

# SHORT-RANGE CORRELATION

from

$^{12}\text{C}(\text{p}, 2\text{p} + \text{n})$  and  $^{12}\text{C}(\text{e}, \text{e}'\text{p} + \text{N})$

John W. Watson  
Kent State University

and the  
EVA Collaboration

**Trento Workshop March 2004**

# Experiment E850

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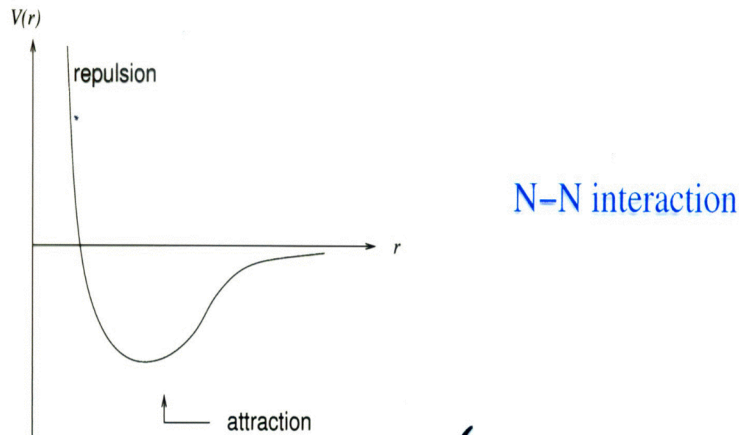
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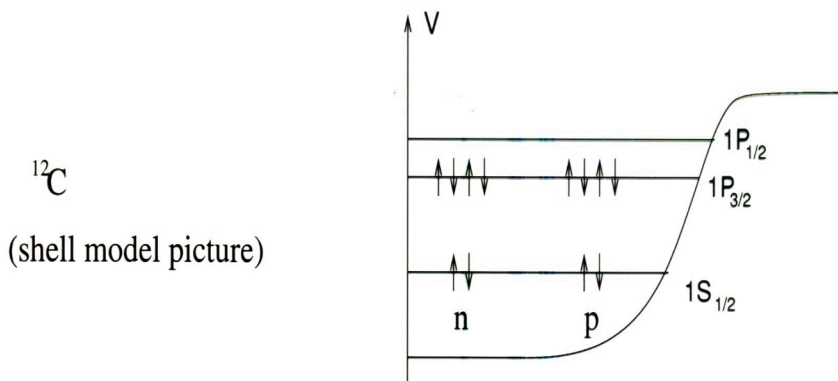


# The N-N Interaction, the Shell Model and



Nuclear Shell Model ( $\sim 1950$ ) { Maria Mayer  
J.H.D. Jensen  
Nobel Prize in 19

The attractive part of the N-N interaction in combination with the Pauli principle produces an average attractive potential with well-defined quantum states.



Short-range repulsion  $\rightarrow$  saturation of nuclear densities,  $\rho$ . However, the short-range repulsive part must also manifest itself in the wavefunctions of nucleons in the nucleus. Because it is of short range, high-momentum components will be affected. Typical

## Nuclear Fermi Momenta from Quasielastic Electron Scattering

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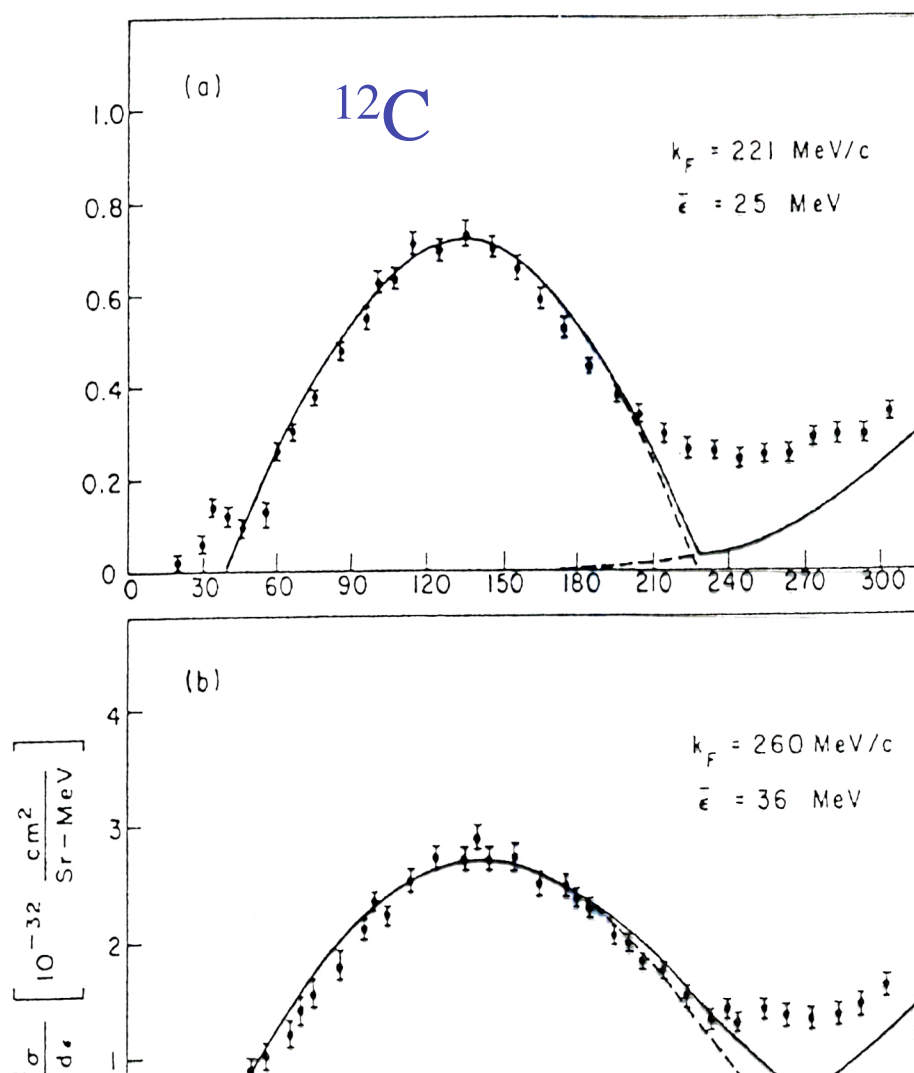
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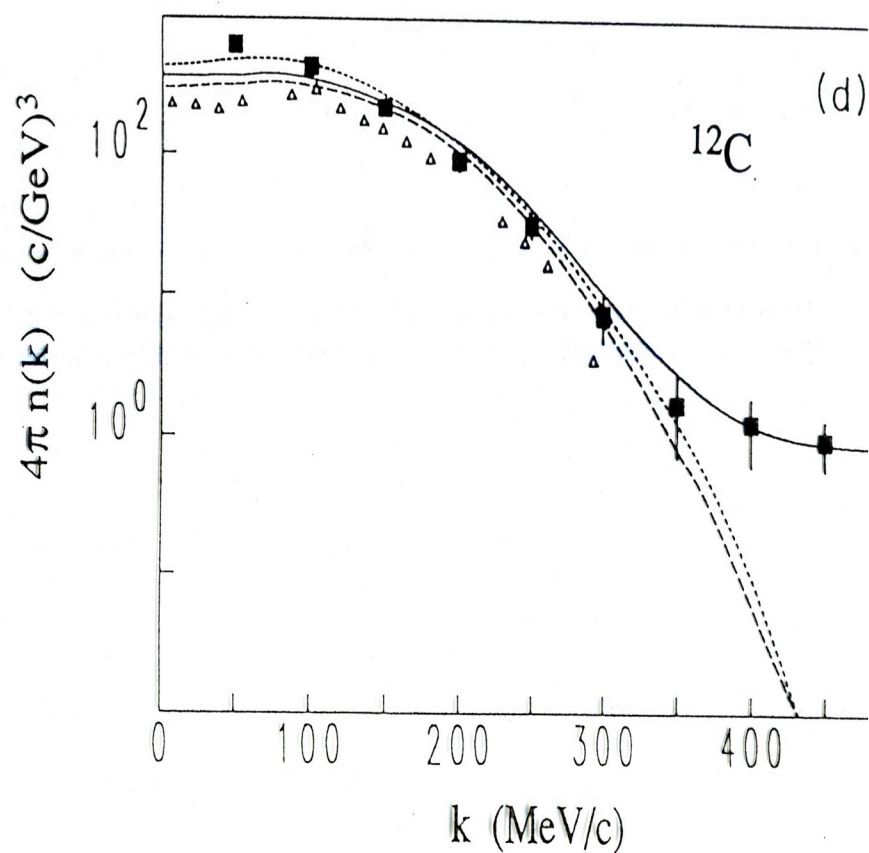
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(Received 12 January 1971)

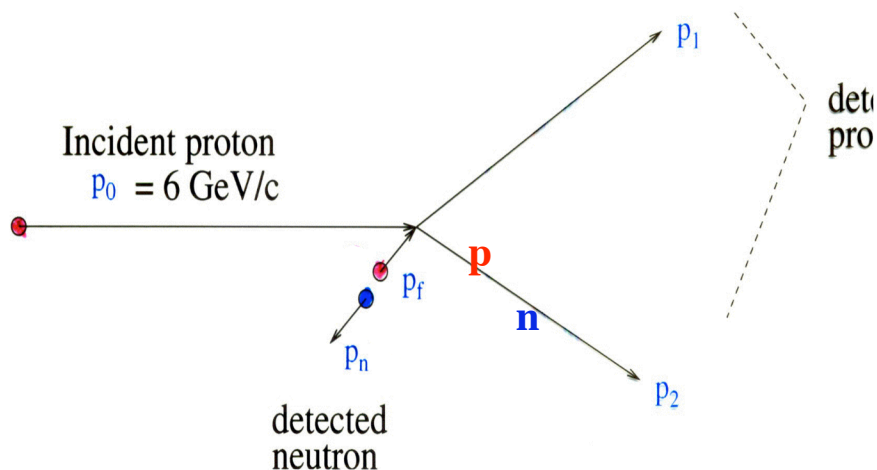


ing analysis of quasielastic electron scattering and nucleon momen  
in few-body systems, complex nuclei, and nuclear matter

C. Ciofi degli Atti,<sup>(1,2)</sup> E. Pace,<sup>(1,3)</sup> and G. Salmè<sup>(1)</sup>



For quasi-elastic reaction, we can apply impulse approximation (IA) to the interaction of the proton and the one active target nucleon:



We reconstruct the momentum  $\vec{p}_f$  of the struck proton:

$$\vec{p}_f = \vec{p}_1 + \vec{p}_2 - \vec{p}_0$$

We then ask is there a neutron in coincidence, a

$\vec{p}_n$  and  $\vec{p}_f$  “Correlated”

i.e. roughly *equal* and *opposite*?

