

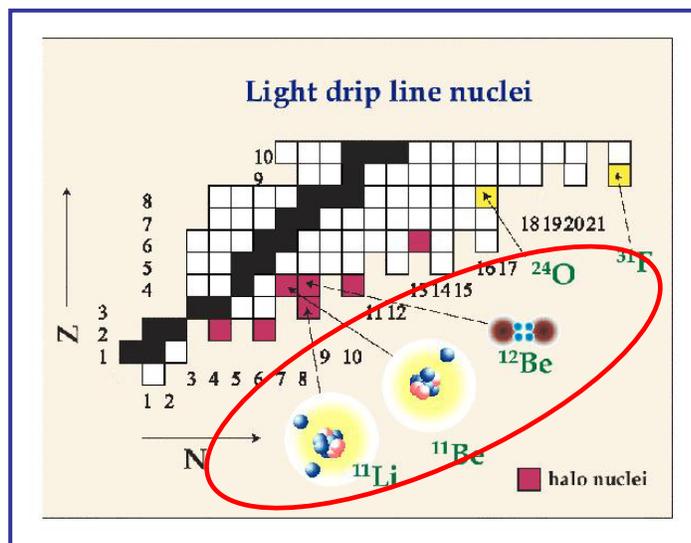
Particle-vibration coupling in halo nuclei

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F. Barranco (Sevilla)

F. Barranco et al., Eur.Phys.Jour. A 11(2001)385

G.Gori et al., nucl-th/0301097



Aim of the talk

To discuss the role of core polarization in halo nuclei.

To show that, based on limited phenomenological input, it is possible to provide a quantitative calculation of the basic features of ^{11}Be , ^{12}Be , ^{10}Li , ^{11}Li and of the spectroscopic factors, in reasonable agreement with experiment.

The parity inversion problem in ^{11}Be

	^{11}Be	^{10}Be
Separation energy	0.5 MeV	6.8 MeV
Lowest excited state	0.32 MeV,	3.4 MeV
Radius	3 fm	2.3 fm

Good situation for the mean field approximation:

But! The quantum numbers of the ground state are not those predicted by the mean field (1p1/2)

. *but 2s1/2, in the next shell!!*

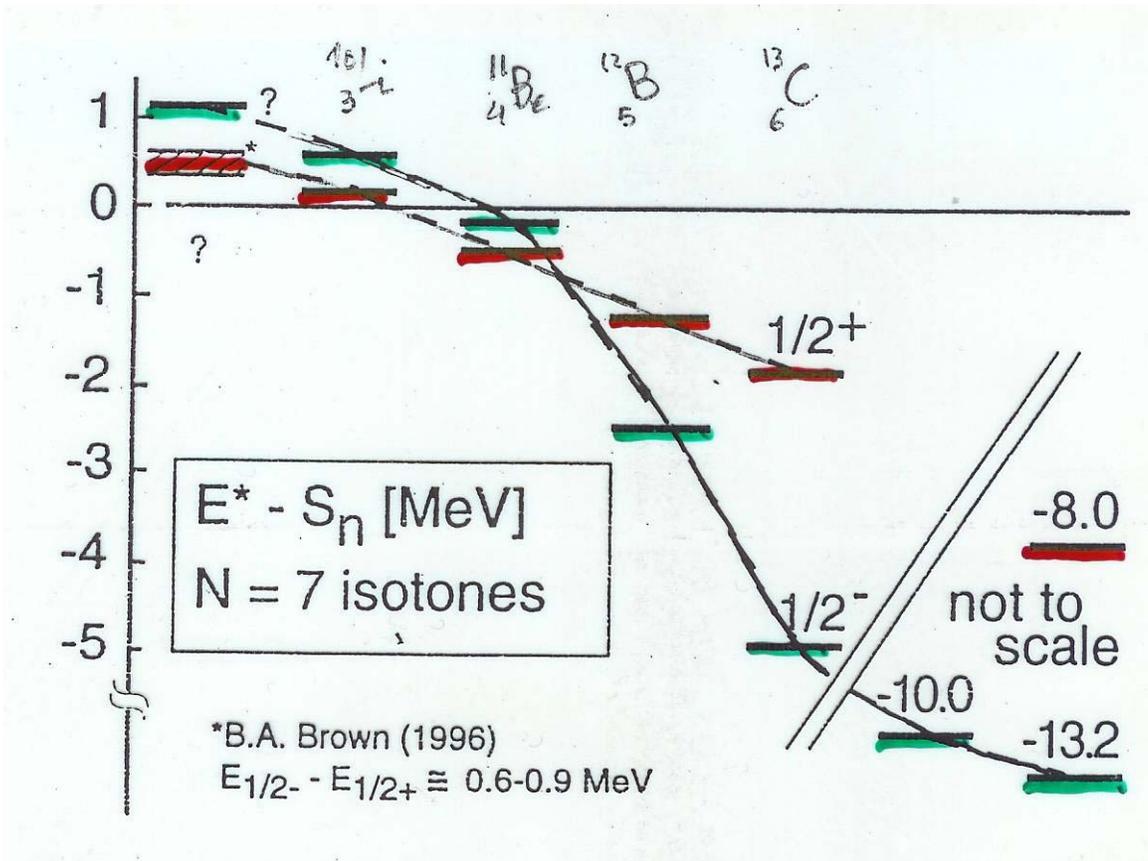
Stronger spin-orbit force for halo states?

(N. Vinh Mau, *Nucl. Phys. A592(95)33*)

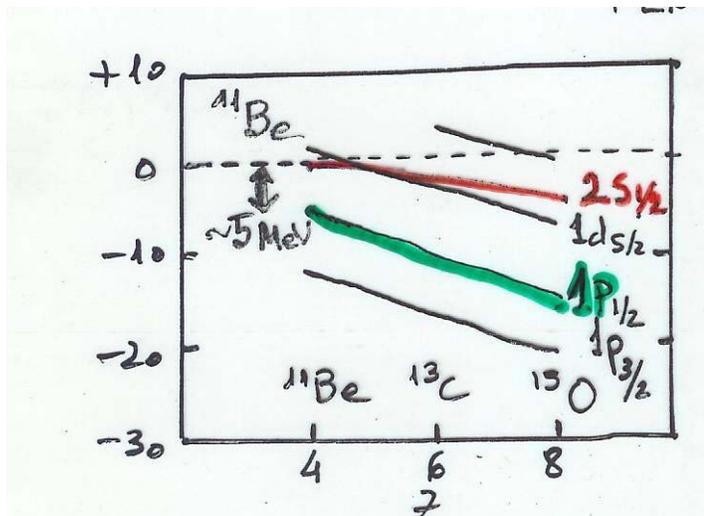
(F. Nunes et al., *Nucl. Phys. A596(96)171*)

.

Experimental systematics

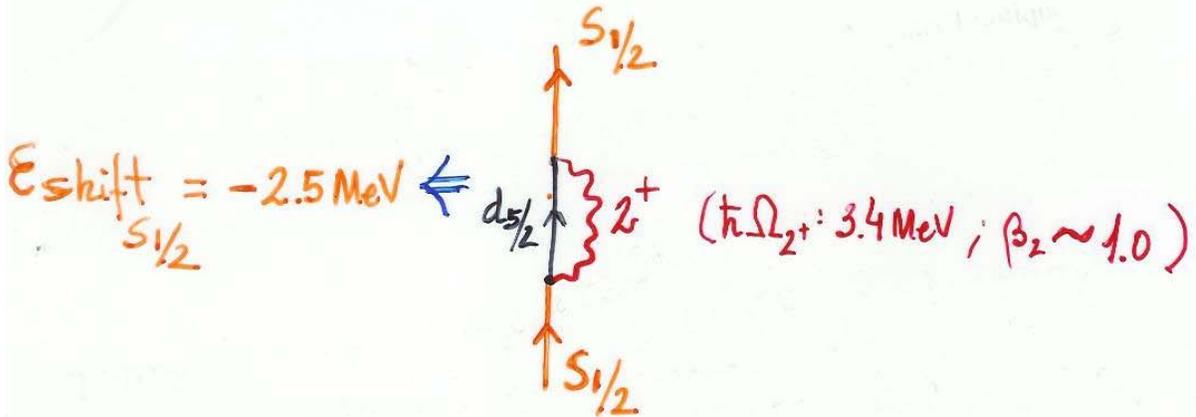


Mean-field results with Skyrme force (Sagawa, Brown, Esbensen PLB 309(93)1)

