

# EXTENDED SUDDEN APPROXIMATION FOR HIGH ENERGY NUCLEON REMOVAL

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*Summary*

1. **INTRODUCTION**
  2. **BASIC ASSUMPTIONS**
  3. **BREAKUP PROBABILITIES**
  4. **MOMENTUM DISTRIBUTIONS**
  5. **COULOMB DISSOCIATION**
  6. **RESULTS**
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# Breakup

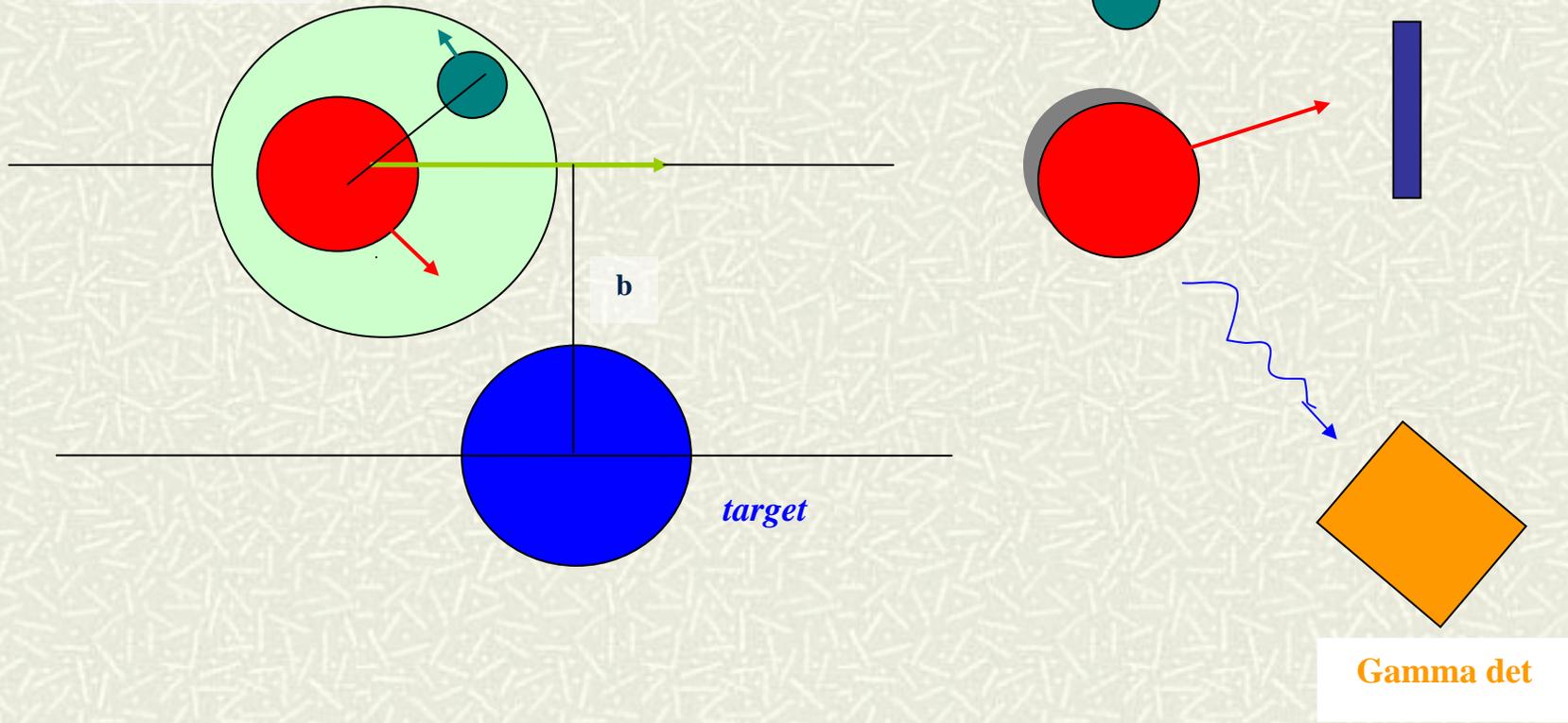
**breakup of loosely bound nuclei**

*projectile  
halo nucleus*

*after*

**Particle det**

**Gamma det**

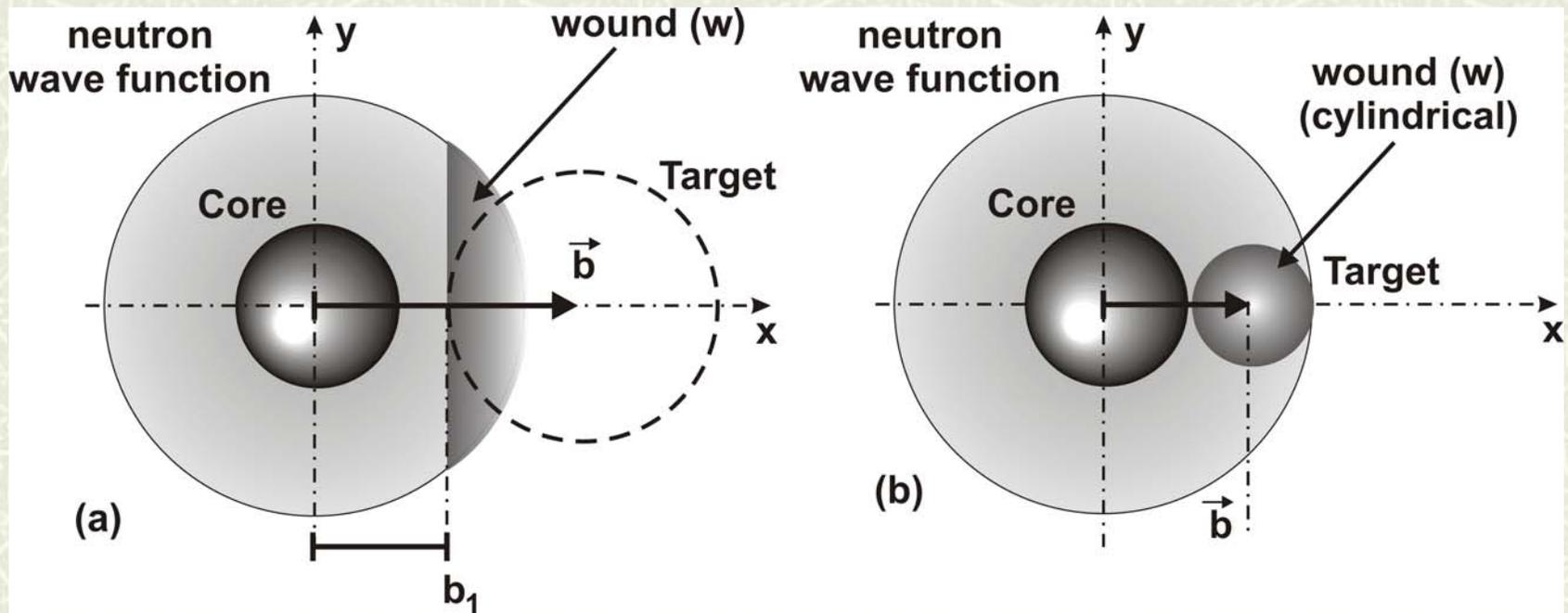


## 2. *Basic assumptions of the model*

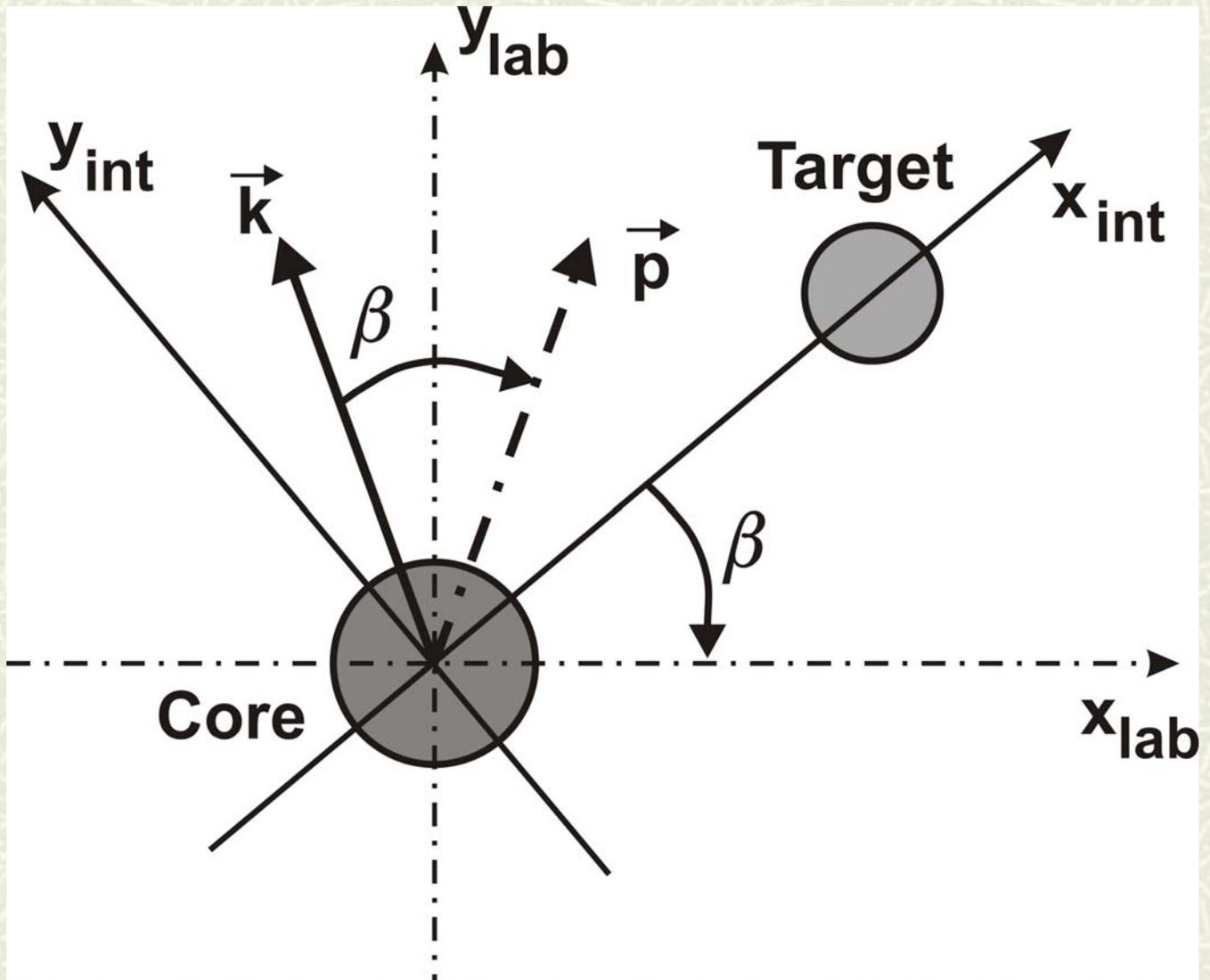
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- # The reaction proceeds by instantaneous removal of a nucleon from the projectile without disturbing the remaining nucleons
  - # **High energy regime. The intrinsic velocity of the valence nucleon is much smaller than the projectile velocity.**
  - # The projectile and the fragment follow straight line trajectories.
  - # Final state interactions are neglected.
  - # Target is a black disk. The absorbed nucleon is not observed.
  - # **One bound state. The transition probabilities to the continuum are calculated via sum rules.**
  - # Only the transverse component of the momentum transfer generated by Coulomb interaction is retained.
-

# Schematic layout



# Coordinates



# 3. Breakup probabilities

The ground state of the projectile

$$|J^\pi \rangle = [I_c^\pi \otimes nlj]^{J^\pi}$$

$$\sigma_{-1n}(I_c^\pi) = \sum_{nlj} C^2 S(I_c^\pi, nlj) \sigma_{sp}(nlj, S_n^{eff}).$$

The removed part of the wave function is

$$\delta\psi(\vec{r}) = \begin{cases} \psi_0(x, y, z) & \text{if } (x, y, z) \in (w) \\ 0 & \text{otherwise.} \end{cases}$$