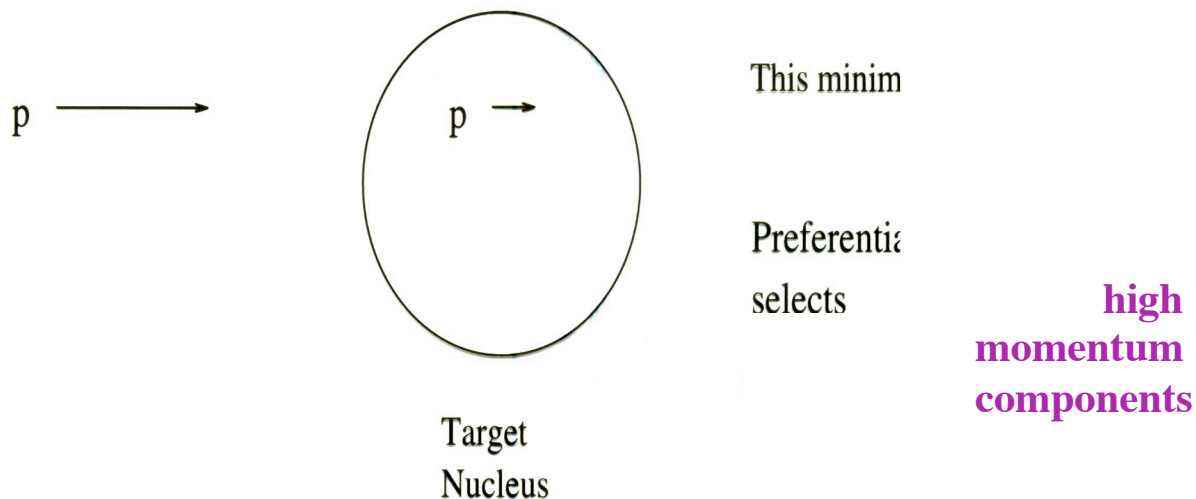
For energies of several GeV and up,  
 For p-p elastic scattering near  $90^\circ$  c.m.,

$$\frac{d\sigma}{dt} \sim s^{-(n_1+n_2+n_3+n_4-2)}$$

$$\sim s^{-10}$$

where the Mandelstam variable  $s = (P_0 + P_F)^2$   
 square of the total c.m. energy.

So for quasi-elastic p-p scattering near  $90^\circ$  c.m.  
 have a very strong preference for reacting with  
 protons with their Fermi motion in the beam dir



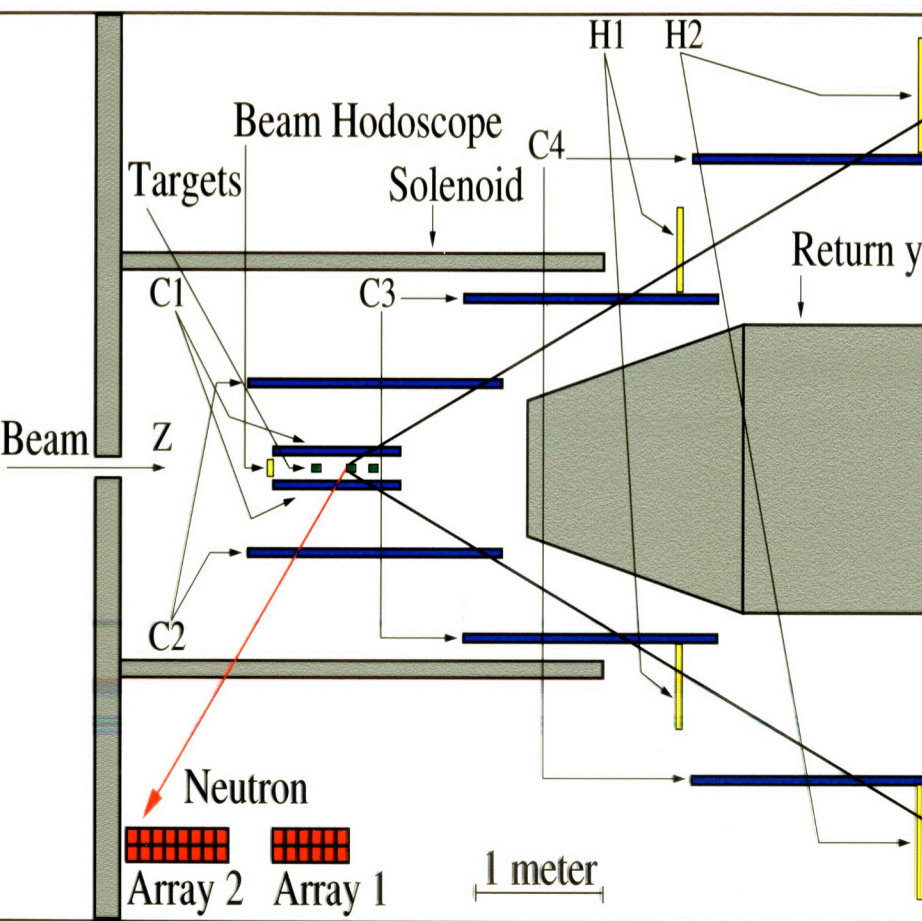
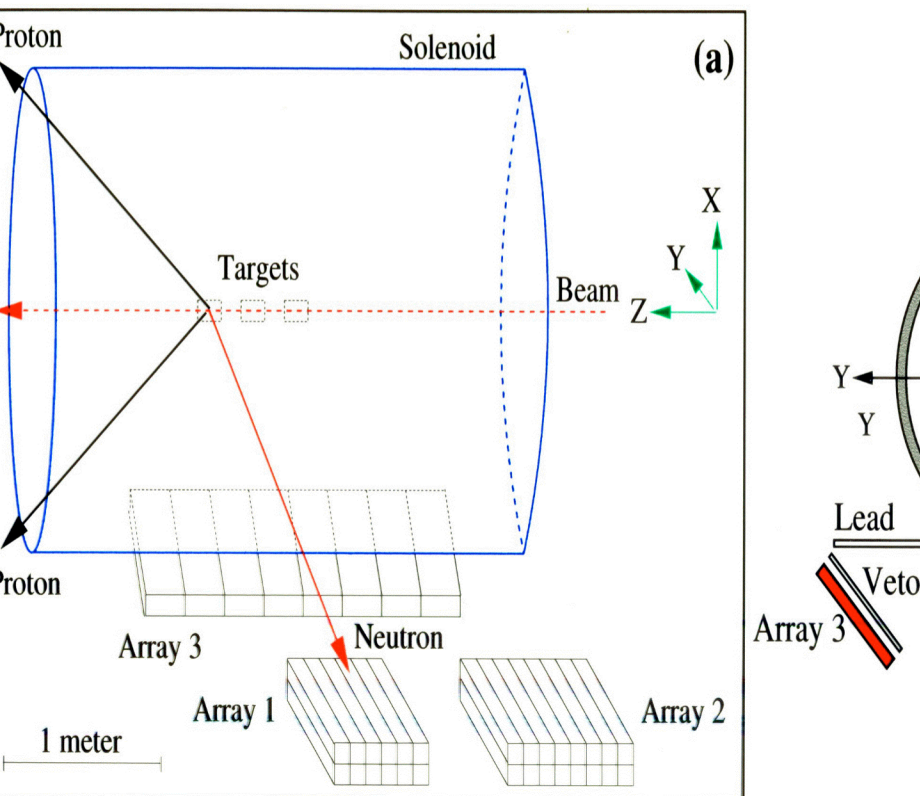


Figure 1: A schematic side view of the EVA spectron





Array 1: total area  $0.6 \times 1.0 \text{ m}^2$ , 12 counters, 2 layers 0.125

Array 2: total area  $0.8 \times 1.0 \text{ m}^2$ , 16 counters, 2 layers 0.125

Array 3: total area  $2 \times 1.0 \text{ m}^2$ , 8 counters, 1 layers 0.1 n

Figure 5: A schematic side view (a) and a head-on view (b) of the detector and the neutron counter arrays.