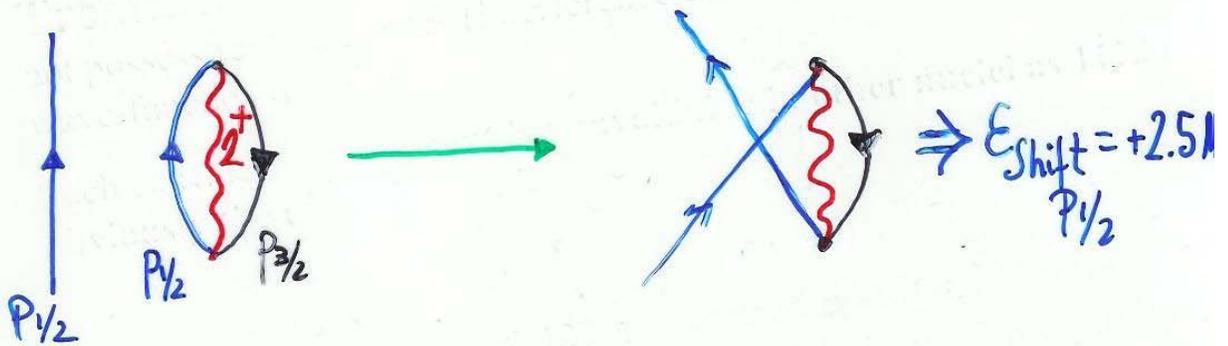


A. SELF ENERGY

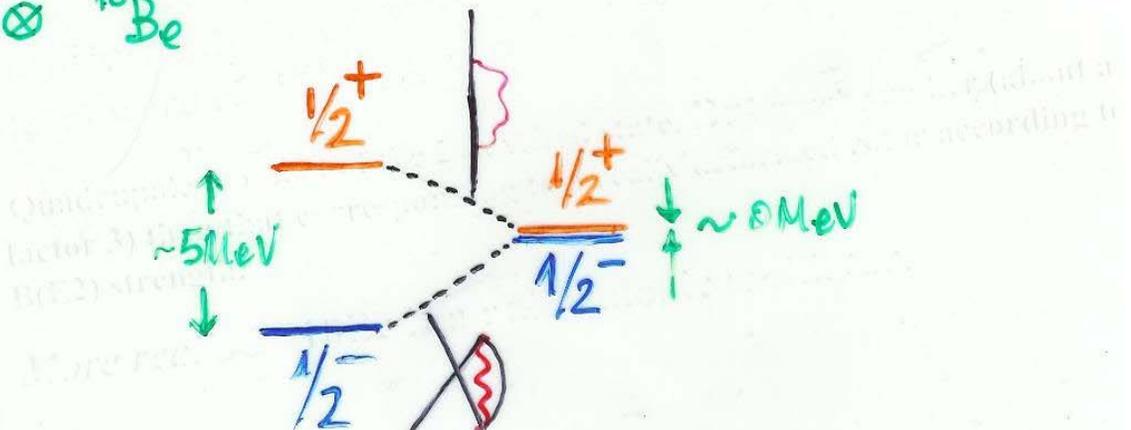
(¹¹Be case: Sagawa, Brown & Esbensen, Phys Rev B(1981))

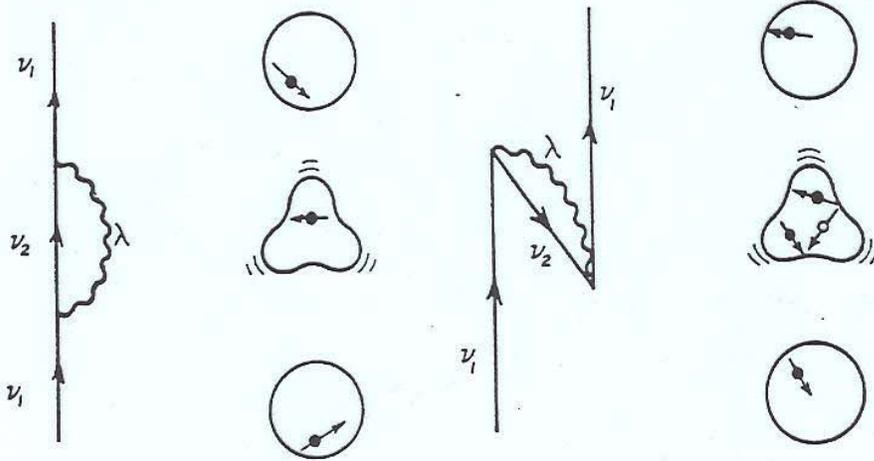


B. PAULI BLOCKING OF \sqrt{V} GROUND STATE CORRELATIONS

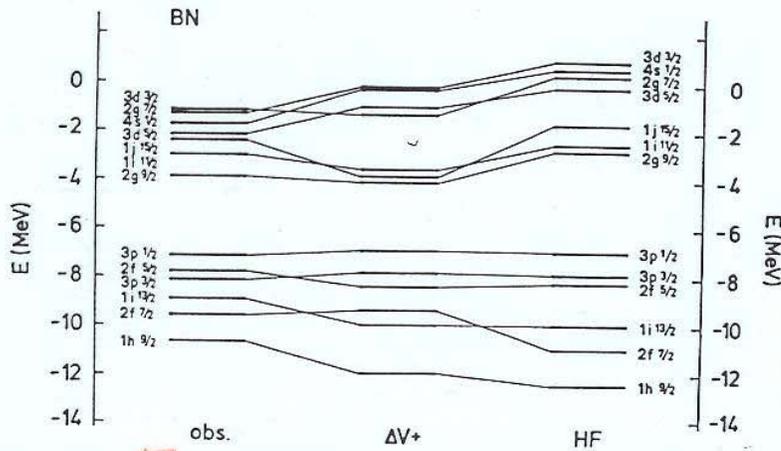


$n \otimes {}^{10}\text{Be}$





→ Phys. Rep. 120(85)1



Bernard & Van Giai
Nud. Phys. A.348 (1975)

Fig. 4.29. Representation of the results of Bernard and Nguyen Van Giai [96] for the neutron quasiparticle energies in the valence shells of ^{208}Pb . The observed values are plotted on the left-hand side and the results of the Skyrme III-Hartree-Fock approximation on the right-hand side. The middle column gives the quasiparticle energies, see section 4.6.5.

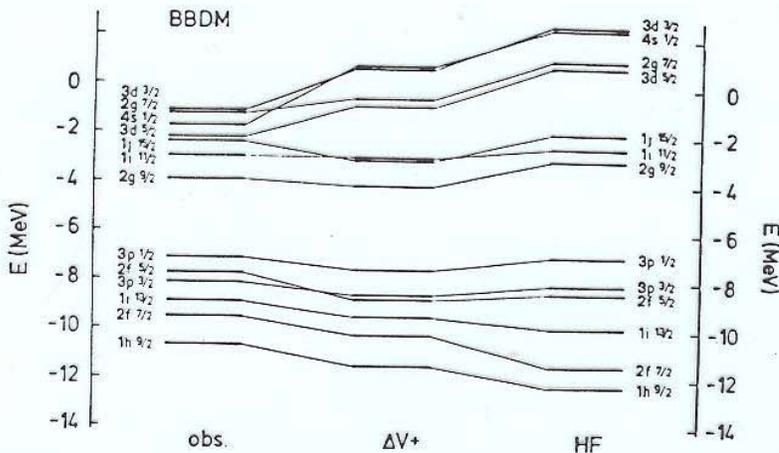


Fig. 4.30. Representation of the results of Bortignon et al. [315] for the neutron quasiparticle energies in the valence shells of ^{208}Pb . The notation is the same as in fig. 4.29.

