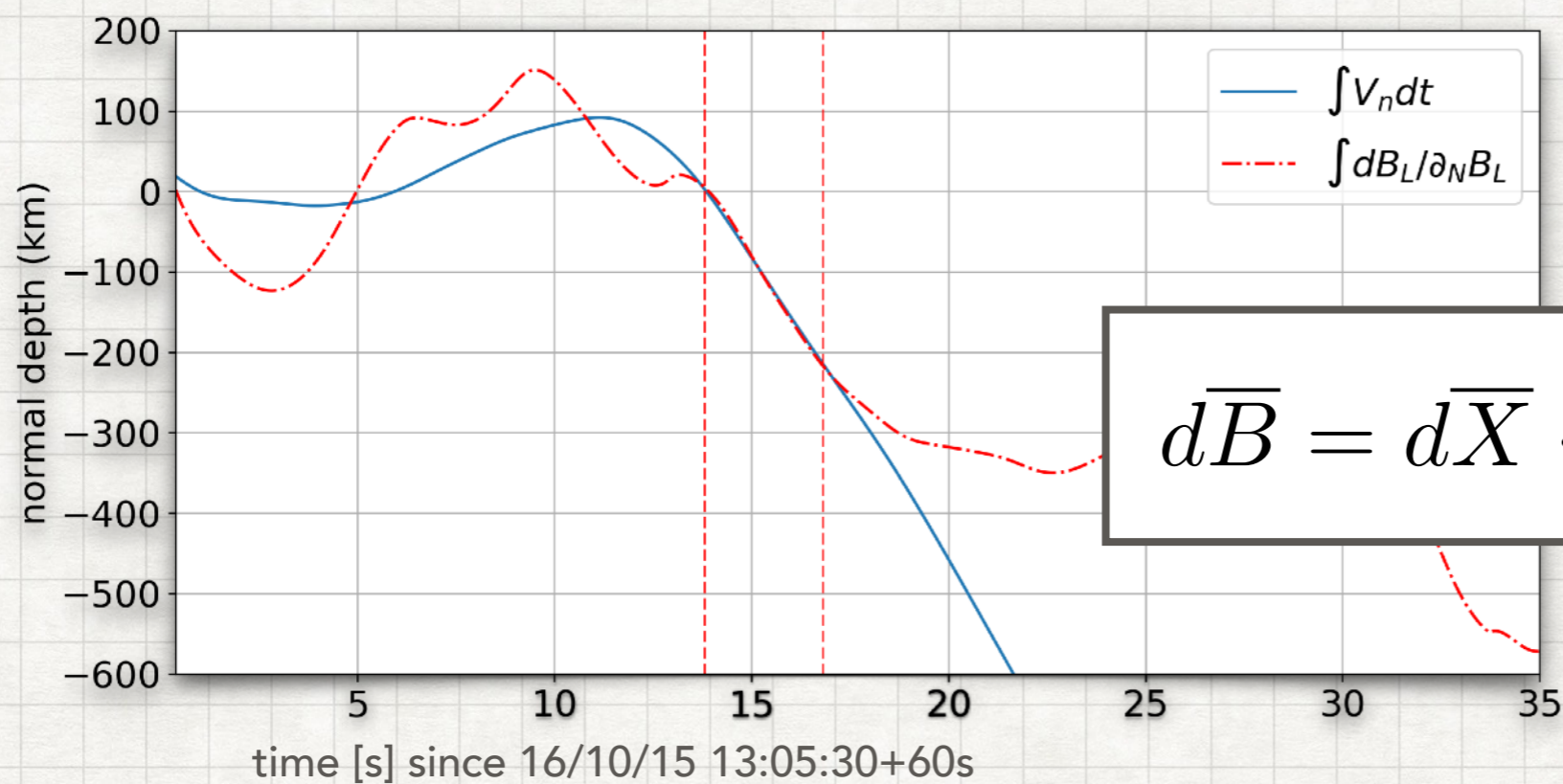


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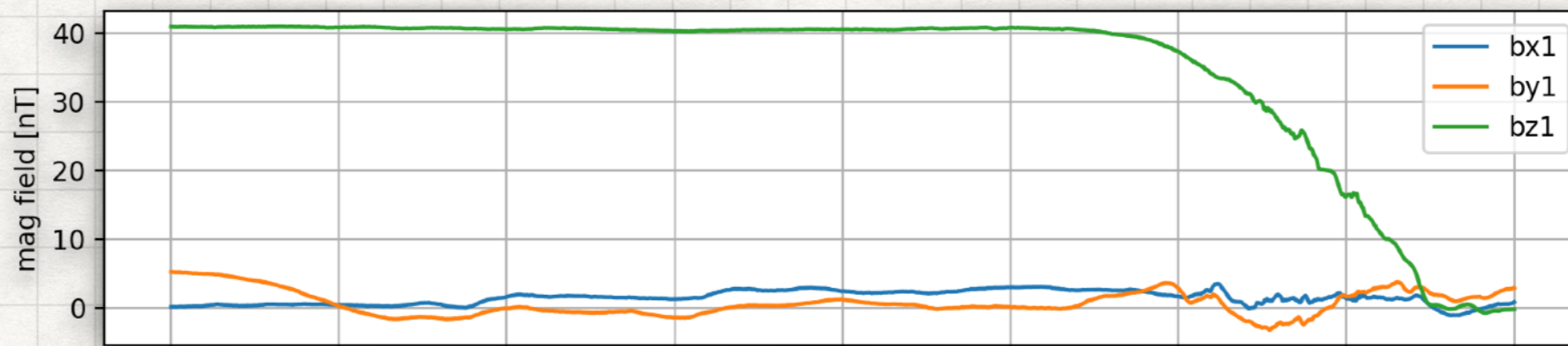
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A more precise determination of the magnetopause thickness...