## Bunch Formation:

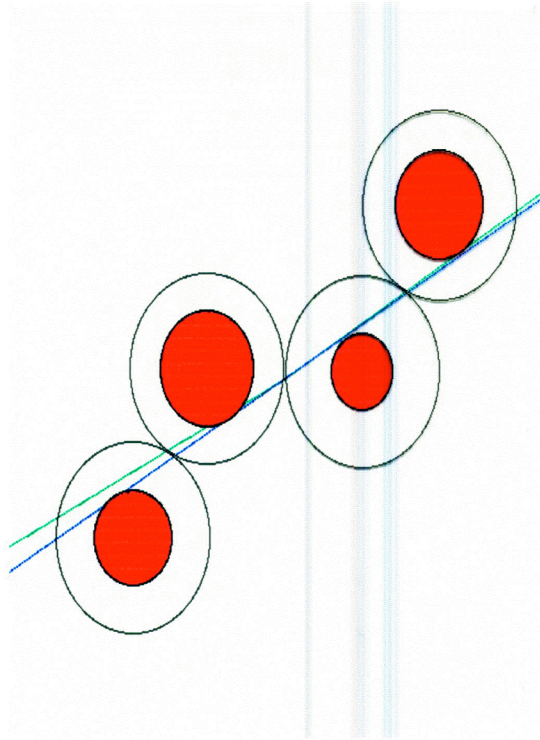


Figure 11: An example of a straw-tube bunch. The outer circles represent the walls of the tube. The radius of the inner circles is the drift distance. The blue line is the local derivative to a trajectory and the green line is the global particle trajectory.

## Track Fit:

$$y(x) = bx + cx^2$$



## Quasi-elastic analysis:

### ➔ Track Reconstruction:

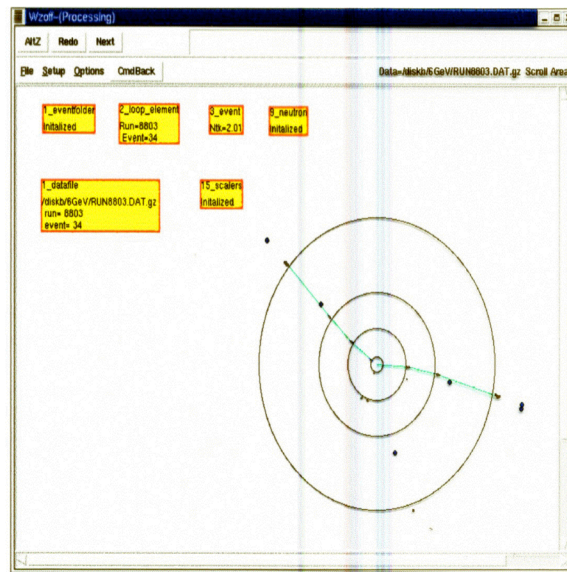
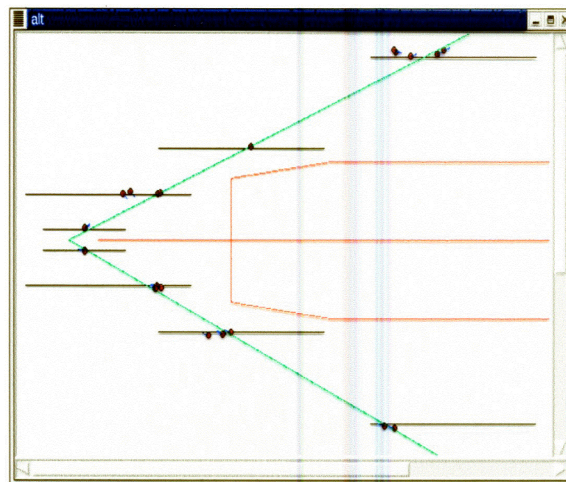


Figure 9: *wzoft* event display in transverse plane.



## ➡ Calculation of Kinematic Variables:

### *z*-coordinate of The Vertex:

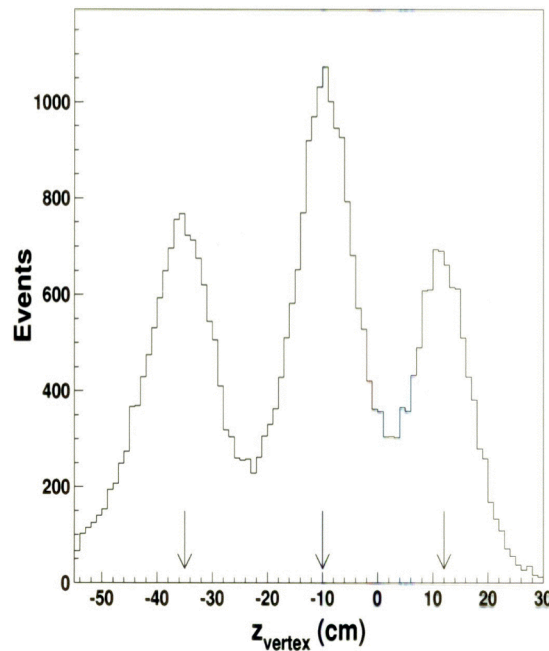


Figure 12: Distribution of  $z_{vertex}$  for reconstructed  $e\nu$  at 5.9 GeV/c beam momentum. The length of each target is 10 cm and the arrows show the three target central positions.

Cuts to identifying the targets:

$$dz < 15 \text{ cm}$$

$$-45 < z_{vertex} < -25 \longrightarrow \text{target at } -35 \text{ cm}$$

$$-20 < z_{vertex} < 0 \longrightarrow \text{target at } -10 \text{ cm}$$

## Polar Angle and Azimuthal Angle:

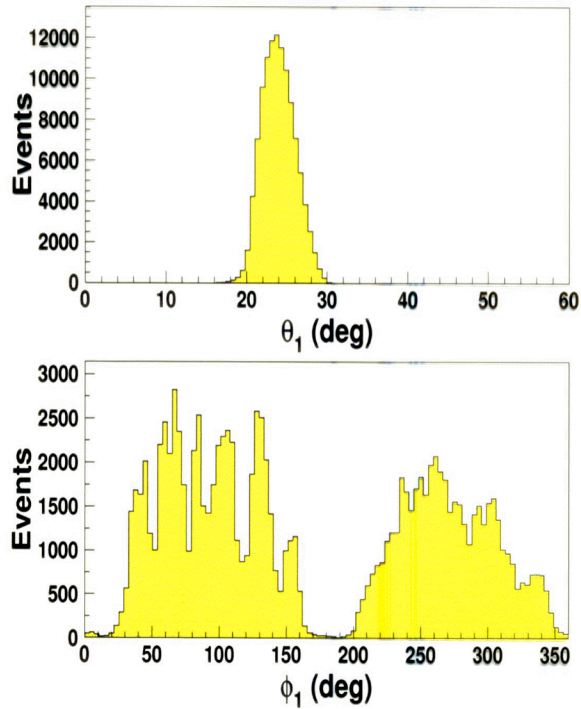


Figure 13: Distributions of the polar angle  $\theta_1$  and the azimuthal angle  $\phi_1$  (for the smaller-angle proton) for  $^{12}\text{C}$  events at 5.9 GeV/c beam momentum.

## Transverse Momentum:

The transverse momentum of an outgoing proton was calculated from the radius of the curvature of its track:

## ➡ Calculation of Physical Quantities:

### Missing Energy:

$$E_{miss} = E_0 + m - E_1 - E_2$$

where  $E_0$  is the beam energy,  $m$  is the mass proton,  $E_1$  and  $E_2$  are the energies of the two outgoing protons.

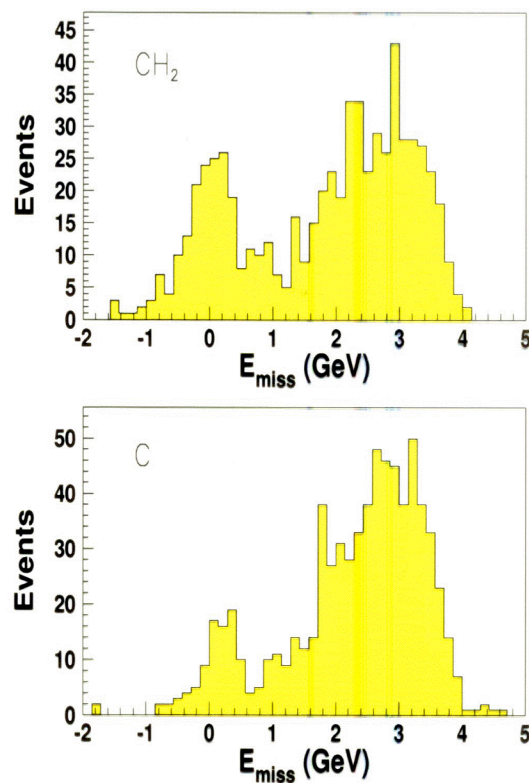


Figure 14: Missing energy spectra for (p,2p) events a

## Measurement of quasi-elastic $^{12}\text{C}(p,2p)$ scattering at high momentum transfer

Y. Mardor <sup>a</sup>, J. Aclander <sup>a</sup>, J. Alster <sup>a</sup>, D. Barton <sup>b</sup>, G. Bunce <sup>b</sup>, A. Carro <sup>c</sup>, N. Christensen <sup>c,1</sup>, H. Courant <sup>c</sup>, S. Durrant <sup>a,b</sup>, S. Gushue <sup>b</sup>, S. Heppelmaier <sup>c</sup>, E. Kosonovsky <sup>a</sup>, I. Mardor <sup>a</sup>, M. Marshak <sup>c</sup>, Y. Makdisi <sup>b</sup>, E.D. Minor <sup>c</sup>, I. Navon <sup>a</sup>, H. Nicholson <sup>c</sup>, E. Piasetzky <sup>a</sup>, T. Roser <sup>b</sup>, J. Russell <sup>f</sup>, C.S. Stenlund <sup>c</sup>, M. Tanaka <sup>b,3</sup>, C. White <sup>c</sup>, J-Y Wu <sup>d,4</sup>