COLLECTIVE SURFACE VIBRATIONS

WELL KNOWN
FROM EXP.

$$R(\hat{\sigma}) = R_0 \left\{ 1 + \sum_{\lambda\mu} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\hat{\sigma}) \right\} \quad ; \quad \lambda = 2, 3, 4, 5$$

$$H_{\text{coll}} = \frac{1}{2} \sum_{\lambda\mu} (B_{\lambda} |\dot{\alpha}_{\lambda\mu}|^2 + C_{\lambda} |\alpha_{\lambda\mu}|^2) \quad ; \quad \hbar\omega_{\lambda} = \hbar \sqrt{\frac{C_{\lambda}}{B_{\lambda}}}$$
$$\beta_{\lambda} = \sqrt{2\lambda+1} \sqrt{\frac{\hbar\omega_{\lambda}}{2C_{\lambda}}}$$

The values of $\hbar\omega_{\lambda}$ and β_{λ} are taken from experiment or alternatively from an RPA calculation

THE MODEL HAMILTONIAN

$$H = \frac{p^2}{2m} + U(\vec{r}; \alpha) + H_{\text{coll}}$$

where

$$U(\vec{r}; \alpha) = U_0 \left(\frac{r}{1 + \sum_{\lambda\mu} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\hat{\sigma})} \right) \approx U_0(r) - r \frac{\partial U_0}{\partial r} \sum_{\lambda\mu} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\hat{\sigma})$$

$$\Rightarrow H = \frac{p^2}{2m} + U_0(r) + H_{\text{coll}} + H_{\text{pv}}$$

With

$$H_{\text{pv}} = -r \frac{\partial U_0}{\partial r} \sum_{\lambda\mu} \sqrt{\frac{\hbar\omega_{\lambda}}{2C_{\lambda}}} [O_{\lambda\mu}^+ + (-)^{\mu} O_{\lambda,-\mu}] Y_{\lambda\mu}(\hat{\sigma})$$

Pauli-blocking correlations

The ^{10}Be core itself is not a simple Slater determinant as supposed in mean field:

There are ground state correlations, that is, mixing of configurations → **partial occupation of orbits that in a pure mean field description are completely empty.**

When the halo neutron is added to form ^{11}Be , the extra neutron will partially block the single-particle orbits available for ^{10}Be to correlate: the binding energy decreases.

The effect is strongest when associated to the lowest "empty" orbit, that is to the $1p_{1/2}$ orbit.

In this way Sagawa, Brown and Esbensen explained the parity inversion in ^{11}Be .

Elaborating on the ^{11}Be calculation

New elements of our calculation:

Standard Woods-Saxon potential including spin-orbit according to Bohr and Mottelson

We include the (discretized) continuum for s-, p- and d-orbits:

Schrödinger equation solved with reflecting boundary conditions at a variable radius $R \Rightarrow$ infinity

The calculations have been carried out using the Nuclear Field Theory: . . .

a systematic and fully consistent scheme for the particle-vibration coupling. It allows a coherent treatment of

configuration mixing, . . .

Pauli-blocking correlations

$$U_0 = -50 \text{ MeV} + \frac{N - Z}{A} 33 \text{ MeV}$$

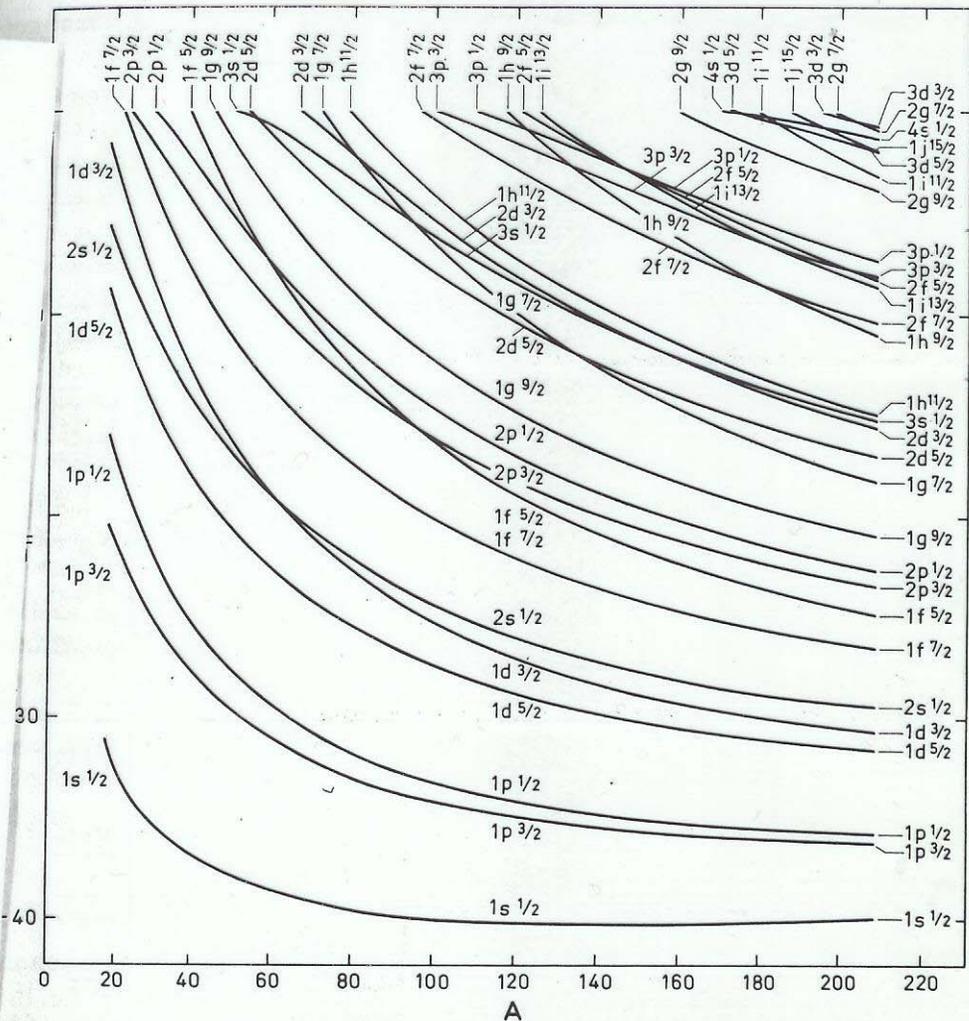
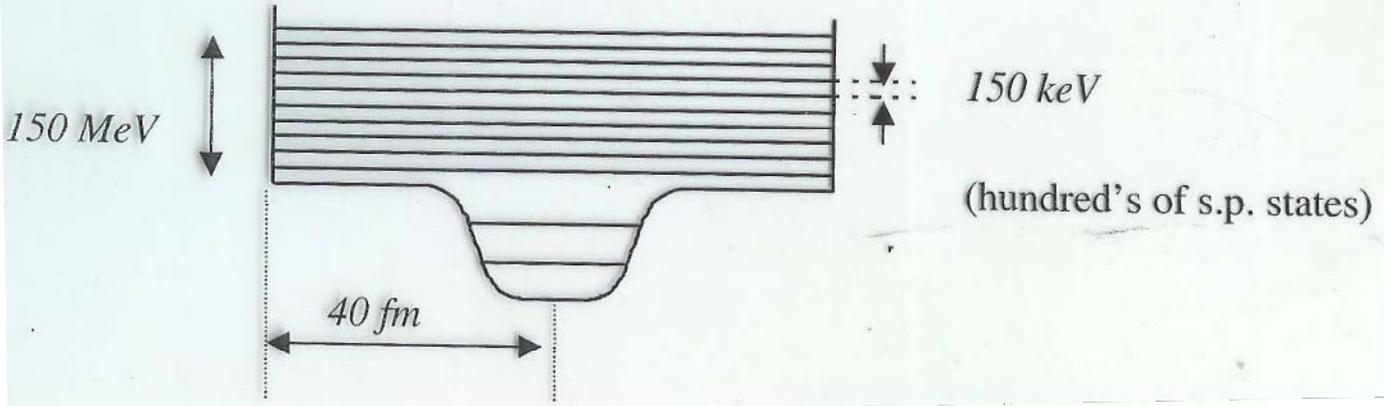
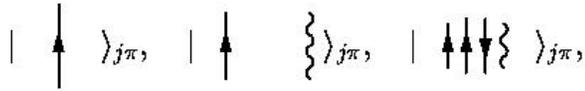


Figure 2-30 Energies of neutron orbits calculated by C. J. Veje (private communication).