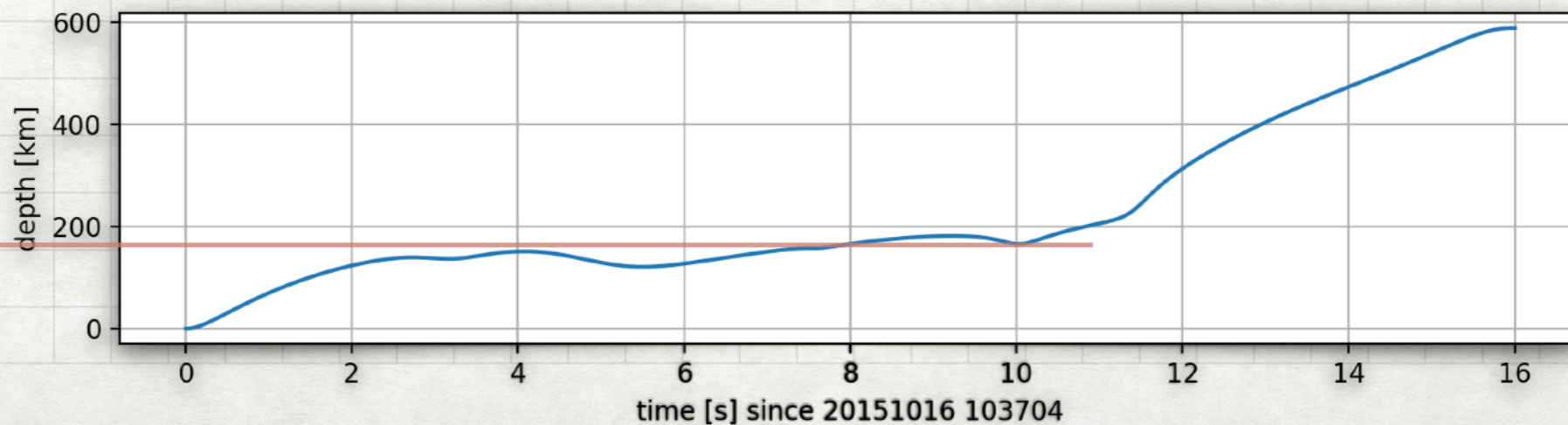


$$d\bar{B} = d\bar{X} \cdot \nabla \bar{B} + a + o(d\bar{X}^2)$$

Rezeau [2017]
+ next study

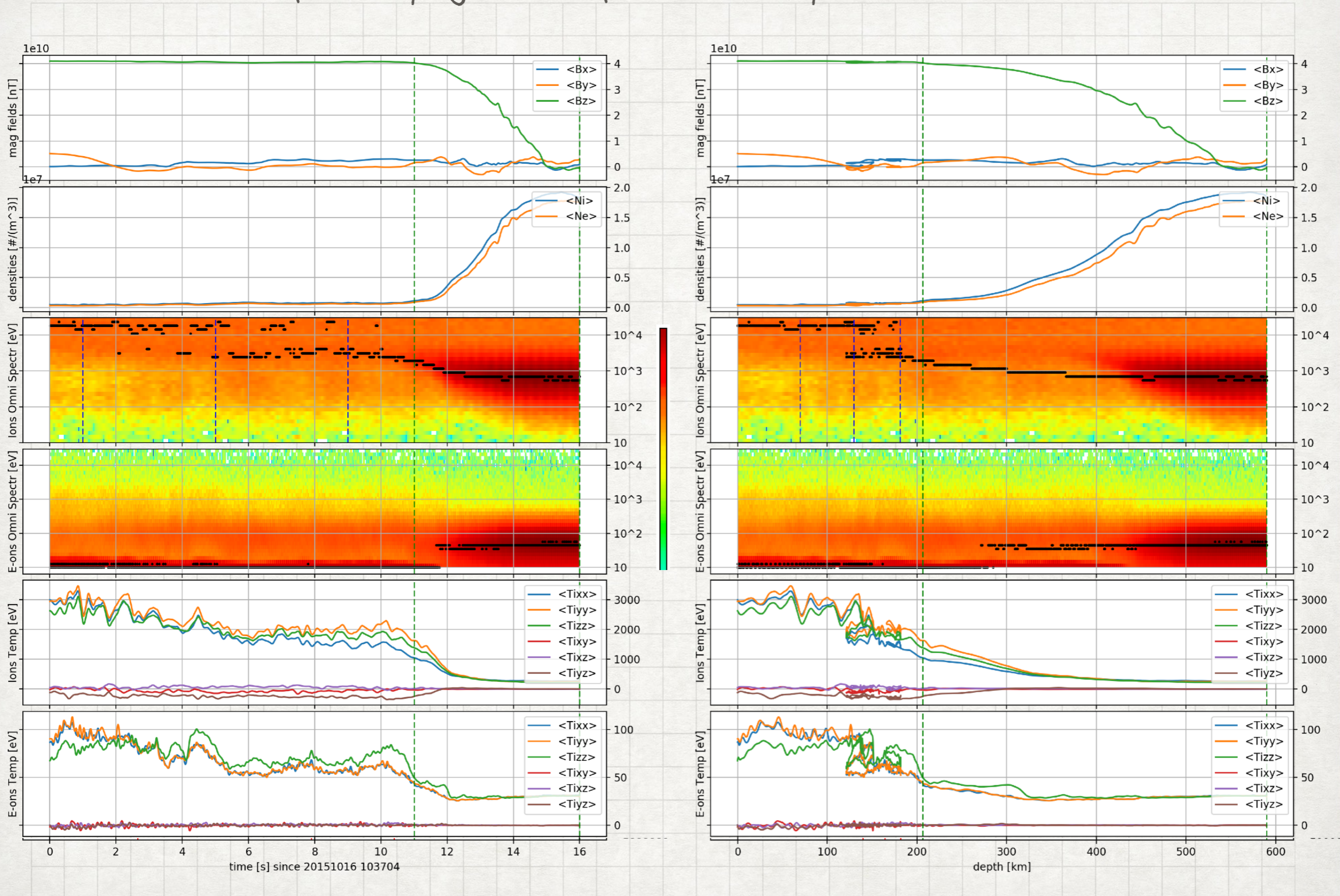


~6 di



Berchem [1982]

...which allows for the projection of data into space:



return

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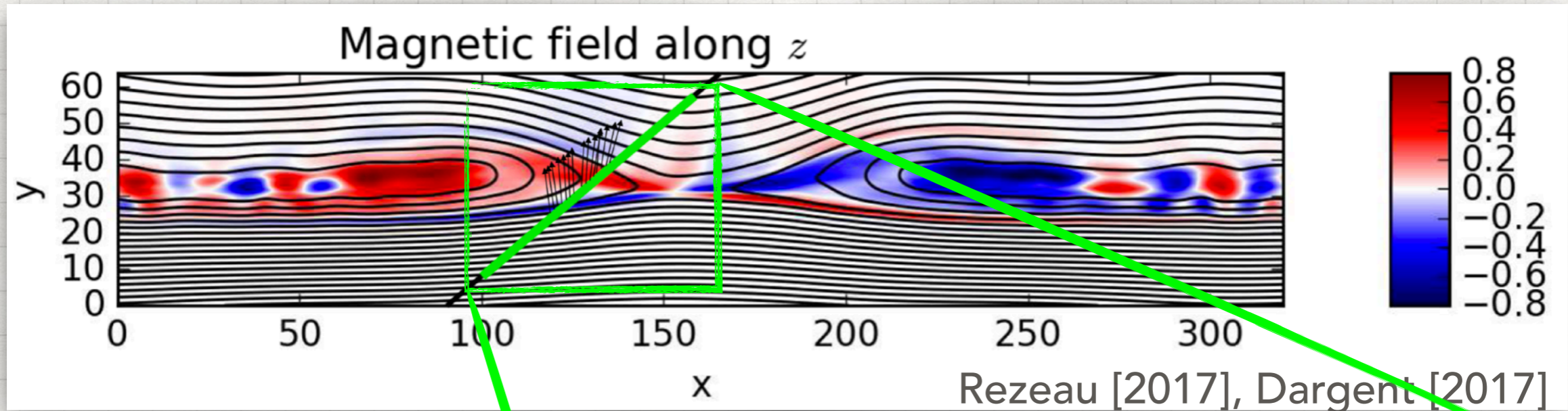


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A more precise determination of the normal to the magnetopause