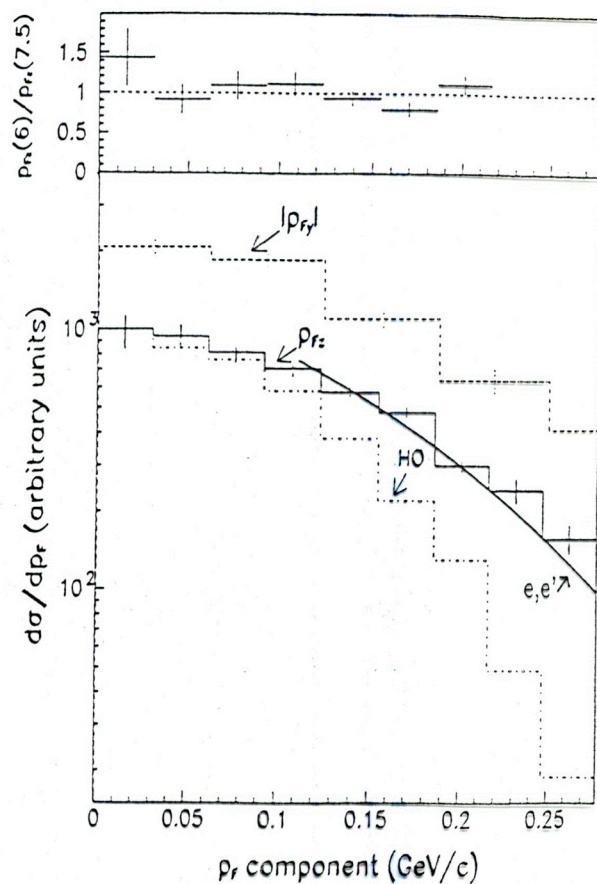
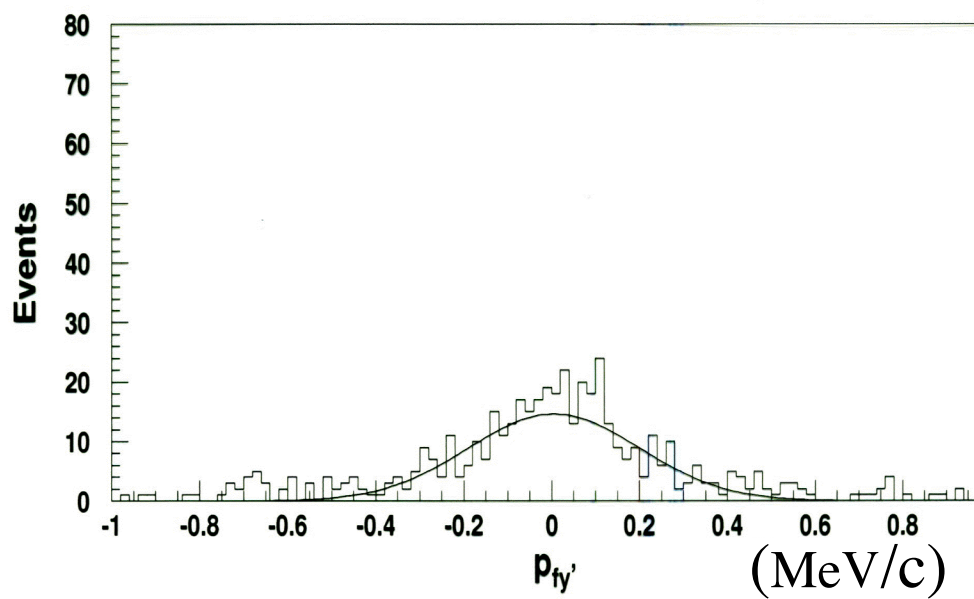
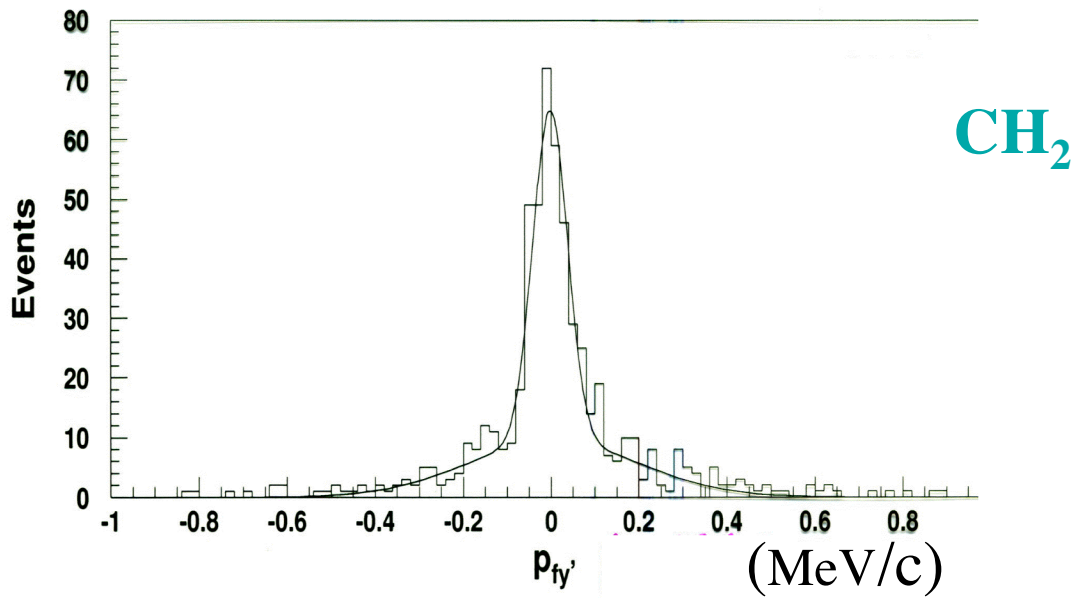


Fig. 3. The upper part of the figure shows the ratio of the two distributions measured at 6 and 7.5 GeV/c (the last two highest momentum points were measured at 6 GeV/c only).  $p_{Fz}$  is the longitudinal ground state momentum distribution obtained from





## Light Cone Description of the (p,2p+n) Reaction

The momentum of a nucleon is described in light space by  $(p_t, \alpha)$ , where  $p_t$  is the transverse momentum and  $\alpha$  defined as:

$$\alpha = \frac{E - p_z}{m}$$

represents the fraction of the nuclear momentum carried by the target nucleon in the light-cone reference frame.

➡ Mandelstam variable  $s$ :

$$\begin{aligned} s &= (P_0 + P_F)^2 \\ &= m^2 + m_1^2 + 2P_0 P_F \\ &= m^2 + m_1^2 + (E_0 - P_0)(E_F + p_F^z) + \alpha m(P_0 + P_F) \\ &\sim m^2 + m_1^2 + 2\alpha m p_0 \end{aligned}$$

where  $\alpha = \frac{E_F - p_F^z}{m}$  is the light cone variable for the target nucleon and for large incident momenta,

## Longitudinal Fermi Momentum and $\alpha$ :

From the momentum conservation:

$$p_{fz} = \frac{p_{t1}}{\tan\theta_1} + \frac{p_{t2}}{\tan\theta_2} - p_0$$

From light cone variable  $\alpha$ :

$$\alpha = \frac{E_f - p_{fz}}{m} \sim 1 - \frac{p_{fz}}{m}$$

$$p_{fz} = m \cdot (1 - \alpha).$$

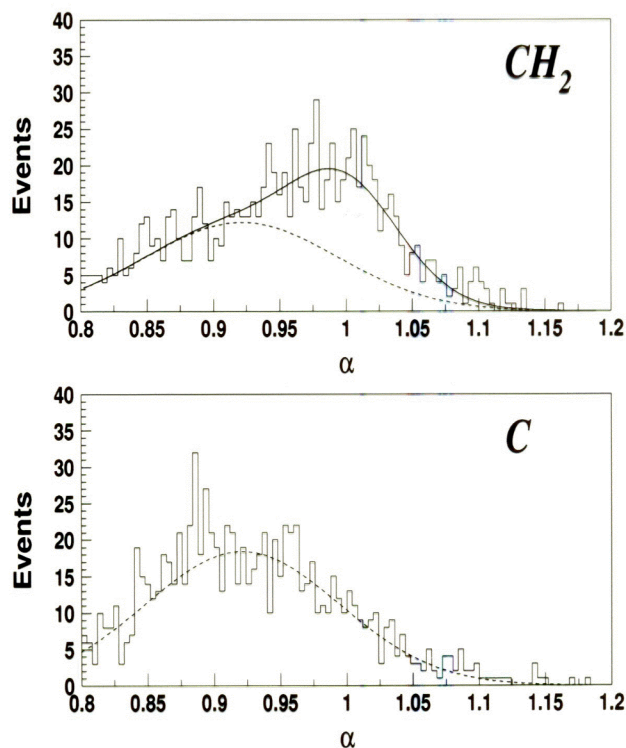


Figure 16: Light cone variable  $\alpha$  distribution for  $CH_2$  and  $C$ .