^{11}Be



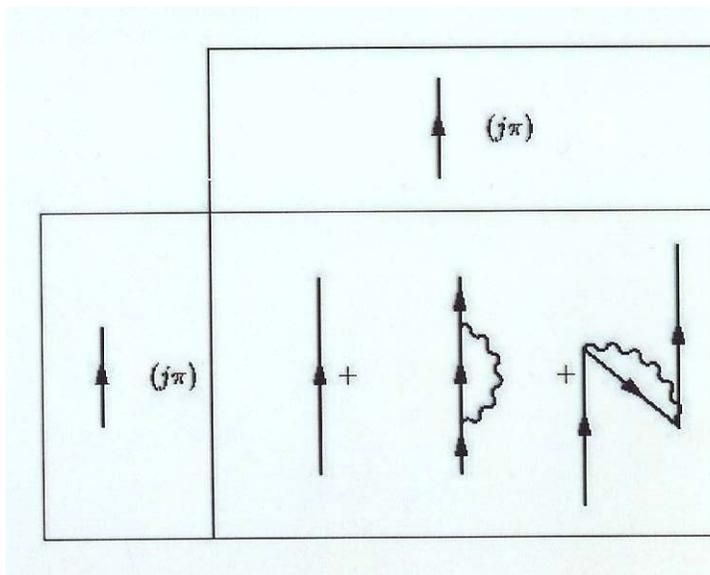
Fermionic degrees of freedom:

- s1/2, p1/2, d5/2 Wood-Saxon levels up to 150 MeV

Bosonic degrees of freedom:

- 2+ and 3- QRPA solutions with energy up to 50 MeV; residual interaction: multipole-multipole separable with the coupling constant tuned to reproduce $E(2^+) = 3.36$ MeV e $0.6 < \beta_2 < 0.7$

Effective, energy-dependent matrix (Bloch-Horowitz)



$$\begin{array}{c} b \\ \swarrow \\ \text{wavy line} \\ \uparrow \\ a \end{array} \omega_{\lambda} f_{\lambda} = \langle b | -r \frac{dU_0}{dr} \frac{1}{\lambda \mu} | a \rangle \sqrt{\frac{\hbar \omega_{\lambda}}{c_{\lambda}}}$$

$$\begin{array}{c} a \\ \uparrow \\ \text{wavy line} \\ \uparrow \\ a \end{array} \omega_{\lambda} f_{\lambda} = \frac{\left[\begin{array}{c} b \\ \swarrow \\ \text{wavy line} \\ \uparrow \\ a \end{array} \right]^2}{\tilde{E}_a - (E_b + \hbar \omega_{\lambda})}$$

$$\begin{array}{c} \text{wavy line} \\ \swarrow \quad \searrow \\ a \quad \quad a \end{array} \omega_{\lambda} f_{\lambda} = \frac{- \left[\begin{array}{c} c \\ \swarrow \\ \text{wavy line} \\ \uparrow \\ a \end{array} \right]^2}{\tilde{E}_a - (2\tilde{E}_a - E_c + \hbar \omega_{\lambda})}$$

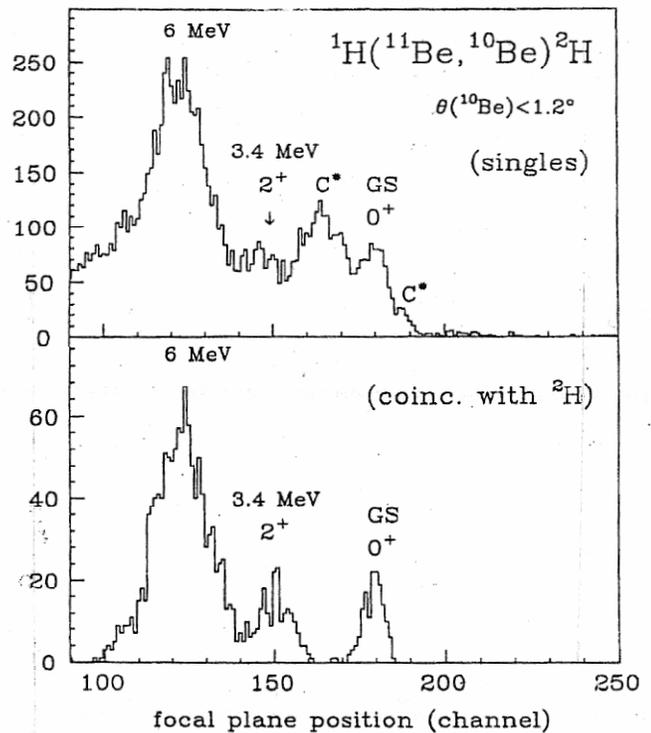
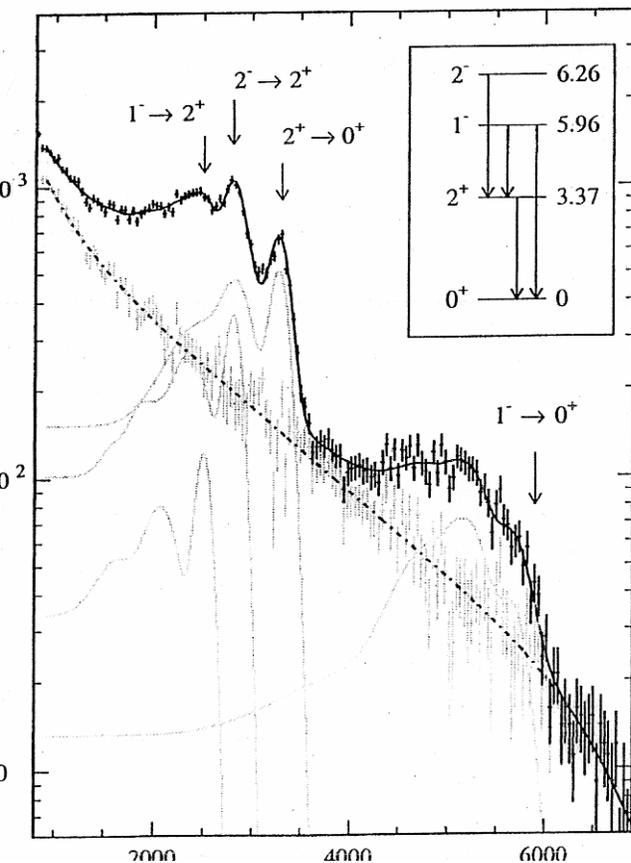
Admixture of $d_{5/2} \times 2^+$ configuration in the $1/2^+$ g.s. of ^{11}Be is about 20%