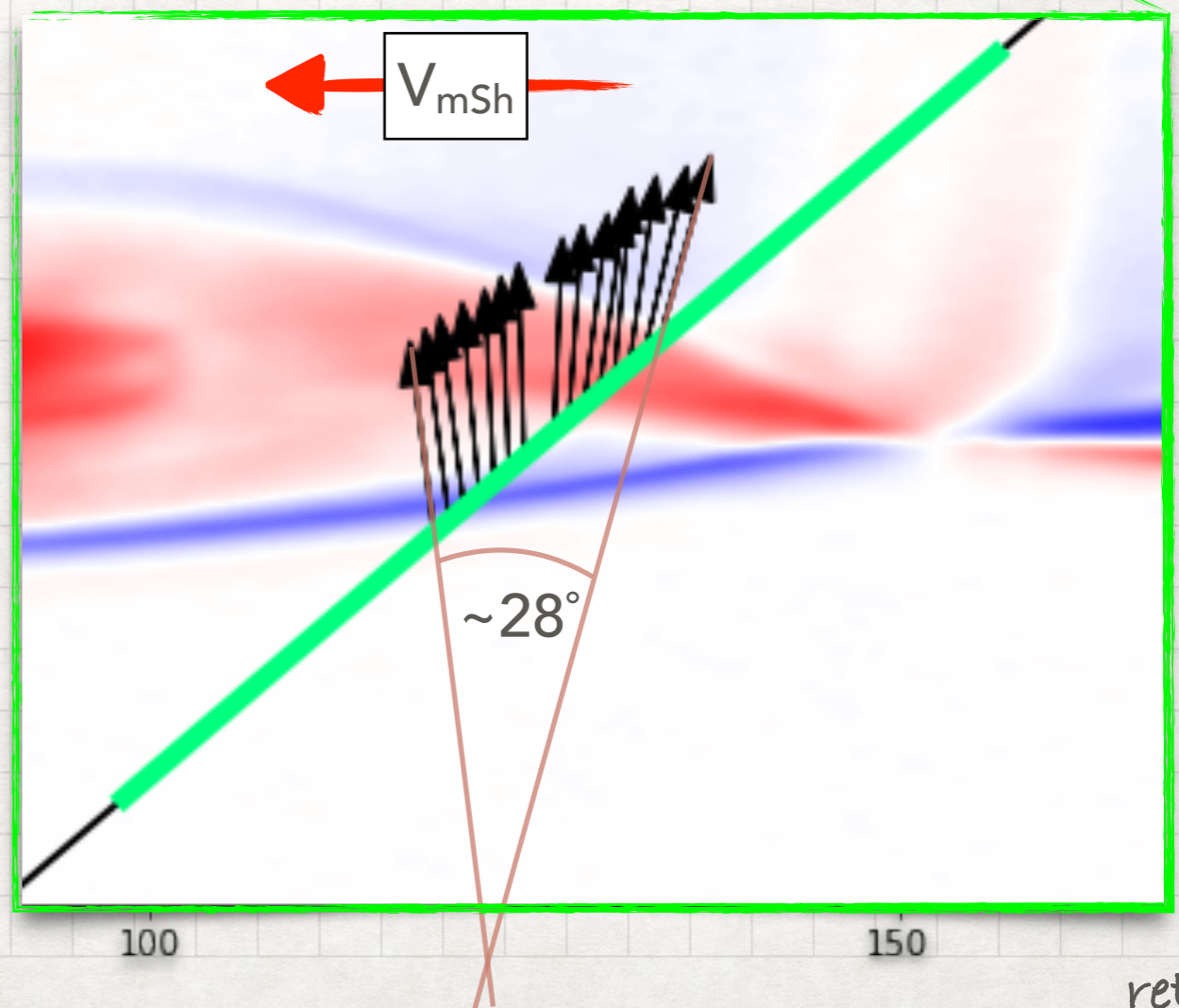


Global method are senseless in these cases!

$$V_{mSh} \sim 300 \text{ km/s}$$

$$x \sin(20^\circ) \sim 80 \text{ km/s}$$

different from
 $\sim 0 \text{ km/s}$!



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2. Simulations

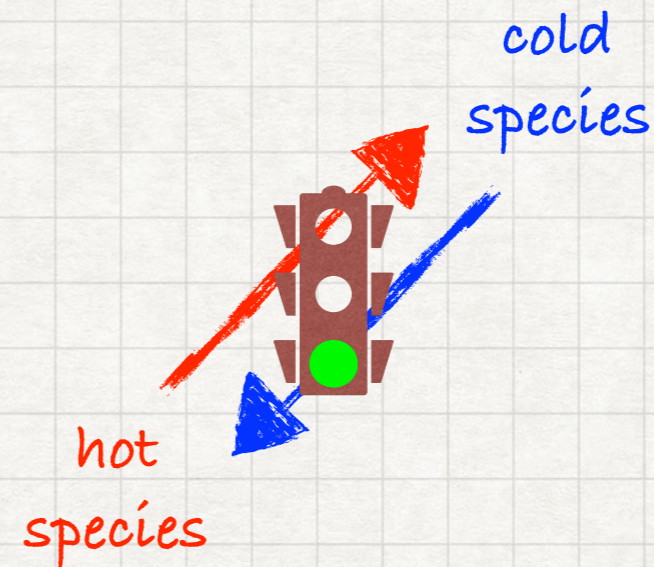
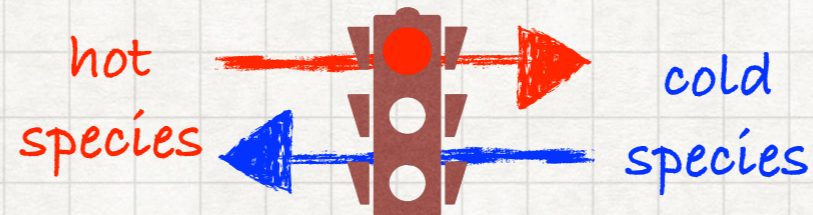
- 2->4-fluid code
- 4-Fluid code (i&e,low_T ⊕ i&e,high_T), large scale structure without en. evo constr.

From the 2-fluid to the 4-fluid

=> Advance the highest order terms, T_α , by means of a polytropic closure where the entropy is conserved because heat sources/fluxes and viscous stresses are neglected.

$$\begin{cases} t & \frac{\partial S_\alpha}{\partial t} + \bar{\nabla} \cdot (S_\alpha \mathbf{U}_\alpha) \propto \cancel{-\bar{\nabla} \cdot \bar{q}_\alpha} \cancel{-\Pi_{ij\alpha} \frac{\partial U_{i\alpha}}{\partial j}} + Q_\alpha \\ t+1 & P_\alpha = S_\alpha n^{\gamma-1} \\ t+2 & T_\alpha = P_\alpha / n \end{cases}$$