## Neutron Analysis:

➡ Inverse Velocity:

$$v^{-1} = \frac{TOF}{l} = \frac{TOF}{\sqrt{x_{hit}^2 + y_{hit}^2 + (z_{hit} - z_{target})^2}}$$

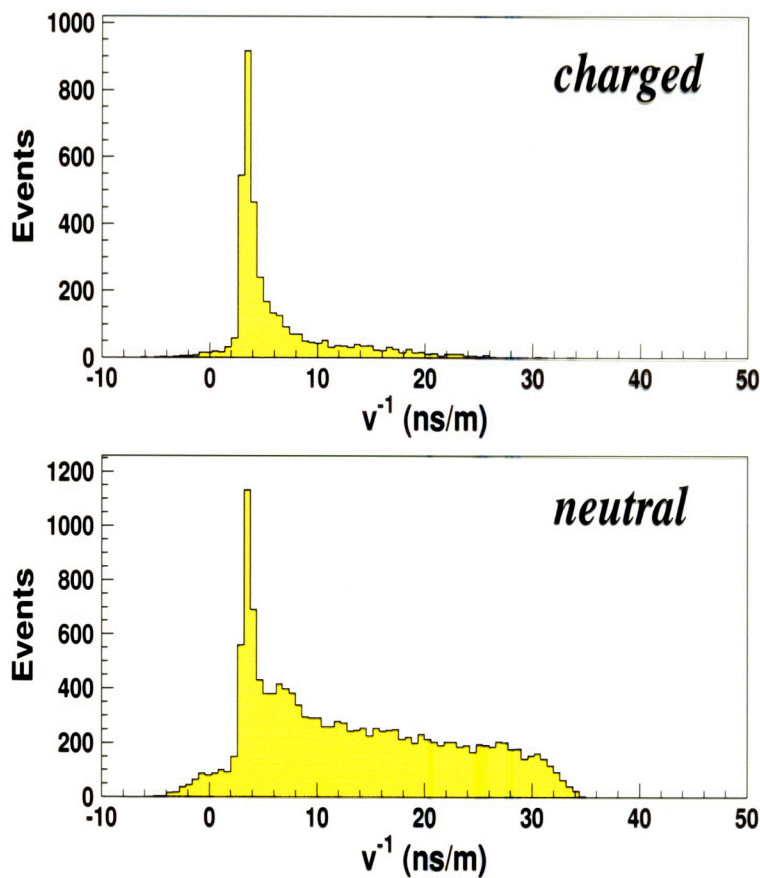


Figure 17: Inverse velocity spectra for charged and ne

# Results and Conclusions

## List of Cuts Applied For Triple Coincident Events

### Cuts on protons:

Čerenkov cut: select protons

Number of tracks: 2 tracks

Target Positions:  $|z_{target} + 10| < 10$

$$|z_{target} + 35| < 10$$

$$|z_1 - z_2| < 12$$

Missing Energy:  $|E_{miss} - 0.32| < 0.5$  GeV

$\phi$  (for arrays 1 and 2):  $45^\circ < \phi_1 < 135^\circ$ , or

$$225^\circ < \phi_1 < 315^\circ$$

$\phi$  (for array 3):  $0^\circ < \phi_1 < 90^\circ$ , or

$$180^\circ < \phi_1 < 270^\circ$$

### Cuts on neutrons:

## Identification of Correlated Events

### One-Dimensional Correlations:

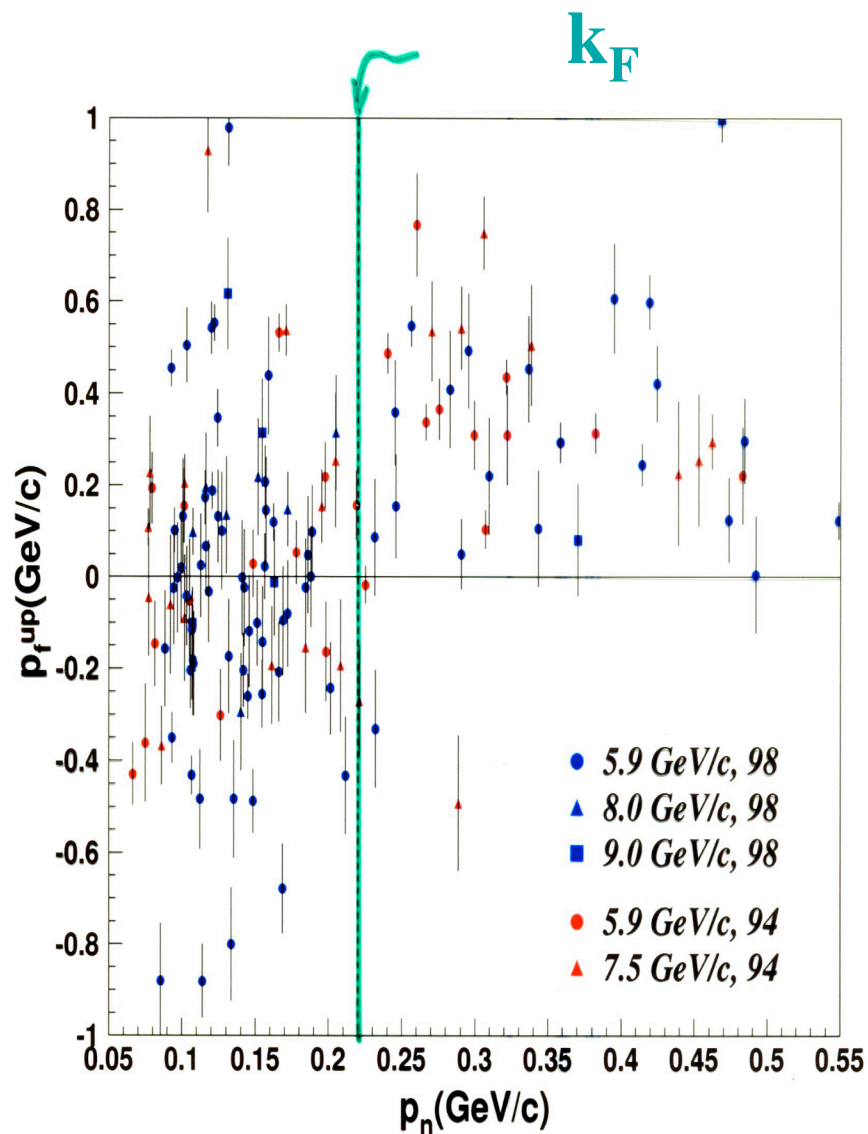
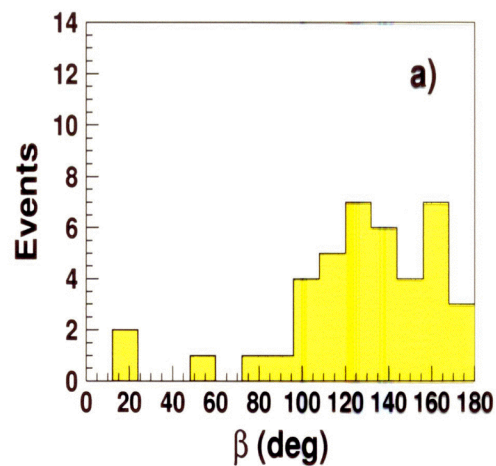


Figure 19:  $p_f^{up}$  vs.  $p_n$  for  $^{12}\text{C}(p,2p+n)$  events. Data lab "98" (solid symbols) are for 98 runs (this experiment). labelled "94" are from Aclander, et al. The vertical line at

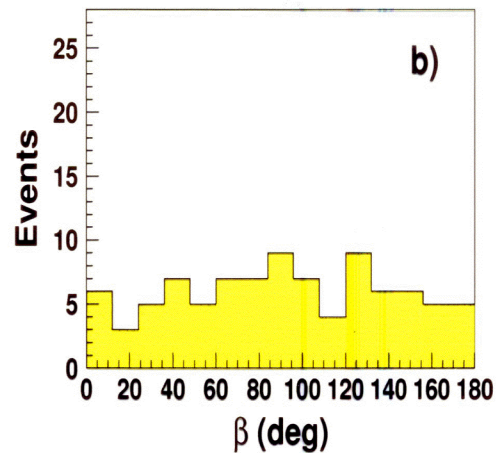
## Transverse Correlations:

The angle between the transverse momenta of proton and neutron is defined as:

$$\beta = \cos^{-1} \left( \frac{\vec{p}_{nt} \cdot \vec{p}_{ft}}{|\vec{p}_{nt}| |\vec{p}_{ft}|} \right).$$



$$p_n > k_F$$



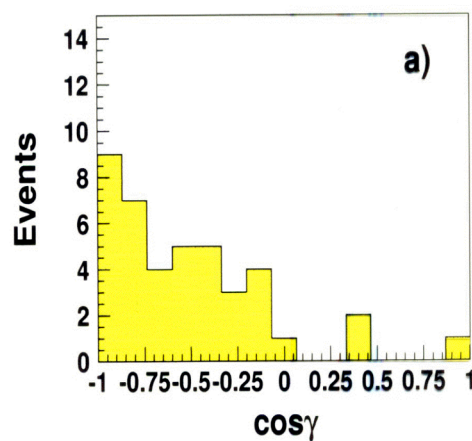
$$p_n < k_F$$

Figure 20: Plots of  $\beta$ , the angle in the transverse plane between  $\vec{p}_f$  and  $\vec{p}_n$ . Panel (a) is for events with  $p_n > 0.22$  GeV

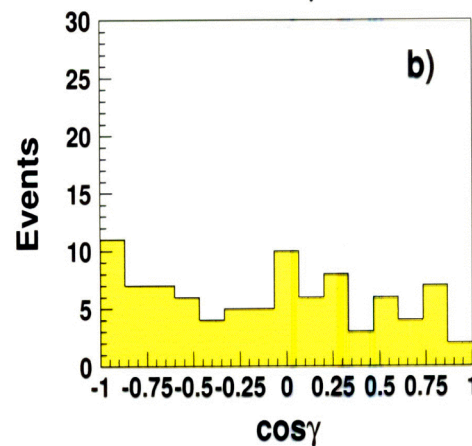
## Full Correlations:

We then construct the directional correlation between  $\vec{p}_f$  and  $\vec{p}_n$  as

$$\cos\gamma = \frac{\vec{p}_f \cdot \vec{p}_n}{|\vec{p}_f| |\vec{p}_n|}$$



$p_n > k_F$



$p_n < k_F$

Figure 21: Plots of  $\cos\gamma$ , where  $\gamma$  is the angle between  $\vec{p}_f$  and  $\vec{p}_n$ . Panel (a) is for events with  $p_n > 0.22 \text{ GeV}/c$

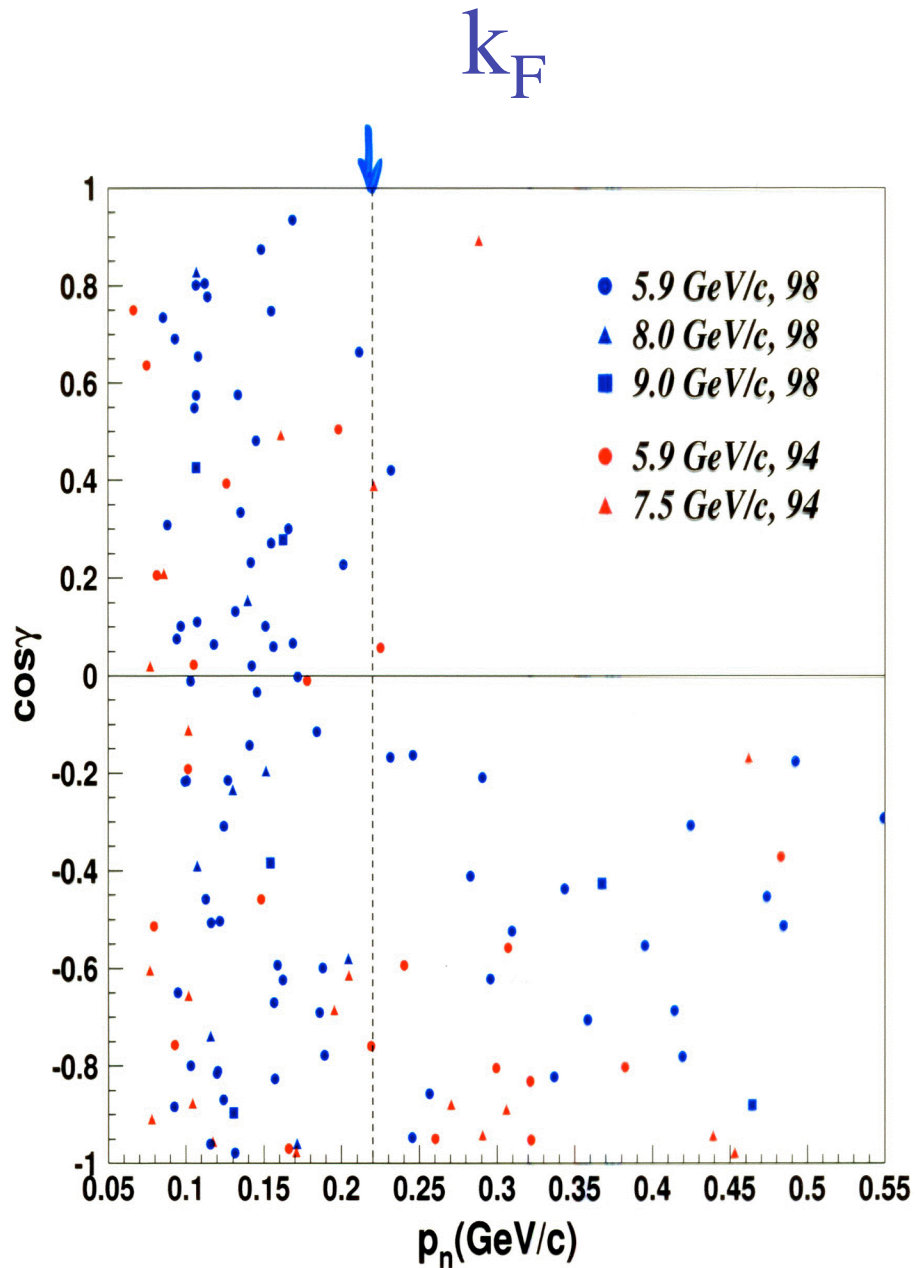


Figure 22:  $\cos \gamma$  vs.  $p_n$  for  $^{12}\text{C}(p,2p+n)$  events. The vertical line at 0.22 GeV/c corresponds to  $k_F$ , the Fermi momentum of  $^{12}\text{C}$ .



## The Correlated Fraction of (p,2p) Events:

For the 6 GeV 1998 data set we estimated the fraction of (p,2p) events with  $p_f > 0.22$  GeV which have a correlated backwards neutrons with  $p_n > 0.22$  GeV/c.

$$F = \frac{\text{corrected \# of (p,2p+n) events}}{\text{\# of (p,2p) events}} = \frac{A}{B}$$

The quantity A was obtained from the sample of all 18 (p,2p+n) events with  $p_n \geq k_F = 0.12$  GeV/c, where a correction for flux attenuation detection efficiency was applied event-by-event and then corrected for the solid-angle coverage

$$A = \frac{2\pi}{\Delta\Omega} \sum_{i=1}^{18} \frac{1}{\epsilon_i} \cdot \frac{1}{t_i} = 1090.$$

The average value of  $(1/\epsilon_i t_i)$  was  $8.2 \pm 0.82$  at  $2\pi/\Delta\Omega = 7.42$ . We can then calculate

$$F = \frac{A}{B} = \frac{1090}{2180} = 0.49 \pm 0.13.$$

➡ The Center of Mass Motion of the  $n - p$  Pa

$$p_z^{cm} = p_{nz} + p_{fz}$$

We can express this in terms of  $\alpha$  as

$$\begin{aligned}\alpha_p + \alpha_n &= \frac{E_f - p_p^z}{m} + \frac{E_f - p_n^z}{m} \\ &= \left(1 - \frac{p_{fz}}{m}\right) + \left(1 - \frac{p_{nz}}{m}\right)\end{aligned}$$



$$p_z^{cm} = 2m\left(1 - \frac{\alpha_p + \alpha_n}{2}\right)$$

➡ The Relative Motion of the Correlated Nucl

$$\begin{aligned}\alpha_p - \alpha_n &= \left(1 - \frac{p_{fz}}{m}\right) - \left(1 - \frac{p_{nz}}{m}\right) \\ &= \left(\frac{p_{nz} - p_{fz}}{m}\right)\end{aligned}$$



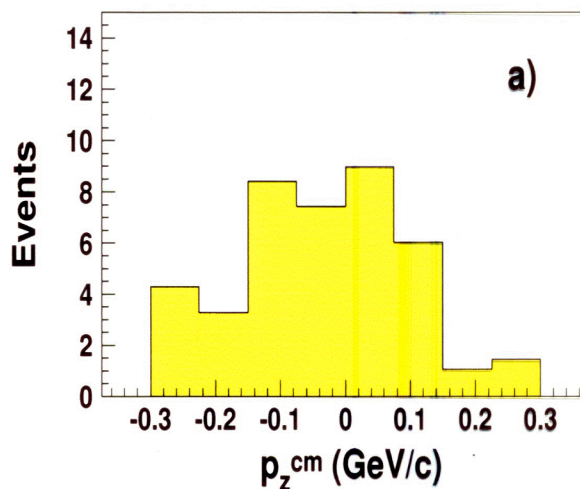
$$p_z^{rel} = |p_{fz} - p_{nz}|$$



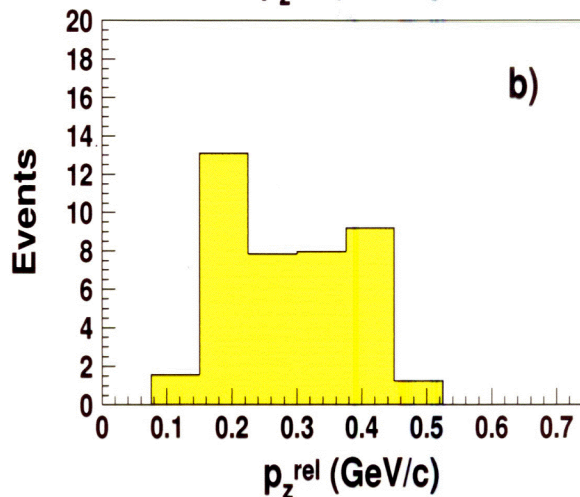
## The Relative and c.m. Motion of Correlated Pairs:

$$p_z^{cm} = 2m\left(1 - \frac{\alpha_p + \alpha_n}{2}\right),$$

$$p_z^{rel} = m|\alpha_p - \alpha_n|.$$



$$\begin{aligned}\text{Centroid} &= -0.013 \pm 0.02 \\ \sigma &= 0.143 \pm 0.01\end{aligned}$$



$$\begin{aligned}\text{Centroid} &= 0.289 \pm 0.01 \\ \sigma &= 0.097 \pm 0.00\end{aligned}$$

Figure 23: Plots of (a)  $p_z^{cm}$  and (b)  $p_z^{rel}$  for correlated pairs.