$^9\text{Be}(^{11}\text{Be}, ^{10}\text{Be} + \gamma) X$

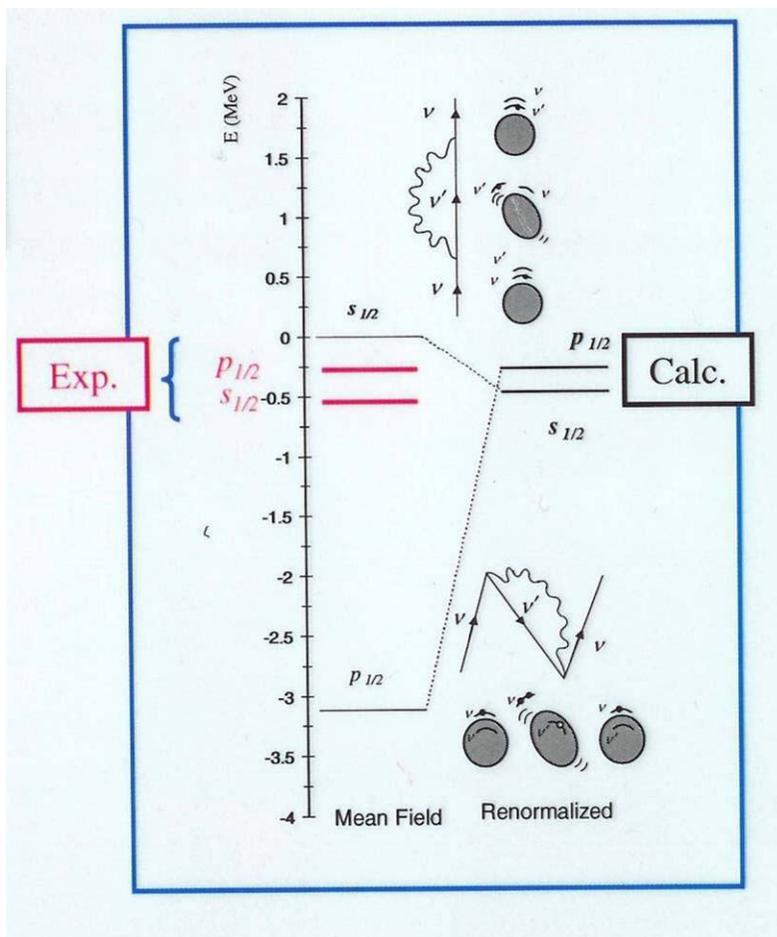
$p(^{11}\text{Be}, ^{10}\text{Be})d$

T. Aumann et al.
PRL 84(2000)35

S. Fortier et al.
Phys. Lett.B461(1999)22



Particle-vibration coupling in ^{11}Be



NFT ground state

$$|1/2+\rangle = \sqrt{0.87} |s_{1/2}\rangle + \sqrt{0.13} |d_{5/2} \otimes 2+\rangle$$

Exp.:

J.S. Winfield et al., Nucl.Phys. **A683** (2001) 48

$$|1/2+\rangle = \sqrt{0.84} |s_{1/2}\rangle + \sqrt{0.16} |d_{5/2} \otimes 2+\rangle$$

$^{11}\text{Be}(p,d)^{10}\text{Be}$ in inverse kinematic detecting both the ground state as well as the 2+ excited state of ^{10}Be .

^{11}Be

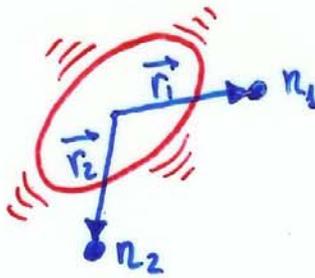
Good agreement between theory and experiment concerning energy and spectroscopic factors

	Exper.	Theory	
		particle-vibration +Argonne	mean field
$E_{s_{1/2}}$	-0.504 MeV	-0.48 MeV	~ 0.14 MeV
$E_{p_{1/2}}$	-0.18 MeV	-0.27 MeV	-3.12 MeV
S[1/2 ⁺]	0.77	0.87	1
S[1/2 ⁻]	0.96	0.96	1

Experimental Spectroscopic Factors from
B. Zwieglinski et al., Nucl.Phys.A315(1979) 124

CORE + 2 neutrons

(2)



COLLECTIVE SURFACE VIBRATIONS

$$R(\hat{\sigma}) = R_0 \left\{ 1 + \sum_{\lambda\mu} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\hat{\sigma}) \right\} \quad ; \quad \lambda = 2, 3, 4, 5$$

$$H_{coll} = \frac{1}{2} \sum_{\lambda\mu} (B_{\lambda} |\alpha_{\lambda\mu}|^2 + C_{\lambda} |\alpha_{\lambda\mu}|^2) \quad ; \quad \hbar\omega_{\lambda} = \hbar \sqrt{\frac{C_{\lambda}}{B_{\lambda}}}$$
$$\beta_{\lambda} = \sqrt{2\lambda+1} \sqrt{\frac{\hbar\omega_{\lambda}}{2C_{\lambda}}}$$

MODEL HAMILTONIAN

$$H = \frac{P_1^2}{2m} + \frac{P_2^2}{2m} + \frac{P_{core}^2}{2M_{core}} + \sum_{nn} V(\vec{r}_1 - \vec{r}_2) + U(\vec{r}_1; \alpha) + U(\vec{r}_2; \alpha) + H_{coll}$$

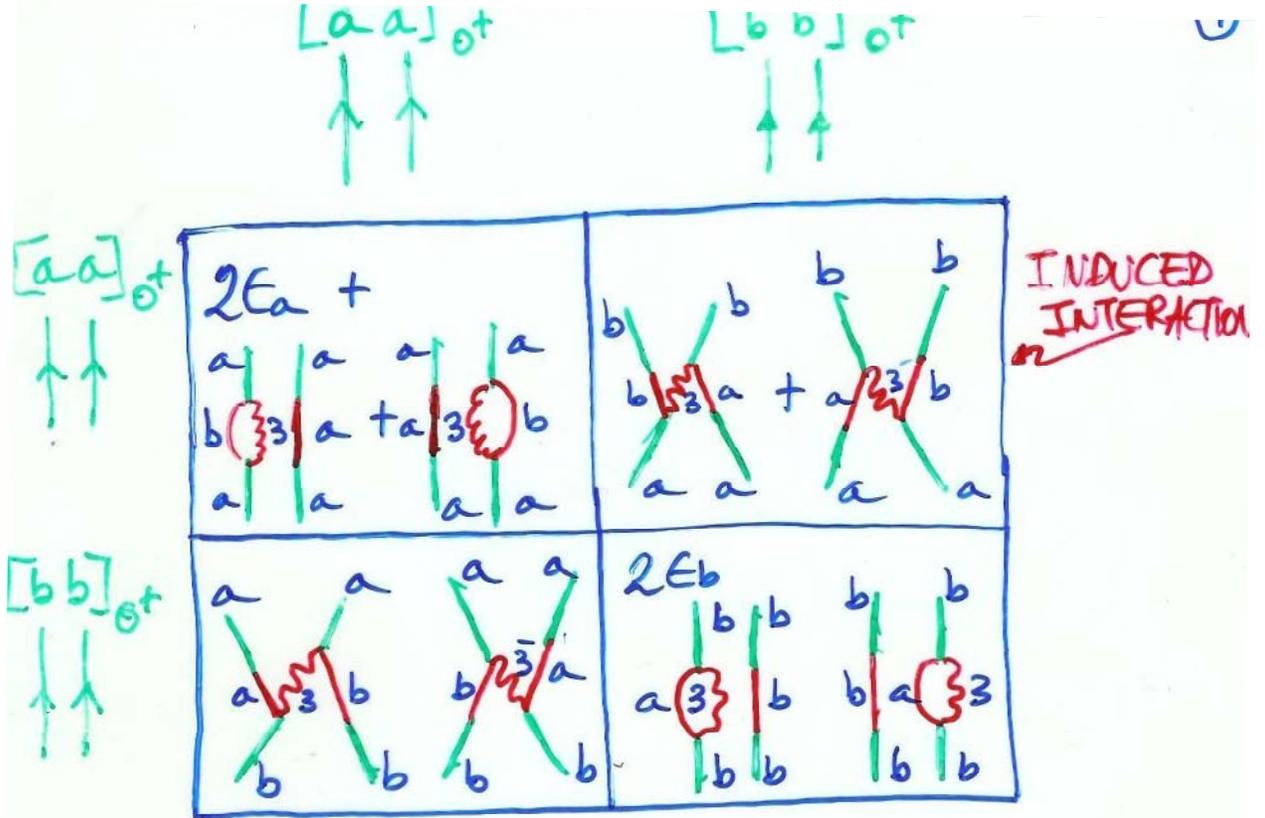
with $\vec{P}_{core} = -\vec{P}_1 - \vec{P}_2$

$$H = \frac{P_1^2}{2\mu} + \frac{P_2^2}{2\mu} + \sum_{nn} V(\vec{r}_1 - \vec{r}_2) + U(\vec{r}_1; \alpha) + U(\vec{r}_2; \alpha) + H_{coll} + \frac{\vec{P}_1 \cdot \vec{P}_2}{M_{core}}$$

where

$$U(\vec{r}; \alpha) = U_0 \left(\frac{r}{1 + \sum_{\lambda\mu} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\hat{\sigma})} \right)$$

$$\cong U_0(r) - \chi r \frac{dU_0}{dr} \sum_{\lambda\mu} \alpha_{\lambda\mu}^* Y_{\lambda\mu}(\hat{\sigma}) \quad ; \quad \chi \approx 1.$$