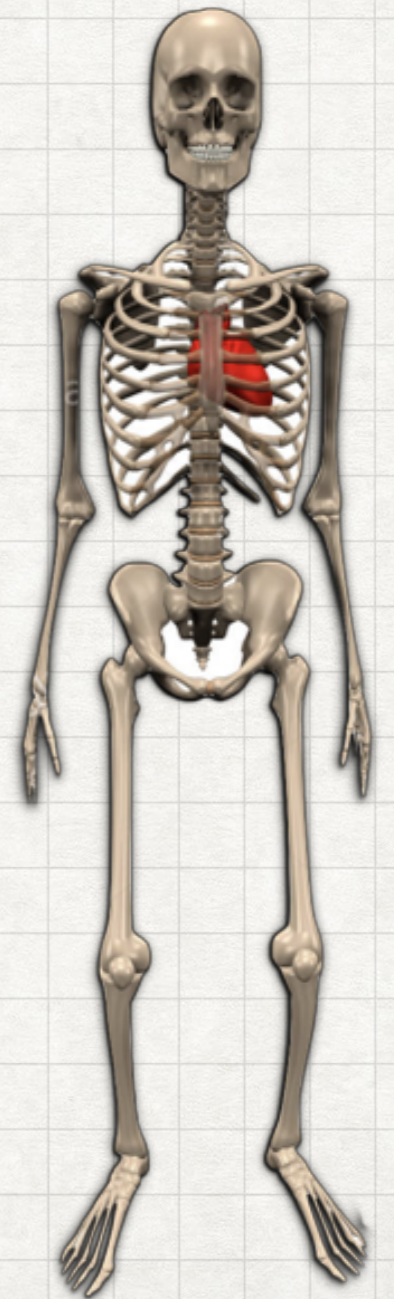
with $\alpha = i \wedge e$



Solution: compute the T_α as function of lower order terms without invoking constraints on the energy exchanges

$$T_\alpha = T_\alpha(n_\alpha, n_\beta, \mathbf{U}_\alpha, \mathbf{U}_\beta)$$

$$\text{with } \alpha = i \vee e \vee i \vee e \wedge \beta = \{i, e, i, e\} \setminus \alpha$$



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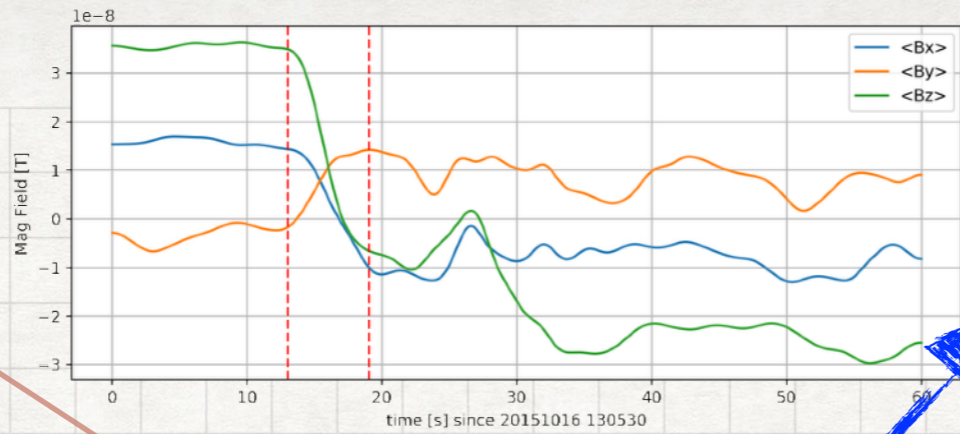
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 - 2-Fluid code (i&e same T), large scale structures with energy evo constraint)
 - 4-Fluid code (i&e, low_T \oplus i&e, high_T), large scale structure without en. evo constr.



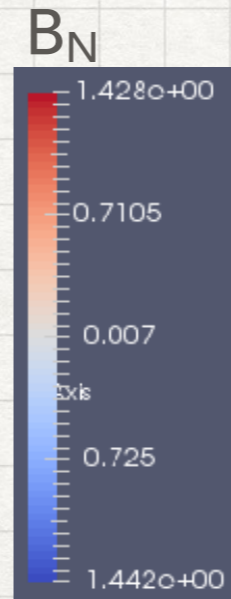
~ 15 R_E



Magnetosphere

Solar Wind

now it's a virtual satellite



Magnetopause

Quantity	Function
$ B $	$a_{ B } + b_{ B } \left(\tanh\left(\frac{x-c_{ B }}{d_{ B }}\right) + b'_{ B } \tanh\left(\frac{x-c'_{ B }}{d_{ B }}\right) \right)$
$B_M \angle B_T$	$a_\alpha + b_\alpha \tanh\left(\frac{x-c_\alpha}{d_\alpha}\right) + a'_\alpha$
B_M	$a_m + b_m \tanh\left(\frac{x-c_m}{d_m}\right)$
B_L	$a_l + b_l \tanh\left(\frac{x-c_l}{d_l}\right)$
N_i	$a_n + b_n \tanh\left(\frac{x-c_n}{d_n}\right)$
U_i	$a_u (1 + \tanh\left(\frac{x-c_u}{d_u}\right))$
P_i	$a_{P_i} + b_{P_i} \tanh\left(\frac{x-c_{P_i}}{d_{P_i}}\right)$
P_e	$a_{P_e} + b_{P_e} \tanh\left(\frac{x-c_{P_e}}{d_{P_e}}\right)$



return

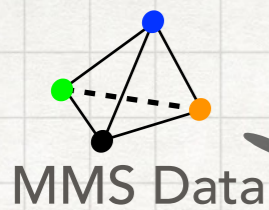
THANKS

References

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- Berchem & al., "The thickness of the magnetopause current layer: ISEE 1 and 2 observations", *J. Geophys. Res.*87-A4, 2108, (1982)
- Rezeau, Belmont, Manuzzo et al., "Analyzing the magnetopause internal structure: new possibilities offered by MMS tested in a case study", submitted to *JGR*, (2017)
- Shi et al., "Dimensional analysis of observed structures using multipoint magnetic field measurements: Application to Cluster", *GRL*, vol.32, L12105, (2005)