## Summary

1. For quasielastic (p,2p) events we reconstructed  $\vec{p}_f$  the momentum of the knocked-out proton before the reaction;  $\vec{p}_f$  was then compared with  $\vec{p}_n$ , measured, coincident neutron momentum. For  $|\vec{p}_n| > k_F = 0.220 \text{ GeV}/c$  (the Fermi momentum) a strong back-to-back directional correlation between  $\vec{p}_f$  and  $\vec{p}_n$  was observed, indicative of short-range n-p correlations.

2. We determined that  $49 \pm 13 \%$  of events with  $|\vec{p}_f| > k_F$  had directionally correlated neutrons with  $|\vec{p}_n| > k_F$ . Thus 2N SRCs are a major source of high-momentum nucleons in nuclei.

3. We also measured the c.m. and relative momenta of correlated n-p pairs in the longitudinal direction.

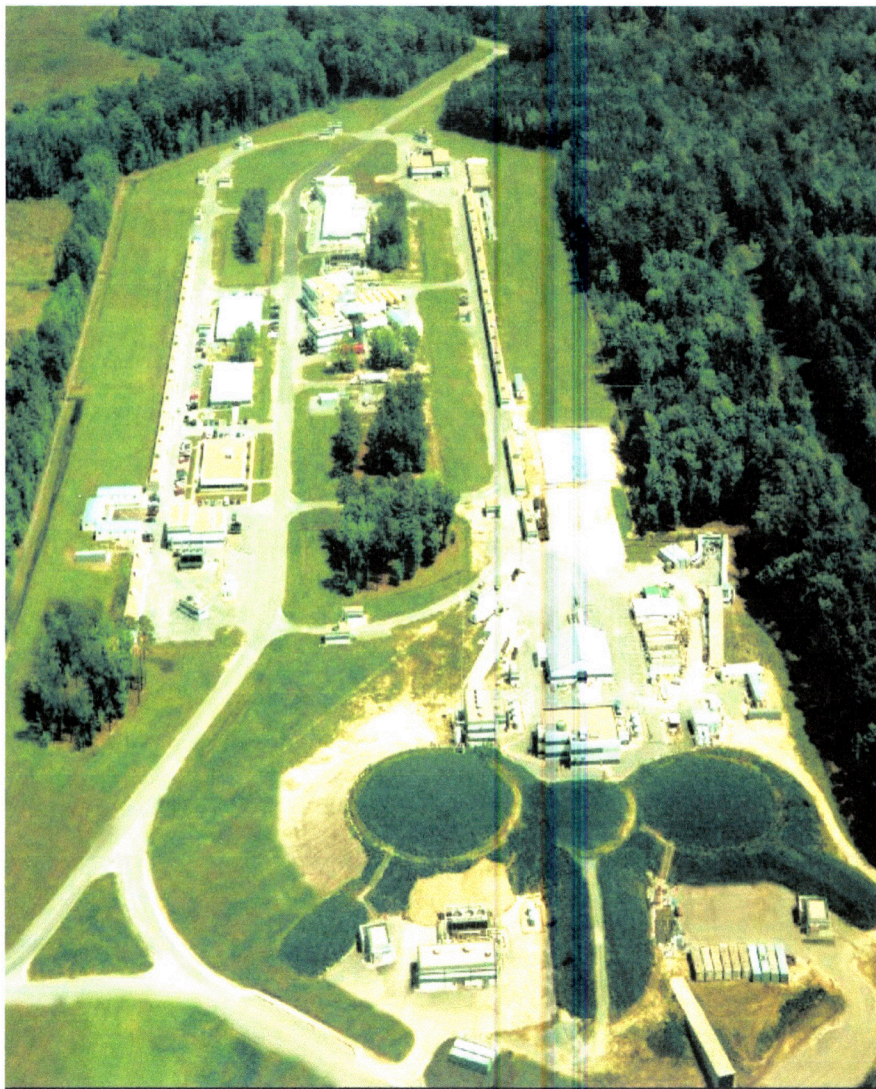
**4. And . . .**

. A. Tang et al.,  
Phys. Rev. Lett. 90, 042301 (

. JLab Experiment E01-015  
Scheduled for **Fall 2004**

Spokesmen: Bill Bertozzi, MIT  
Eli Piazetski, Tel Aviv  
John Watson, Kent Sta  
Steve Wood, JLab

**Trento Workshop March 2004**



The CEBAF accelerator complex  
at Thomas Jefferson Laboratory

**Trento Workshop March 2004**



# We optimized the kinematics to minimize competing processes

HIGH ENERGY, LARGE  $Q^2$

(2 GeV<sup>2</sup>/c<sup>2</sup>)

MEC are reduced as  $1/Q^2$

LARGE  $x$

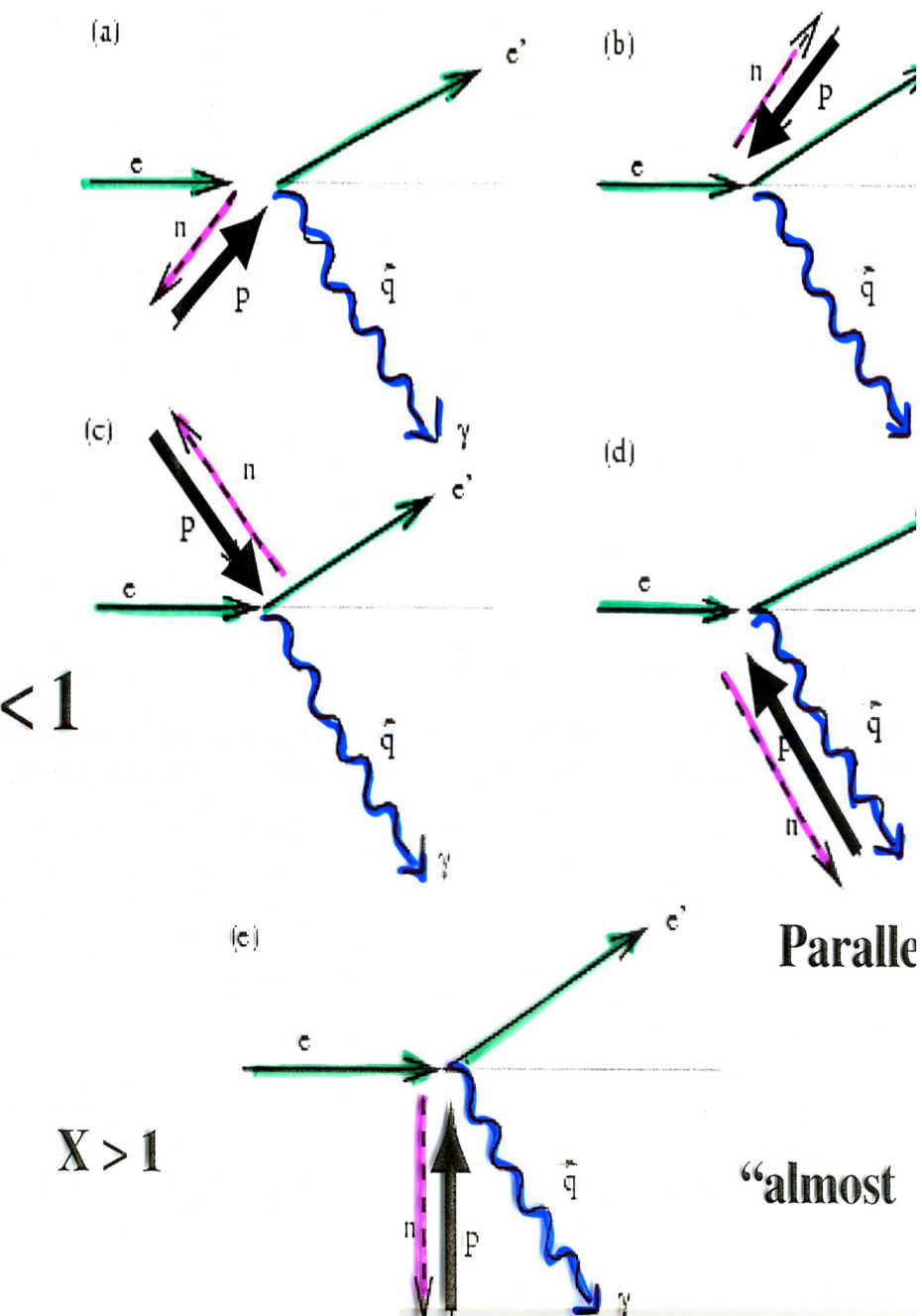
$$= Q^2/2m\nu$$

IC are reduced by performing the experiment in “anti-parallel” kinematics ( $x_B > 1$ ), which is possible only for large  $Q^2$ .

LARGE  $E_m, P_m, P_{mz}$

FSI can be treated in Glauber approximation. Also, the relevant parameter in the light-cone formalism ( $\alpha$ ) is not sensitive to FSI.

Significant reduction, compared to low- $Q^2$  measurements, in the ambiguity of the identification of the struck and recoil nucleons.