Bloch-Horowitz perturbation method

> Total Space: $\left\{ \begin{array}{l} \uparrow\uparrow \\ aa \end{array} ; \begin{array}{l} \uparrow\uparrow \\ bb \end{array} ; \begin{array}{l} \uparrow\uparrow \\ b3a \end{array} ; \begin{array}{l} \uparrow\uparrow \\ a3b \end{array} \right\}$

> Model Space: $\left\{ \begin{array}{l} \uparrow\uparrow \\ aa \end{array} ; \begin{array}{l} \uparrow\uparrow \\ bb \end{array} \right\}$

Model Space states must not appear as intermediate states

$$\begin{array}{c} a \\ \diagdown \\ \text{---} \\ \diagup \\ a \end{array} = \frac{\left[\begin{array}{c} a \\ \diagdown \\ \text{---} \\ \diagup \\ b \end{array} + \begin{array}{c} \uparrow \\ \text{---} \\ \uparrow \end{array} \right]}{[E_{gs} - E_{int}]}$$

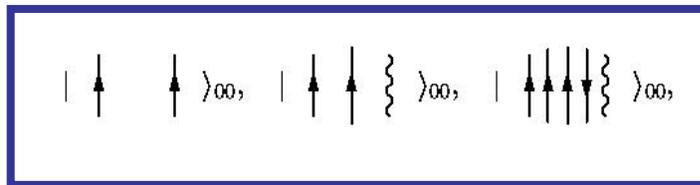
^{12}Be

Fermionic degrees of freedom:

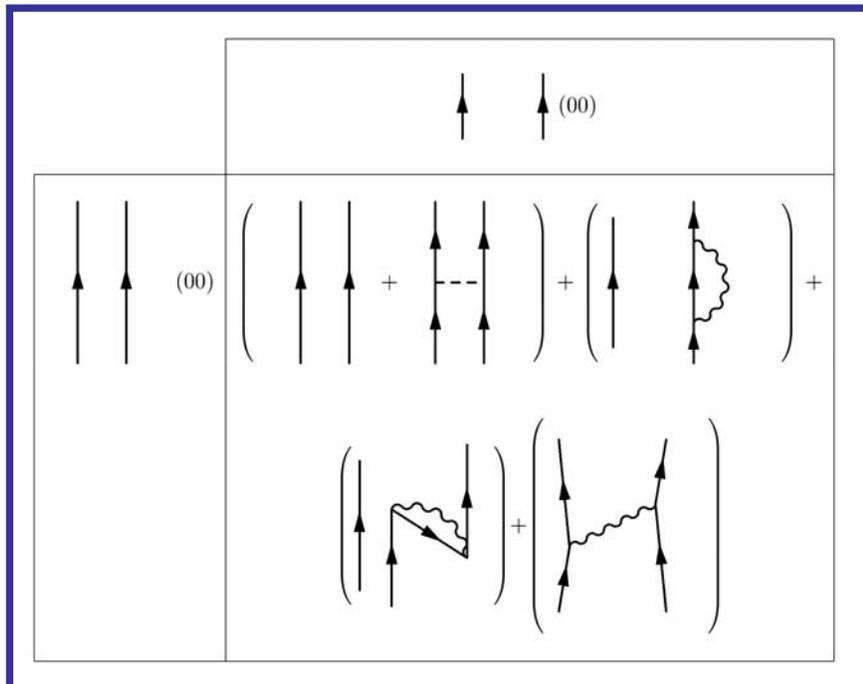
- two particle states coupled to zero angular momentum on $s_{1/2}$, $p_{1/2}$, $d_{5/2}$ Woods-Saxon levels up to 150 MeV

Bosonic degrees of freedom:

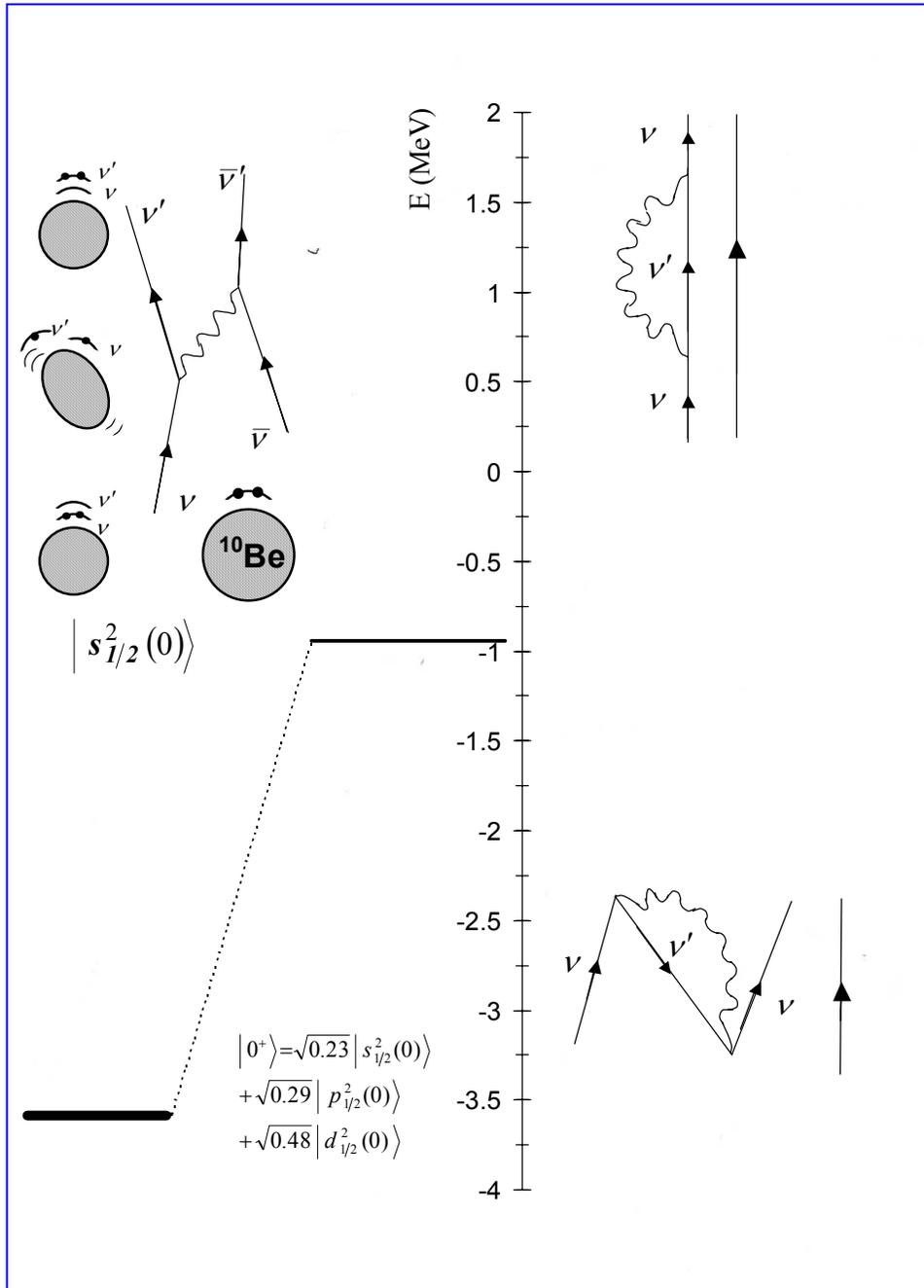
- 1^- , 2^+ and 3^- QRPA solutions up to 50 MeV, associated to a multipole-multipole separable interaction with coupling constant tuned to reproduce $E(1^-)=2.7$ MeV and $B(E1)=0.052$ $e^2\text{fm}^2$ $E(2^+)=2.1$ MeV and $0.6 < \beta_2 < 0.7$