APPENDICES

The Minimum Directional Derivative method (MDD, Shi [2005])...



$$\bar{\bar{G}} = \nabla \bar{B} \quad \bar{n} \cdot \bar{\bar{G}} = \bar{D} = \frac{\partial \bar{B}}{\partial \bar{n}}$$

If $\mathbf{n} = \mathbf{N}$ was the invariant direction along which all the parameters remain constant $\Rightarrow D^2 = 0$

$$\text{diagonalization}(\bar{\bar{G}} \bar{\bar{G}}^T) \left\{ \begin{array}{lll} \lambda_1 & \bar{v}_1 & \text{maximum} \\ \lambda_2 & \bar{v}_2 & \text{intermediate} \\ \lambda_3 & \bar{v}_3 & \text{minimum} \end{array} \right\} \text{ of } \mathbf{D} \quad \left. \begin{array}{l} \lambda_1 \gg \lambda_2 \wedge \lambda_3 \Rightarrow \text{1D str.} \\ \lambda_1 \sim \lambda_2 \gg \lambda_3 \Rightarrow \text{2D str.} \\ \lambda_1 \sim \lambda_2 \sim \lambda_3 \Rightarrow \text{3D str.} \end{array} \right\}$$

... our Local Normal Analysis method (LNA, Rezeau [2017])

Hp.: stationarity and 1D



$$\bar{J} = \bar{N} \times \partial_N \bar{B} \perp \partial_N \bar{B} = -V_N \cdot \partial_N \bar{B}$$

Methods used to find the normal to the magnetopause

Common Hypotheses: magnetopause = 1D and stationary layer $\Rightarrow \mathbf{B}_n \neq \mathbf{B}_n(N, t)$

Single spacecraft

Minimum Variance
Analysis method

1) Find \mathbf{N} in order to minimize:

$$\sum_i \left\| (\mathbf{B}_i - \bar{\mathbf{B}}) \cdot \mathbf{N} \right\|^2$$

2) How to? Diagonalize

$$\left\{ \begin{array}{l} M_{\mu\nu} = \langle B_\mu B_\nu \rangle - \langle B_\mu \rangle \langle B_\nu \rangle \\ \mu, \nu = x, y, z \end{array} \right.$$

3) Results:

-) eigenvalues: $\lambda_1, \lambda_2, \lambda_3$
-) eigenvectors: $\mathbf{L}, \mathbf{M}, \mathbf{N}$

Pro: simple hypotheses
Vs: bad determination if not 1D

BV
method

1) Other hypotheses needed:

-) no flow through the magnetopause
-) \mathbf{B} behaves like:

$$\left\{ \begin{array}{l} B_L = B_{0L} \cos(\alpha) \\ B_N = B_{0N} \\ B_M = B_{0M} \sin(\alpha) \end{array} \right.$$

where:

$$\alpha = \alpha_1 + (\alpha_2 - \alpha_1) \frac{N}{y_{max}}$$

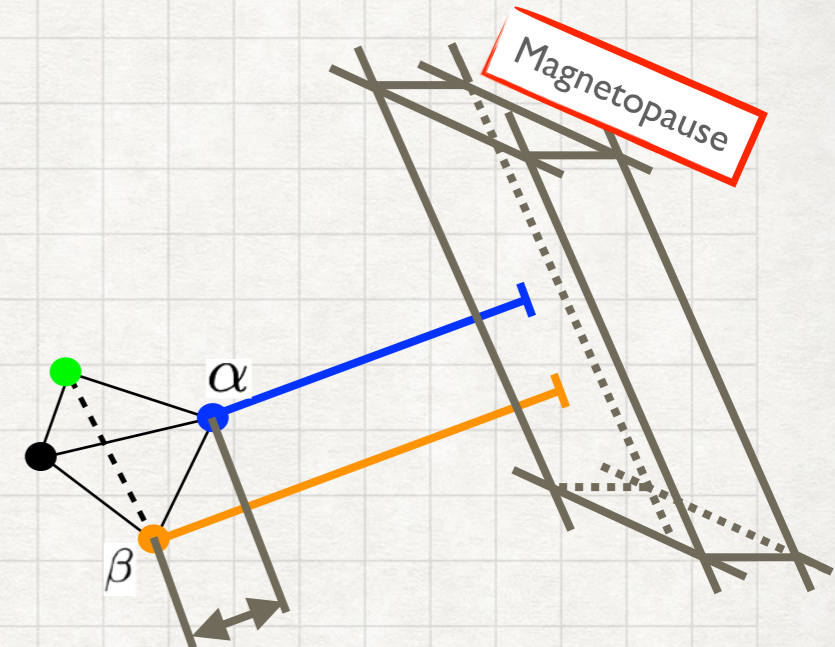
and

$$\mathbf{N} = \int_{crossing} \mathbf{V}_{BF}(t) \cdot \mathbf{N} dt$$

Pro: particle data involved too
Vs: Hypotheses

Multi spacecraft

Constant Velocity
Approach method



$$\begin{array}{l} \Delta t_{\alpha\beta} \\ \mathbf{r}_{\alpha\beta} \end{array}$$