The complement ( $\bar{\psi}$ )

$$\psi_0 = \bar{\psi} + \delta\psi$$

$$\int d\vec{r} \bar{\psi}^* \delta\psi = \int d\vec{r} \bar{\psi} \delta\psi^* = 0$$

The stripping (absorption) probability

$$P_a(b) = \int d\vec{r} |\delta\psi|^2$$

The wave function after collision

$$\psi(\vec{r}) = e^{i\phi^t}(\psi_0 - \delta\psi) = e^{i\phi^t} \bar{\psi}$$

The elastic content

$$\gamma_{el} = \int d\vec{r} \psi \psi_0^*(\vec{r})$$

The decaying state ( $\psi_d(\vec{r})$ ),

$$\psi_d(\vec{r}) = \psi_0(\vec{r}) - \delta\psi(\vec{r}) - \gamma_{el} e^{-i\phi^t} \psi_0(\vec{r})$$

The elastic probability

$$P_{el}(b) = 1 - P_a(b) - |\gamma_{el}(b)|^2$$

## I. ELASTIC PROBABILITY

The elastic probability defined by,

$$\gamma_{el} = \int d\vec{r} \psi_0^*(\vec{r}) e^{iq\vec{r}} (\psi_0 - \delta\psi) \equiv \gamma_C - \gamma_{C+N}$$

$$|\gamma_{C+N}|^2 = \hat{\rho}_0^2 \frac{4\pi^2 R_t^2}{q^2} J_1^2(qR_t)$$

## 5. Coulomb dissociation in sudden approximation

$$\vec{R}(t) = \vec{b} + vt\hat{z}$$

$$V_2(\vec{r}, t) = V_{nat}(\vec{r} + \vec{R}(t)) + V_{dip}(\vec{r}, t),$$

$$V_{dip}(\vec{r}, t) = \frac{Z_c Z_t e^2}{A_p} \frac{\vec{r} \vec{R}(t)}{R^3(t)}.$$

The TC breakup amplitude,

$$g_{lm}(\vec{k}, \vec{b}) = \frac{1}{i\hbar} \int_{-\infty}^{\infty} dt \langle \phi^f | V_2(\vec{r}, t) | \phi_{lm}^i \rangle$$

$$g_{lm}(\vec{k}, \vec{b}) = \frac{1}{i\hbar} \int d\vec{r} \int dt e^{-i\vec{k}\vec{r} + i\omega t} e^{\frac{i}{\hbar} \int_t^{\infty} dt' V_2(\vec{r}, t')} V_2(\vec{r}, t) \phi_{lm}(\vec{r}) \equiv \langle \vec{k} | I(\omega) | lm \rangle$$

$$I_C(\omega) = \frac{1}{i\hbar} \int_{-\infty}^{\infty} dt e^{i\omega t} e^{\frac{i}{\hbar} \int_t^{\infty} dt' V_{dip}(t')} V_{dip}(t).$$