Effective, energy-dependent matrix



The pairing energy between the valence neutrons originates mostly from polarization effects, and not by the nucleon-nucleon bare interaction (Argonne potential)

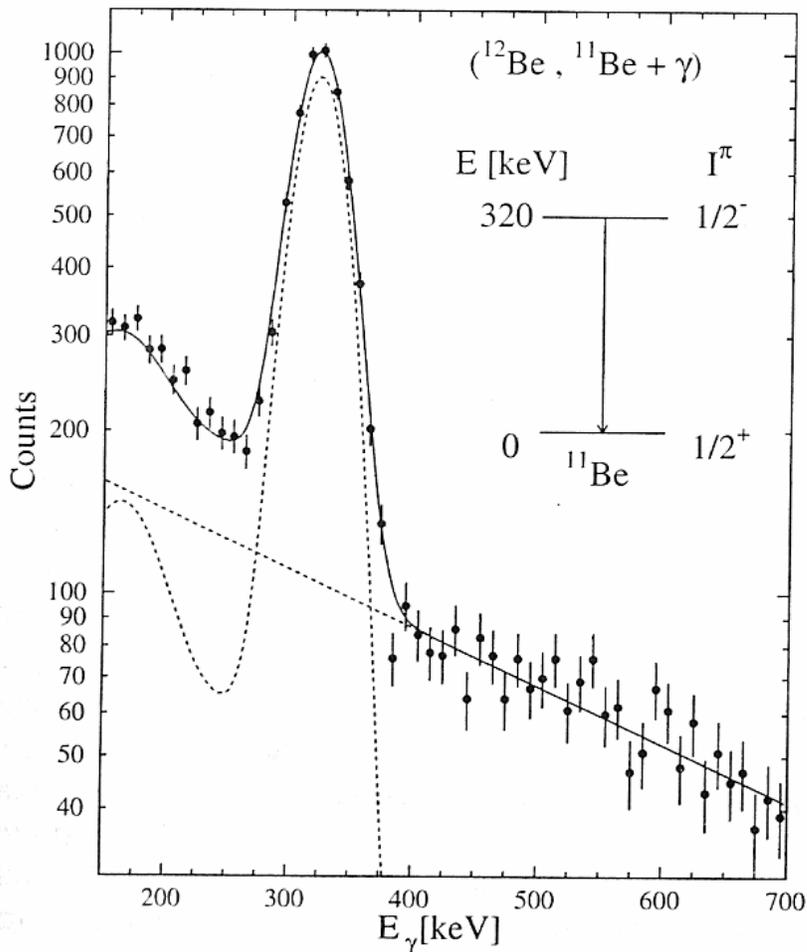


Calc.

Spectroscopic factors from ($^{12}\text{Be}, ^{11}\text{Be} + \gamma$)
reaction to $\frac{1}{2}^+$ and $\frac{1}{2}^-$ final states:

$$S[1/2^-] = 0.42 \pm 0.10 \quad S[1/2^+] = 0.37 \pm 0.10$$

A. Navin et al.,
PRL 85(2000)266



$$T_{1/2} = \sum_{np_{1/2}} \tilde{\xi}_{np_{1/2}} \left\{ \sum_{\substack{p \\ pp'}} \xi_p \xi_{pp'} \times \begin{array}{c} p \\ \uparrow \\ \text{---} \\ \uparrow \\ pp' \end{array} a_{np_{1/2}} + \sum_{\substack{p, \lambda \\ dd'}} \xi_p \xi_{dd'} \times \begin{array}{c} p \\ \uparrow \\ \text{---} \\ \uparrow \\ dd' \end{array} a_{np_{1/2}} \right\}$$

(0.85) (-0.01)

$$+ \sum_{\substack{p'', \lambda \\ n, pp'}} \xi_{p''} \xi_{pp'} \times \begin{array}{c} p'' \\ \uparrow \\ \text{---} \\ \uparrow \\ pp' \end{array} a_{np_{1/2}} + \begin{array}{c} p'' \\ \uparrow \\ \text{---} \\ \uparrow \\ pp' \end{array} a_{np_{1/2}}$$

(0.85) (-0.01)

$$\sum_{\substack{p'', \lambda \\ pp'}} \xi_{p''} \xi_{pp'} \times \left[\begin{array}{c} p'' \\ \uparrow \\ \text{---} \\ \uparrow \\ pp' \end{array} a_{np_{1/2}} \begin{array}{c} p'' \\ \uparrow \\ \text{---} \\ \uparrow \\ pp' \end{array} \lambda 2^+ + \begin{array}{c} p'' \\ \uparrow \\ \text{---} \\ \uparrow \\ pp' \end{array} a_{np_{1/2}} \begin{array}{c} p'' \\ \uparrow \\ \text{---} \\ \uparrow \\ pp' \end{array} \lambda 2^+ \right]$$

(0.01) (-1.61)

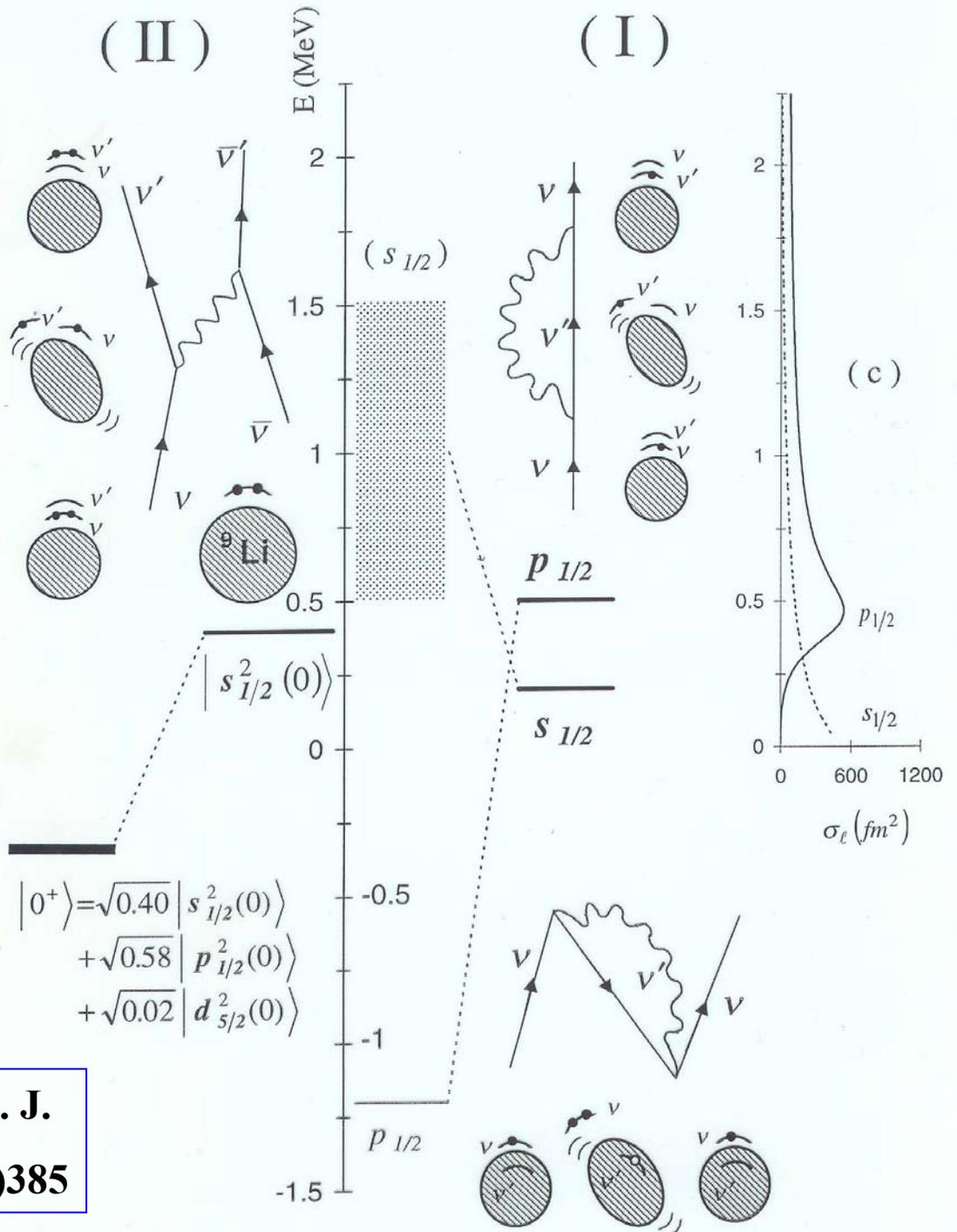
$$\xi_p = \tilde{\xi}_p / \sqrt{N(^{11}\text{Be})},$$