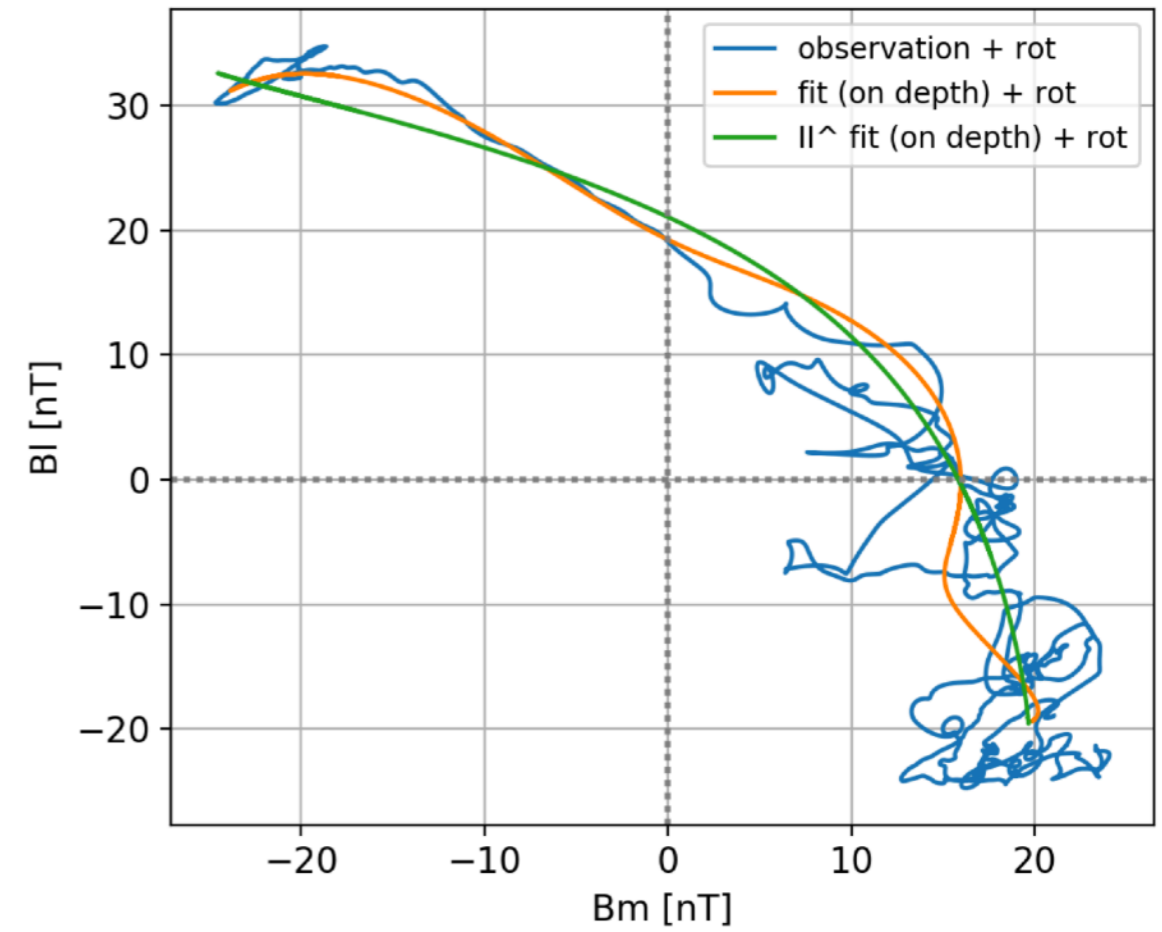
$$(\mathbf{V} \Delta t_{\alpha\beta}) \cdot \mathbf{N} = \mathbf{r}_{\alpha\beta} \cdot \mathbf{N}$$