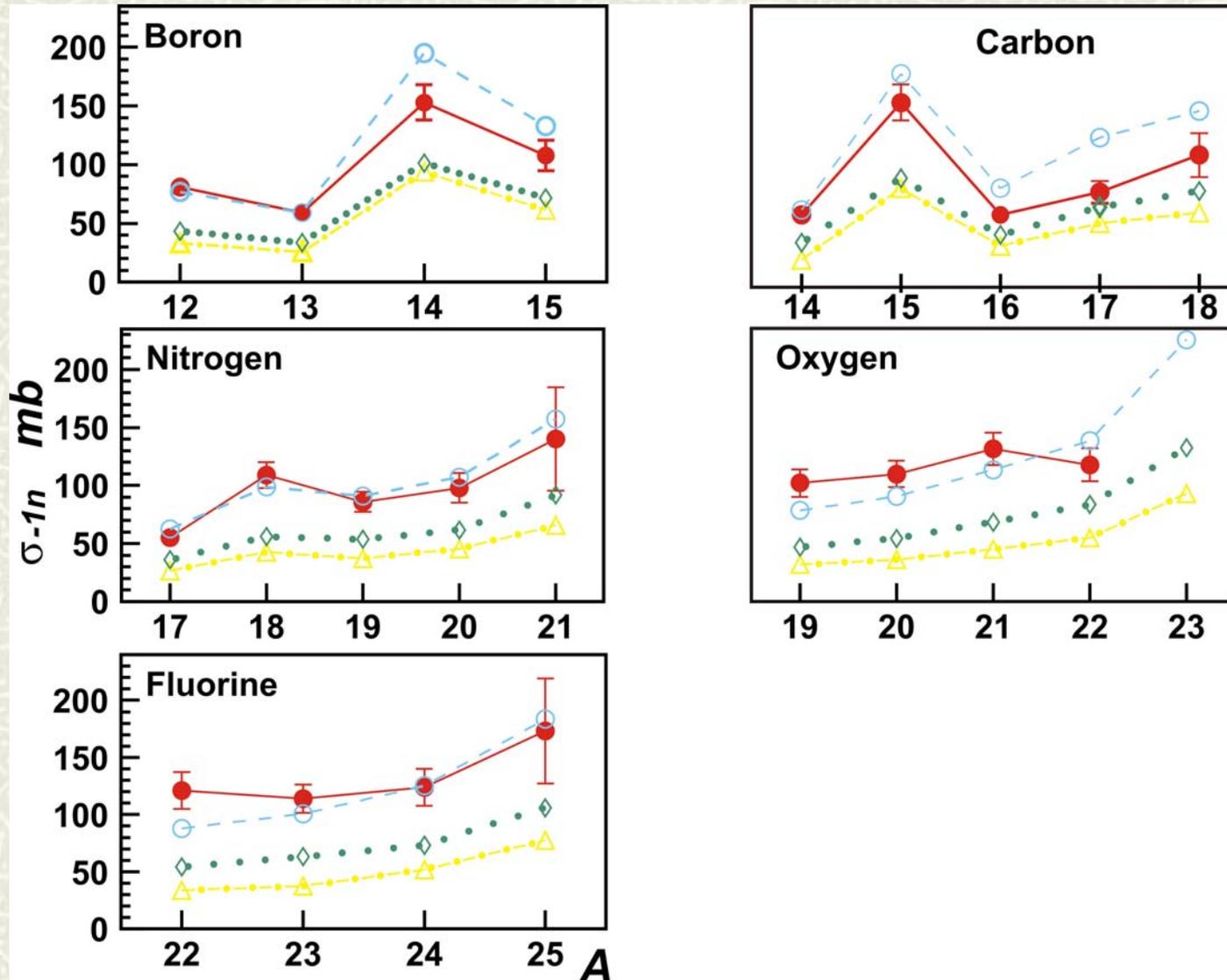
$$I_C^{sa} = e^{-i\chi_C} - 1$$

with,

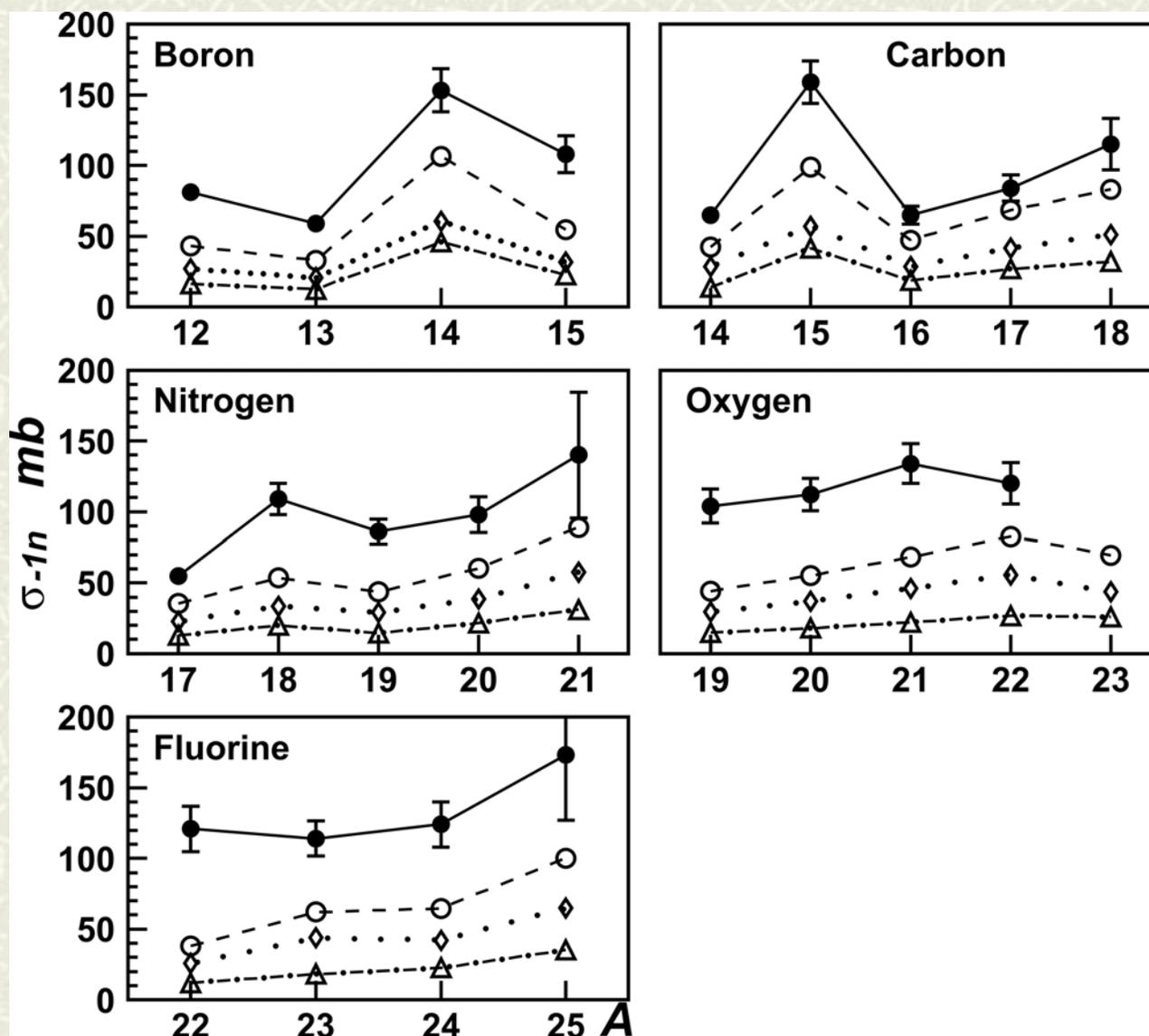
$$\chi_C = \frac{1}{\hbar} \int_{-\infty}^{\infty} dt V_{dip}(t) = \frac{1}{\hbar} \int_{-\infty}^{\infty} dt \frac{Z_c Z_t e^2}{A_p} \frac{\vec{s}\vec{b} + zvt}{(b^2 + v^2 t^2)^{3/2}} = \frac{2Z_c Z_t e^2}{A_p} \frac{\vec{s}\vec{b}}{\hbar v b^2}$$