$$\xi_{ii'} = \tilde{\xi}_{ii'} / \sqrt{N(^{12}\text{Be})},$$

ξ_i are obtained diagonalizing the energy-dependent matrix

Particle-vibration coupling

in ^{10}Li and ^{11}Li



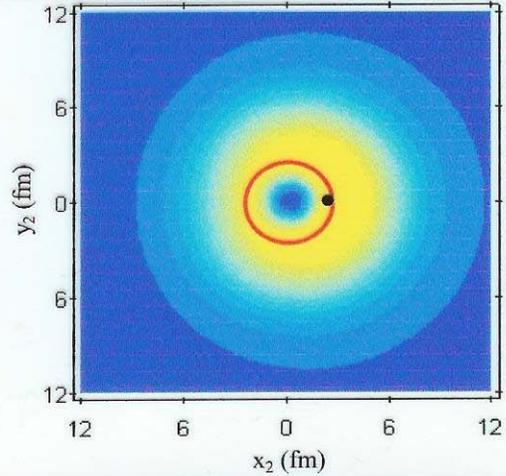
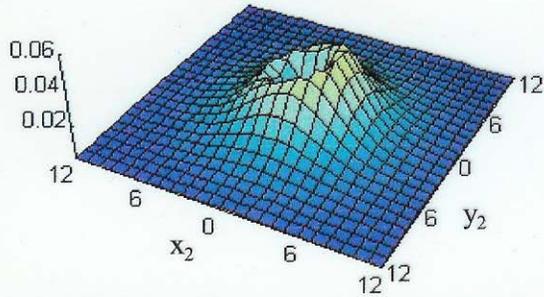
Eur. Phys. J.
A11(2001)385

Comparison with experiment

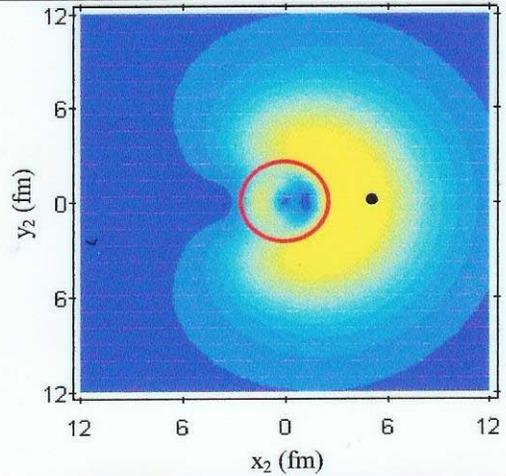
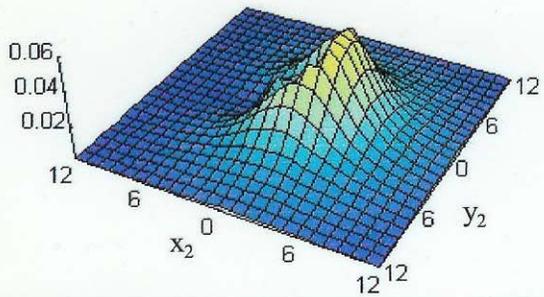
		Exper.	Theory	
			particle-vibration +Argonne	mean field
$^{10}_3\text{Li}_7$ (not bound)	s	0.1 – 0.2 MeV	0.2 MeV (virtual)	≈ 1 MeV (virtual)
	p	0.5 – 0.6 MeV	0.5 MeV (res.)	-1.2 MeV (bound)
$^{11}_3\text{Li}_8$ (bound)	S_{2n}	0.294 ± 0.03 MeV	0.33 MeV	2.4 MeV
	s^2, p^2	50 % , 50 %	41% , 59 %	0% , 100%
	$\langle r^2 \rangle^{1/2}$	3.55 ± 0.1 fm	3.9 fm	
	σ_{\perp}	$48 \pm 10 \frac{\text{MeV}}{c}$	$55 \frac{\text{MeV}}{c}$	

Spatial correlations between the two halo neutrons

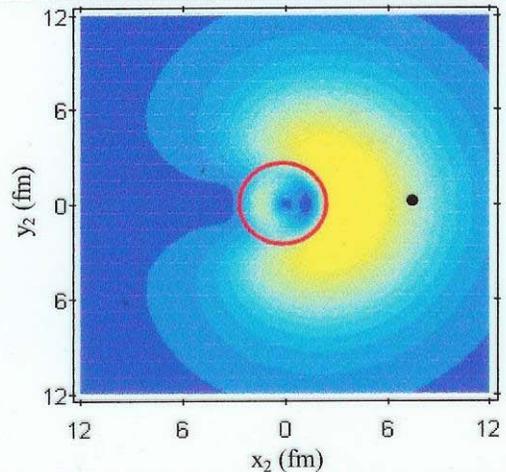
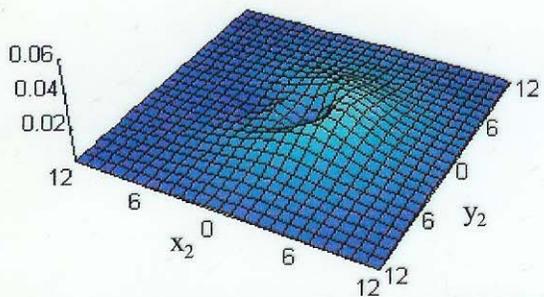
$r_1 = 2,5$ fm



$r_1 = 5$ fm



$r_1 = 7,5$ fm



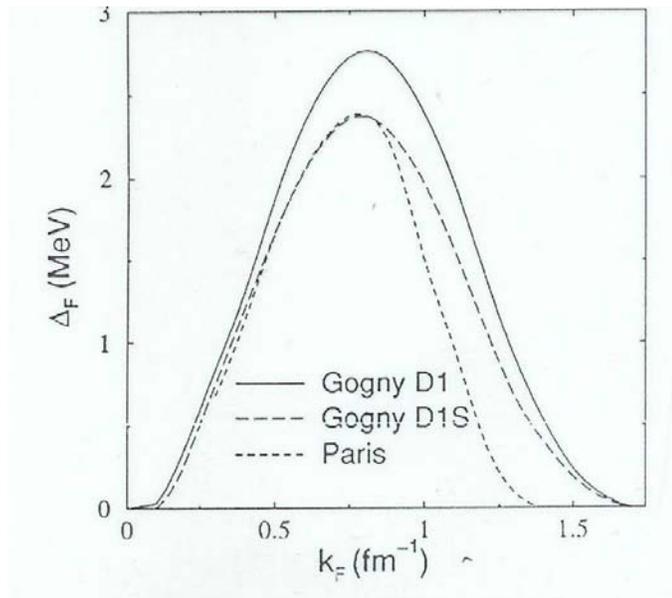
ADVANTAGES OF THE MODEL:

- Standard mean-field potential, without adjustments of the spin-orbit force or l -dependent terms; the same parametrization for Li and Be isotopes
- Coupling with continuum states is taken into account
- Bare interaction between the valence neutrons, without ad-hoc density dependent terms
- Limited amount of phenomenological input: strength of low-lying vibrations
- Consistent treatment of the Pauli principle (Nuclear Field Theory)

- SOME LIMITATIONS OF THE MODEL :

- One-phonon configurations
- Harmonic vibrations of the core
- Tamm-Dancoff treatment of pairing vibrations

Pairing gaps in uniform matter calculated with effective and bare interactions look similar...



However, in ¹²⁰Sn Argonne potential reproduces experiment only taking into account renormalization effects