Pro: Less hypoth, Simple, Mean
Vs: Problem with MMS data

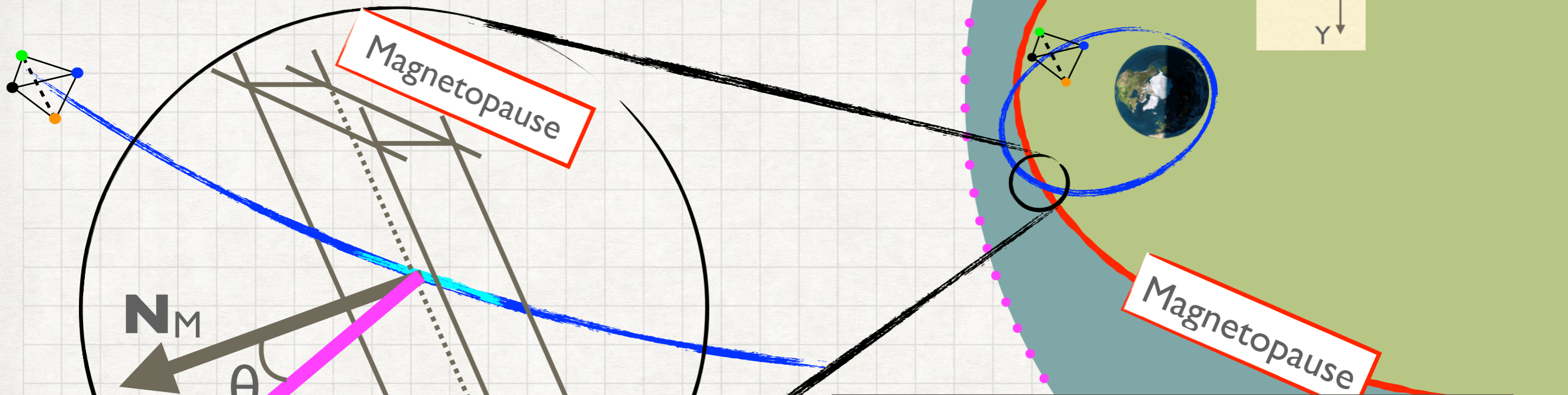
return

First 2-fluid simulations

Quantity	Function	Parameters	Normalized Parameters
$ B $	$a_{ B } + b_{ B } \left(\tanh\left(\frac{x-c_{ B }}{d_{ B }}\right) + b'_{ B } \tanh\left(\frac{x-c'_{ B }}{d_{ B }}\right) \right)$	$a_{ B } = 33.5 \text{ nT}$ $b_{ B } = -11.7 \text{ nT}$ $b'_{ B } = -0.5$ $c_{ B } = 151.9 \text{ km}$ $c'_{ B } = 486.4 \text{ km}$ $d_{ B } =$	$\tilde{a}_{ B } = 1.21$ $\tilde{b}_{ B } = -0.42$ $\tilde{b}'_{ B } = -0.5$ $\tilde{c}_{ B } = -0.30$ $\tilde{c}'_{ B } = 0.48$
$B_M \angle B_T$	$a_\alpha + b_\alpha \tanh\left(\frac{x-c_\alpha}{d_\alpha}\right) + a'_\alpha$	a_α	
B_M	$a_m + b_m \tanh\left(\frac{x-c_m}{d_m}\right)$		
B_L	$a_l + b_l \tanh\left(\frac{x-c_l}{d_l}\right)$		
N_i	$a_n + b_n \tanh\left(\frac{x-c_n}{d_n}\right)$		
U_i	$a_u (1 + \tanh\left(\frac{x-c_u}{d_u}\right))$	$a_u =$ $c_u =$ $d_u =$	
P_i	$a_{P_i} + b_{P_i} \tanh\left(\frac{x-c_{P_i}}{d_{P_i}}\right)$	$a_{P_i} = 2133 \text{ eV/cm}^3$ $b_{P_i} = 933 \text{ eV/cm}^3$ $c_{P_i} = 57.6 \text{ km}$ $d_{P_i} = 55.8 \text{ km}$	$\tilde{a}_{P_i} = 0.558$ $\tilde{b}_{P_i} = 0.244$ $\tilde{c}_{P_i} = -0.52$ $\tilde{d}_{P_i} = 0.13$
P_e	$a_{P_e} + b_{P_e} \tanh\left(\frac{x-c_{P_e}}{d_{P_e}}\right)$	$a_{P_e} = 136.8 \text{ eV/cm}^3$ $b_{P_e} = 98.5 \text{ eV/cm}^3$ $c_{P_e} = 140.6 \text{ km}$ $d_{P_e} = 74.7 \text{ km}$	$\tilde{a}_{P_e} = 0.036$ $\tilde{b}_{P_e} = 0.026$ $\tilde{c}_{P_e} = -0.33$ $\tilde{d}_{P_e} = 0.17$



Magnetopause orientations



Analysis methods	<u>explications_glob</u>	<u>explications_loc</u>
	global	local
single	MVA	LNA Rezeau[2017], Sb->JGR
multi	CVA	MDD Shi[2005]

16/10/2015	13:05:30+60s		13:05:44+5s	
	mean	std	mean	std
MDD vs LNA_max	2.04E+01	1.89E+01	7.71E+00	5.79E+00
MDD vs MVAB	1.38E+01	1.02E+01	2.44E+01	4.49E+00
LNA_max vs MVAB	3.52E+01	2.12E+01	3.21E+01	2.94E+00

16/10/2015	10:37:01+35s		10:37:15+3s	
	mean	std	mean	std
MDD vs LNA_max	7.63E+00	8.66E+00	1.55E+00	2.38E-01
MDD vs MVAB	1.47E+01	1.18E+01	1.43E+01	1.76E+00
LNA_max vs MVAB	1.79E+01	1.08E+01	1.26E+01	1.40E+00
MDD vs Shue	2.70E+01	1.54E+01	3.52E+01	1.71E+00
MDD vs LNA_fpi	1.52E+01	4.27E+00	1.27E+01	4.61E-01
LNA_fpi vs Shue	2.52E+01	6.23E+00	2.25E+01	1.22E+00
LNA_fpi vs MVAB	7.62E+00	6.39E+00	3.31E+00	1.99E+00
LNA_max vs Shue	3.85E+01	1.08E+01	3.35E+01	1.35E+00
LNA_fpi vs LNA_max	1.47E+01	7.29E+00	1.14E+01	7.05E-01

	12:05:39+5s		
	std	mean	std
MDD vs Shue	2.38E+01	9.36E+00	4.68E+00
MDD vs LNA_fpi	1.23E+01	3.68E+01	1.99E+01
LNA_fpi vs Shue	2.25E+01	4.01E+01	2.30E+01
LNA_fpi vs MVAB	1.09E+01	3.15E+01	1.64E+01
LNA_max vs Shue	2.07E+01	9.32E+00	4.97E+00
LNA_fpi vs LNA_max	2.06E+01	3.40E+01	1.64E+01
LNA_fpi vs MVAB	2.19E+01	3.86E+01	2.20E+01
LNA_max vs Shue	3.59E+01	2.12E+01	3.58E+01
LNA_fpi vs LNA_max	8.95E+00	2.54E+00	1.10E+00