$$e^{i\chi_C} \equiv e^{i\chi_C}$$

# One neutron-removal cross sections in the planar cut-off approximation



# One neutron-removal cross sections in the cylindrical wound approximation

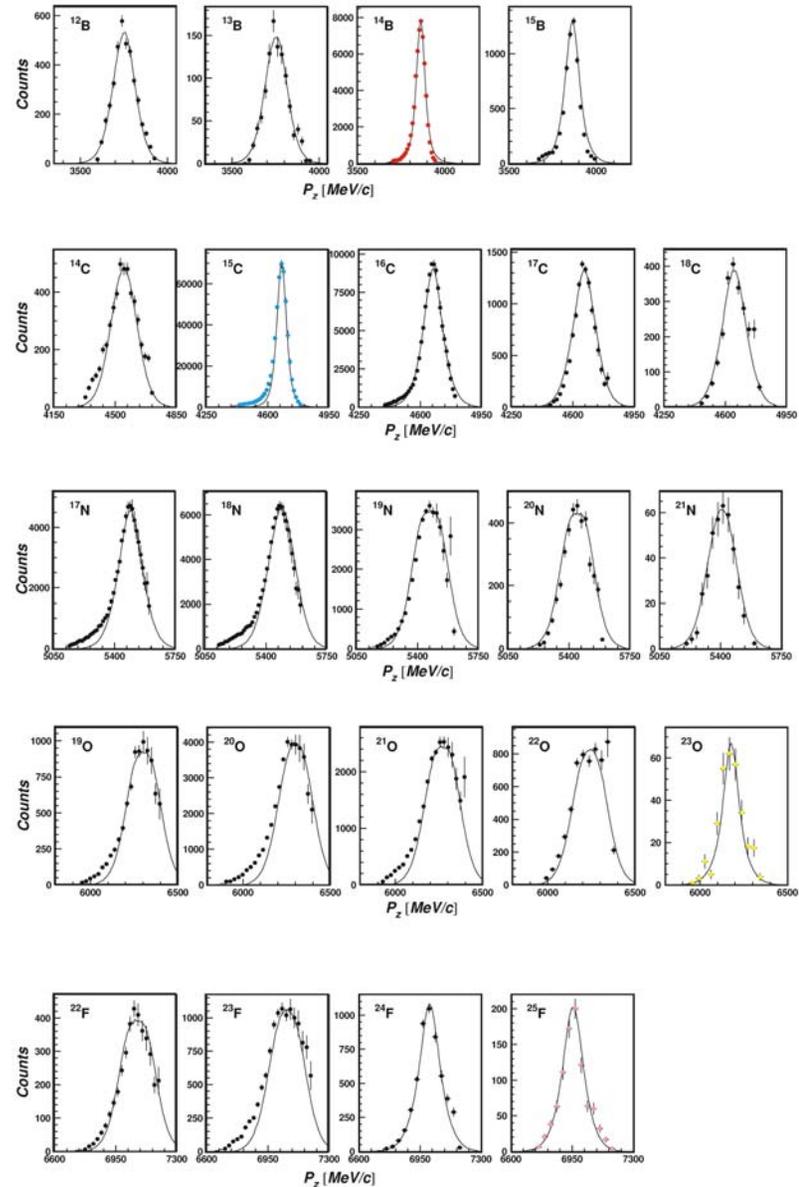


# 4. Parallel momentum distributions

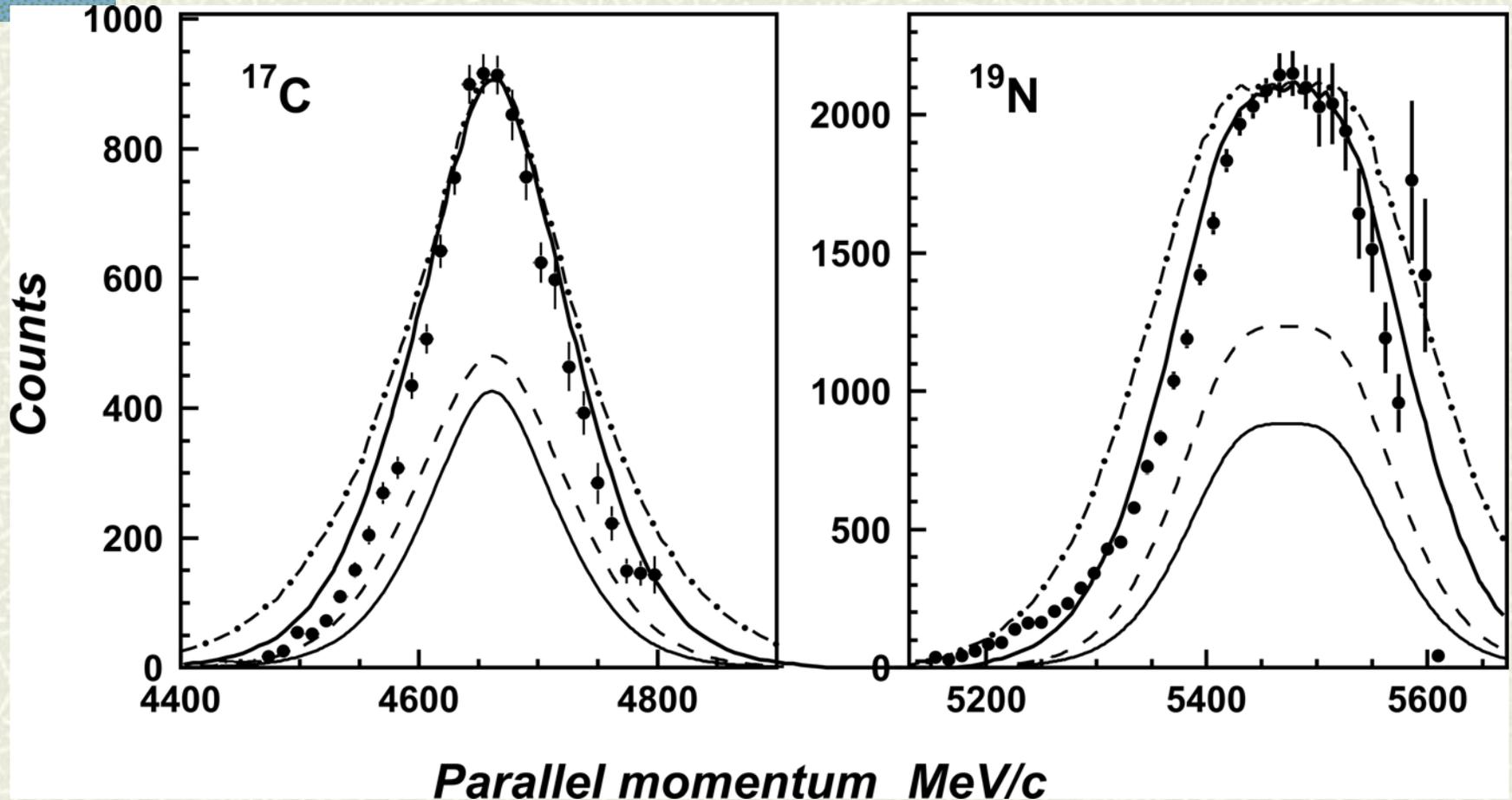
One neutron-removal reactions for nuclei in psd-shells  $E/A=40-60$  MeV/u

Data from:

E. Sauvan et al., Phys Rev C 69 (2004), in press



# *Sudden approx vs Extended Glauber*



# Transverse momentum distributions

■ **Another result:** One neutron-removal reactions for nuclei in psd-shells  
 $E/A=40-60$  MeV/u

Data from:

E. Sauvan et al., Phys Rev C 69 (2004), in press

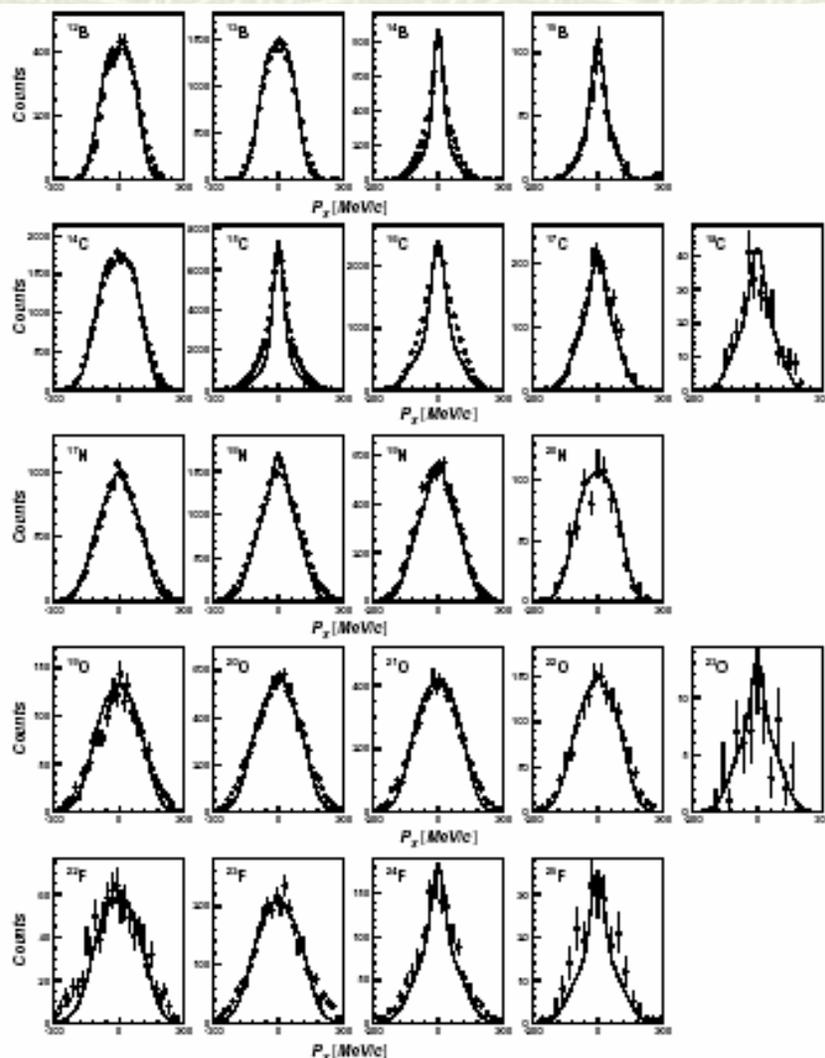
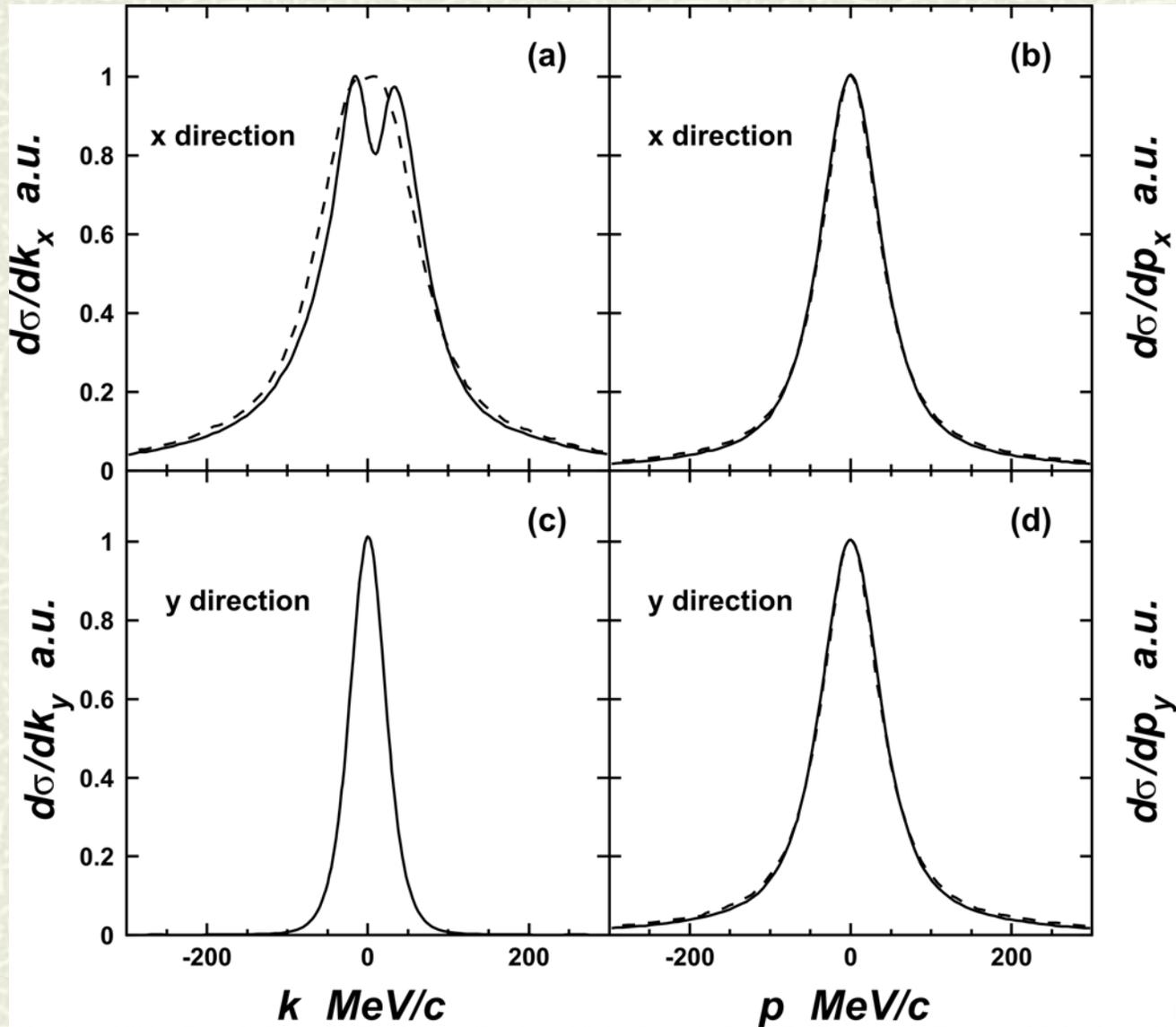
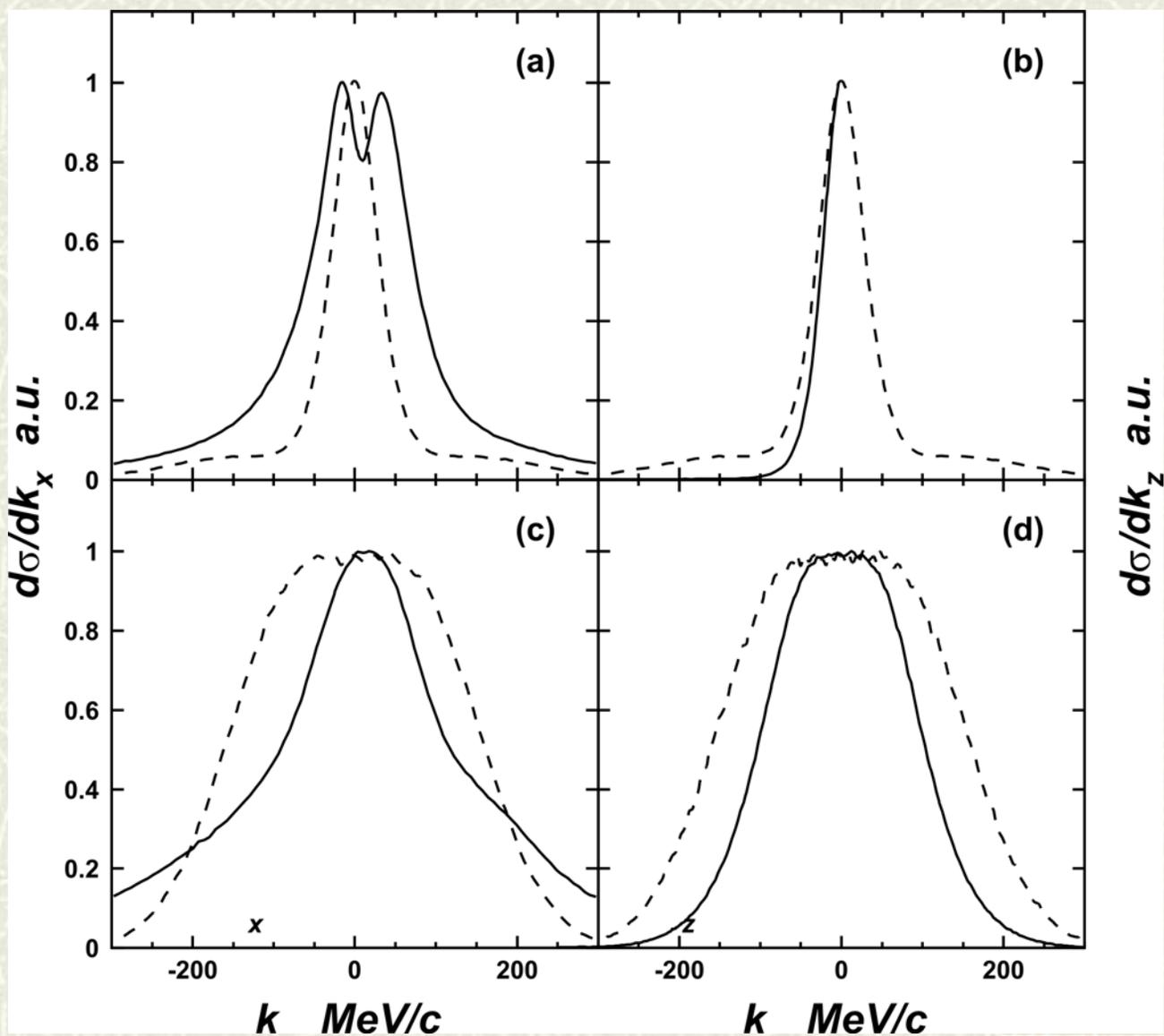


FIG. 1. Comparison of experimental core fragment transverse momentum distributions ( $p_x$ ) on carbon target and Glauber model calculations (plain line).

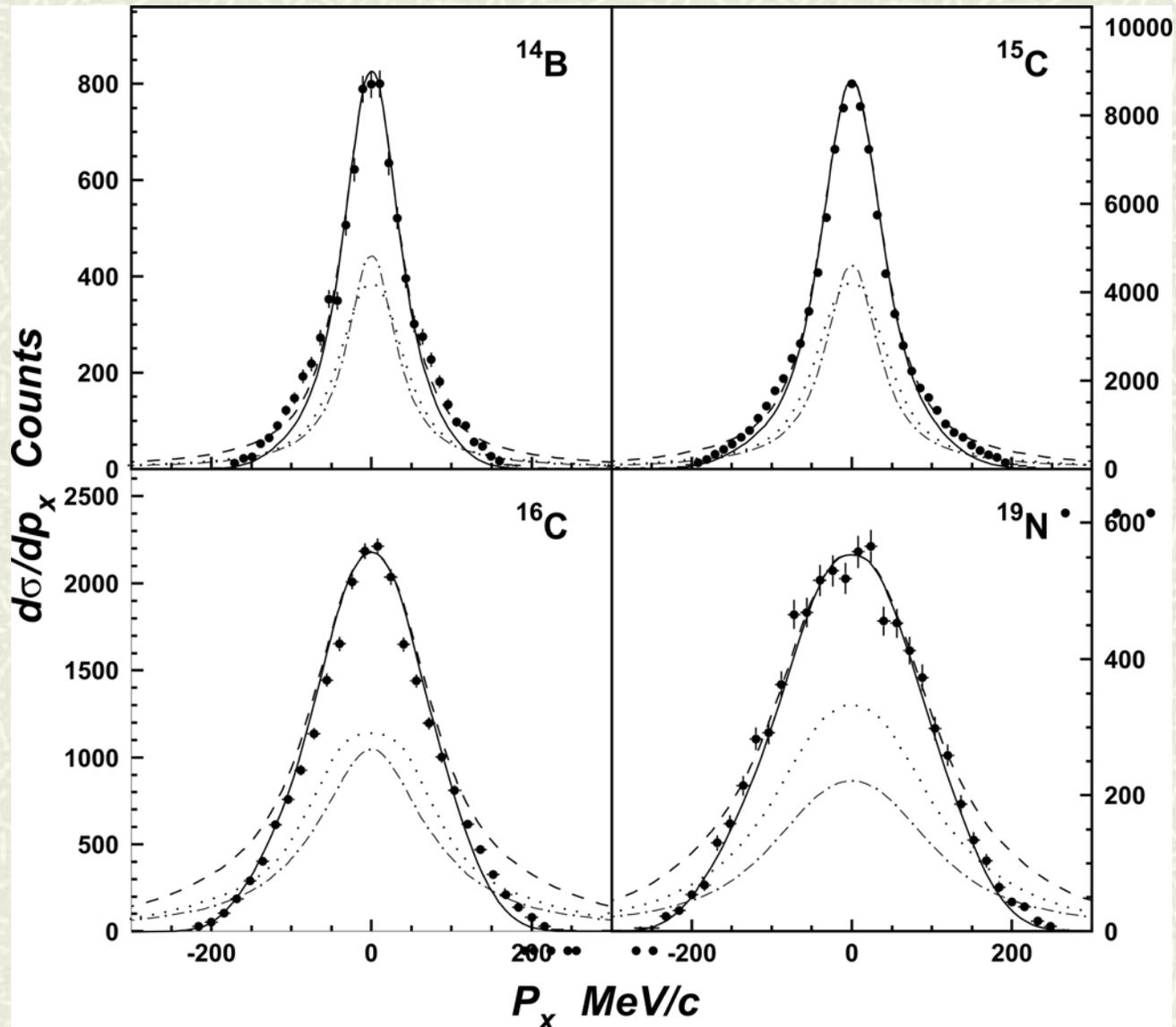
# *Rest frame and lab system distributions*



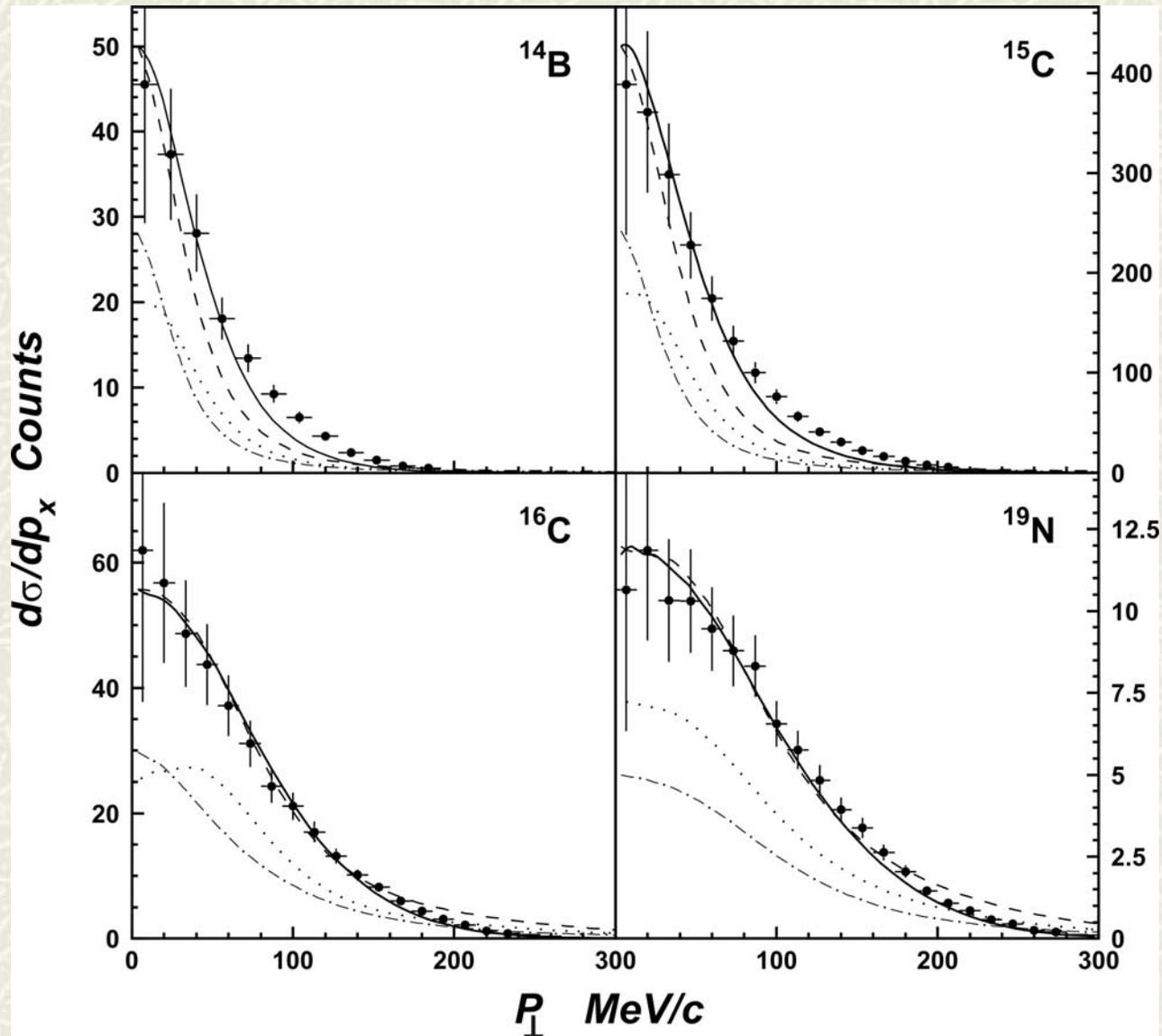
# Reaction model effects on the shape of distributions



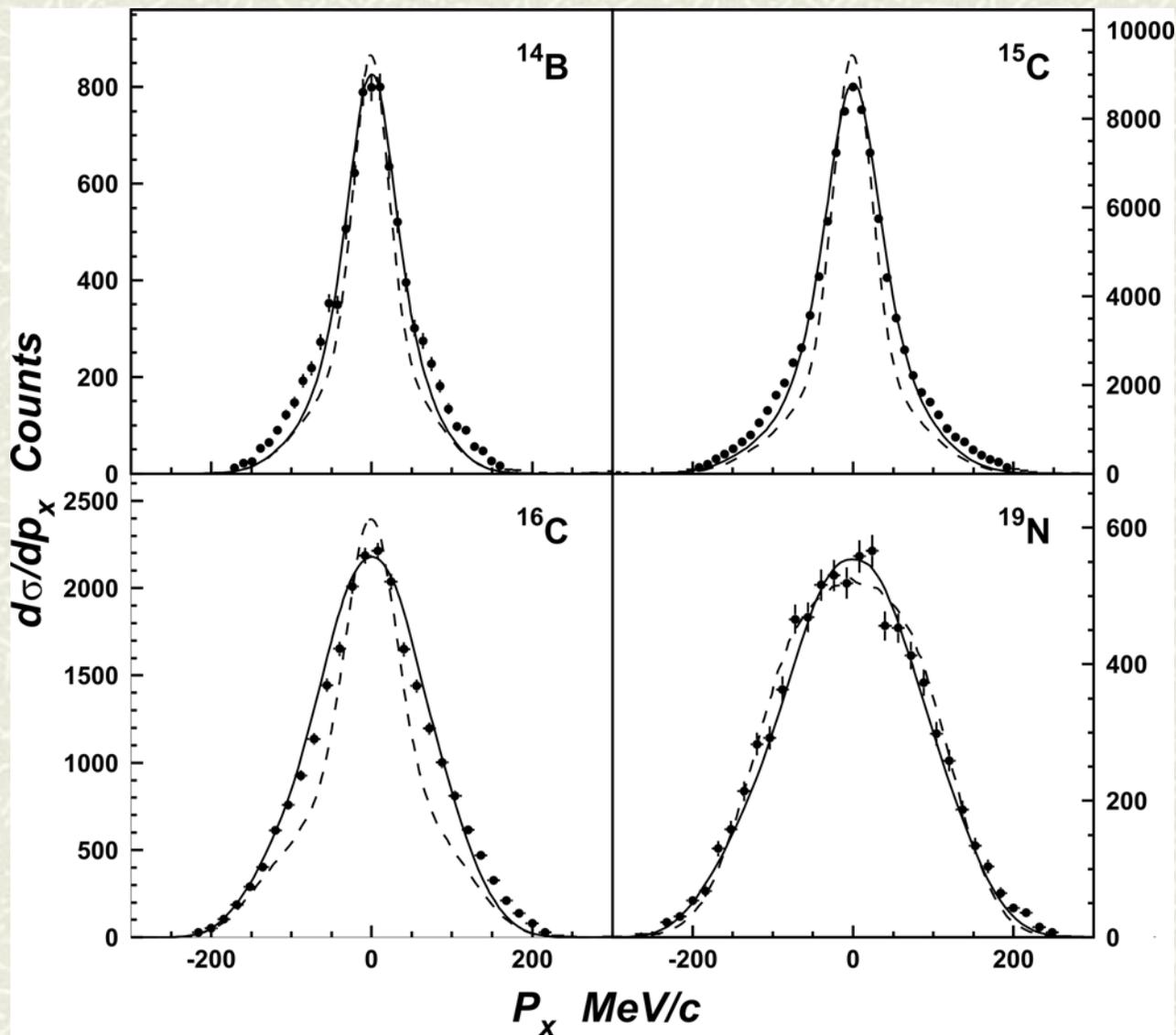
# Transverse momentum distributions



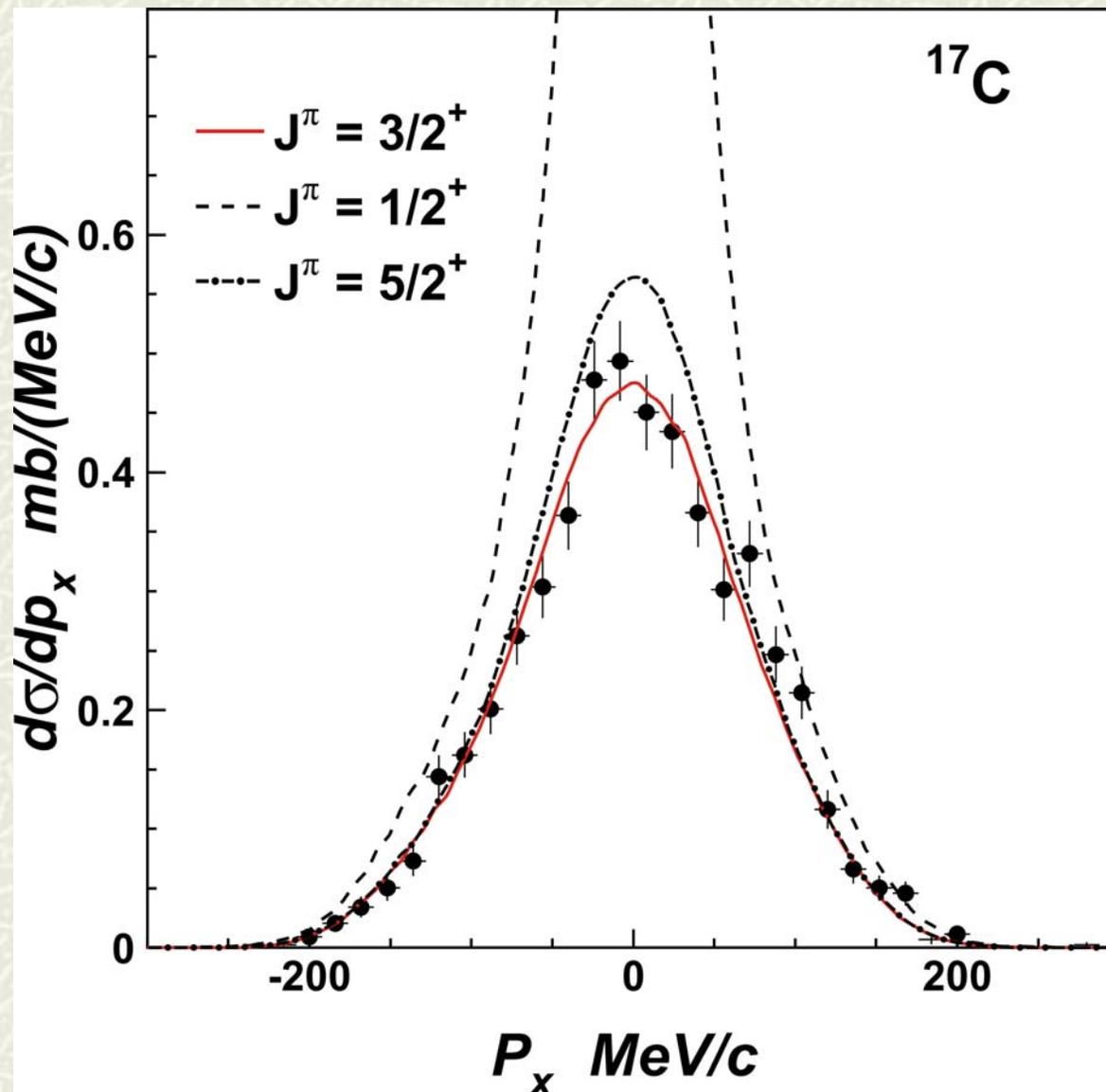
# Perpendicular momentum distributions



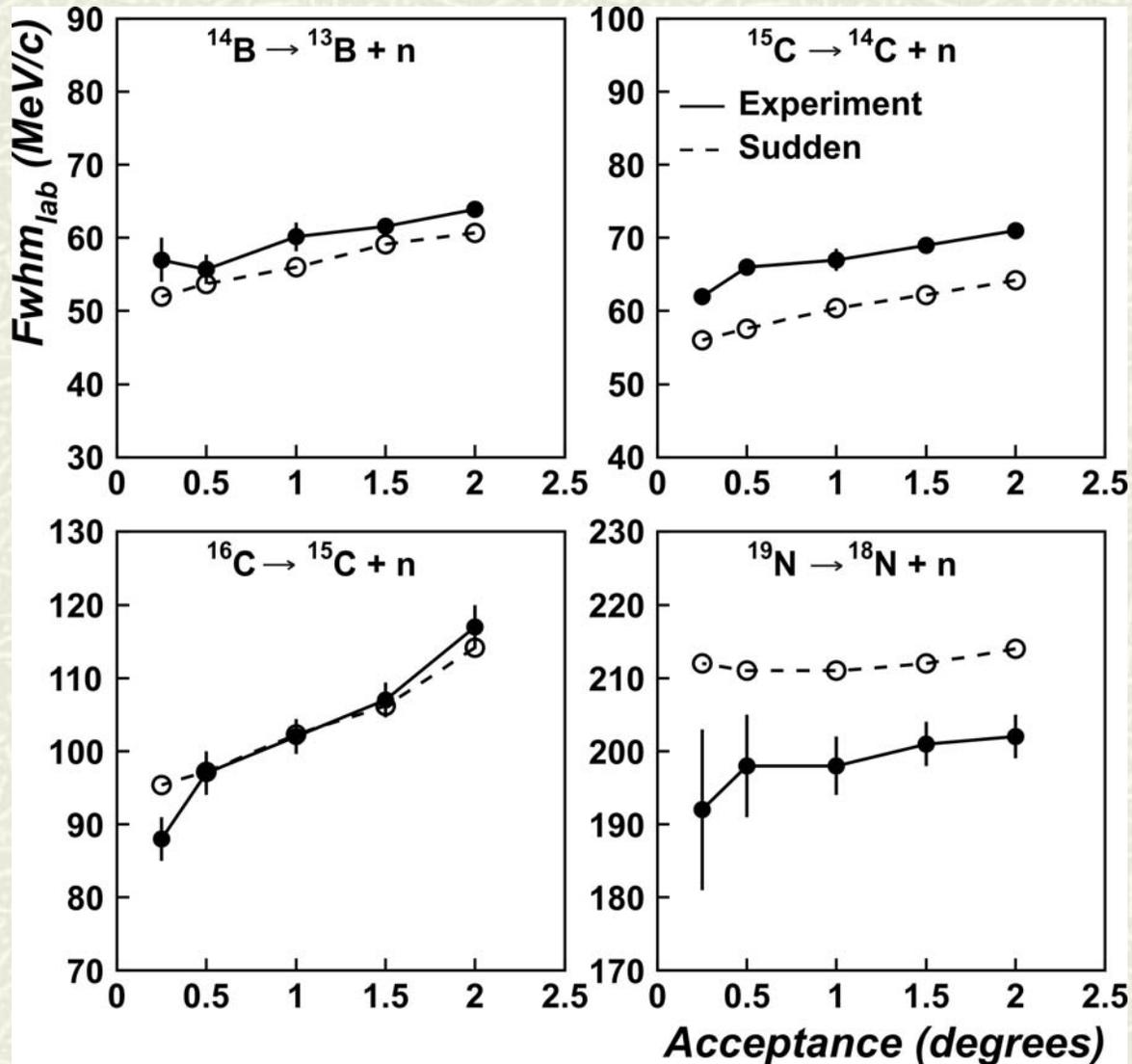
# *Sudden vs Glauber – transverse mom distributions*



# *Transverse mom distrib as spectroscopic tool*

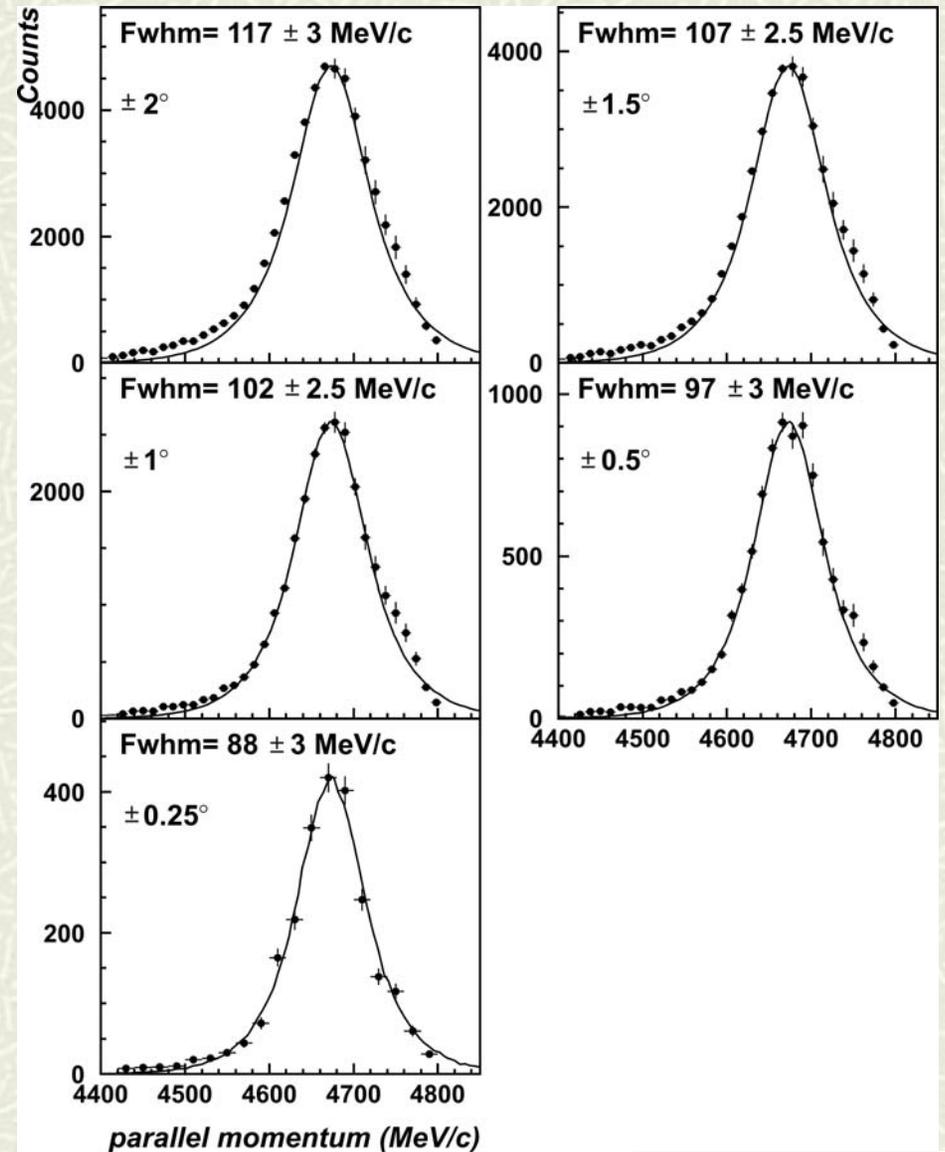


# Parallel distrib widths vs spectr acceptance



# $^{16}\text{C}$ case

#  $^{16}\text{C}$  one neutron-removal parallel mom distrib vs spectrometer acceptance



# $^{19}\text{N}$ case

#  $^{19}\text{N}$  one neutron-removal parallel mom distrib vs spectrometer acceptance