**XXXL**

We optimized kinematics to minimize  
the competing processes

**HIGH ENERGY**

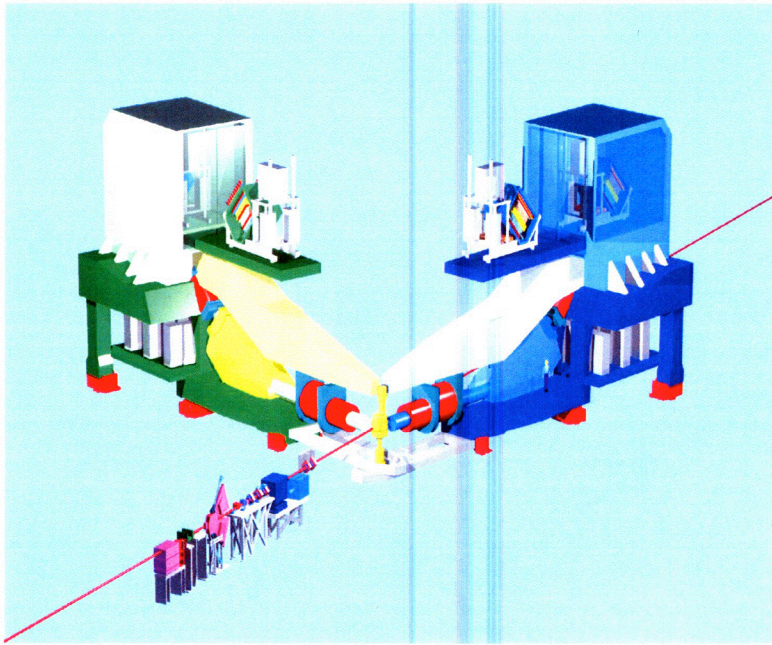
**LARGE  $Q^2$**

**LARGE X**

**LARGE  $E_m, p_m, p_{mz}$**

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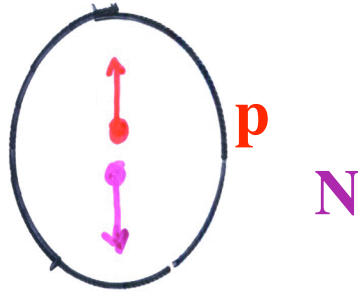
## Hall A at Jefferson Lab



- Two large high resolution spectrometers (HRS) in hall A.
- Hall A has much expertise in performing  $(e,e'p)$  experiments.
- BigBite spectrometer will be used as a third arm in conjunction with the two HRS.

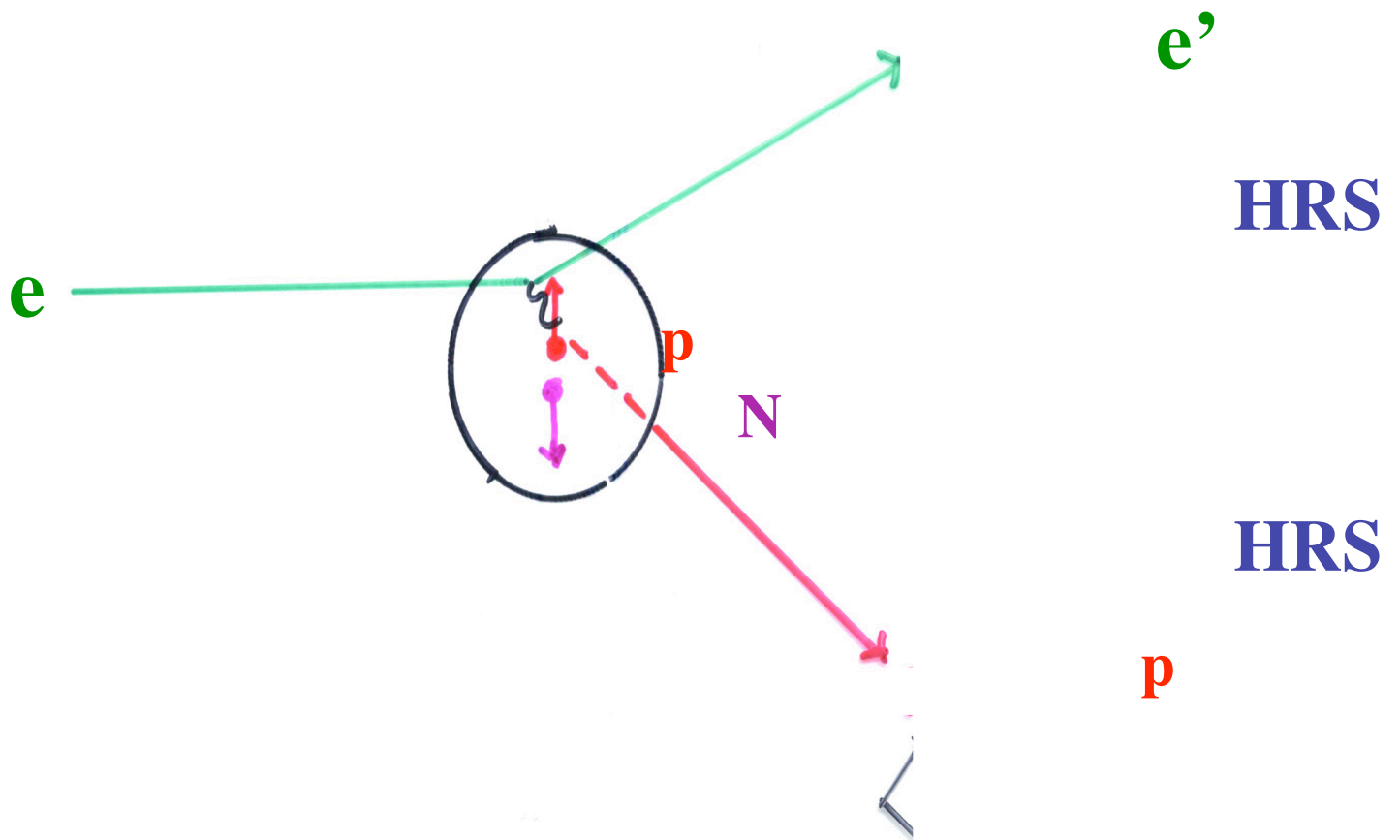


$^{12}\text{C}$

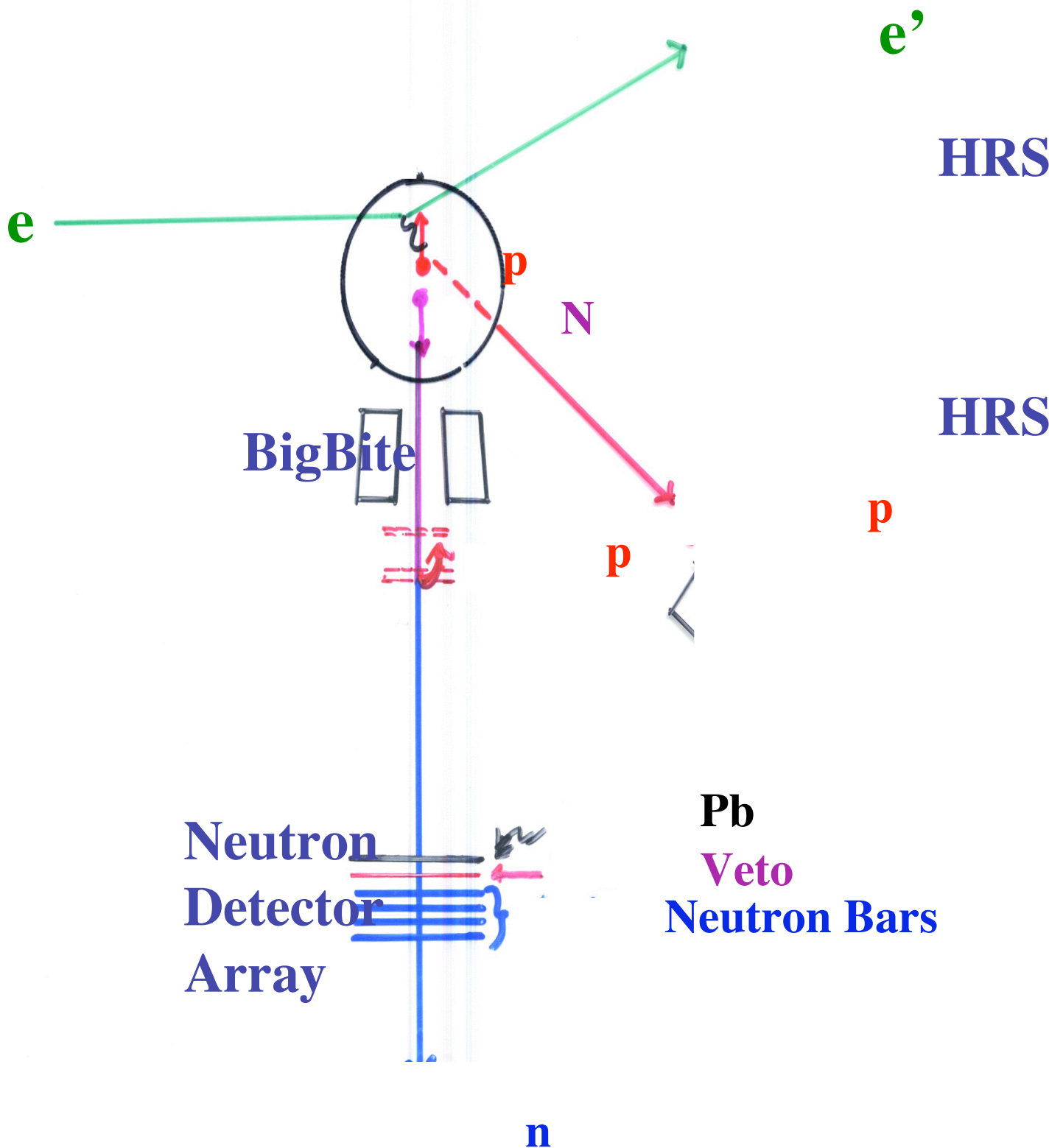


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$^{12}\text{C}(\text{e},\text{e}'\text{p})$

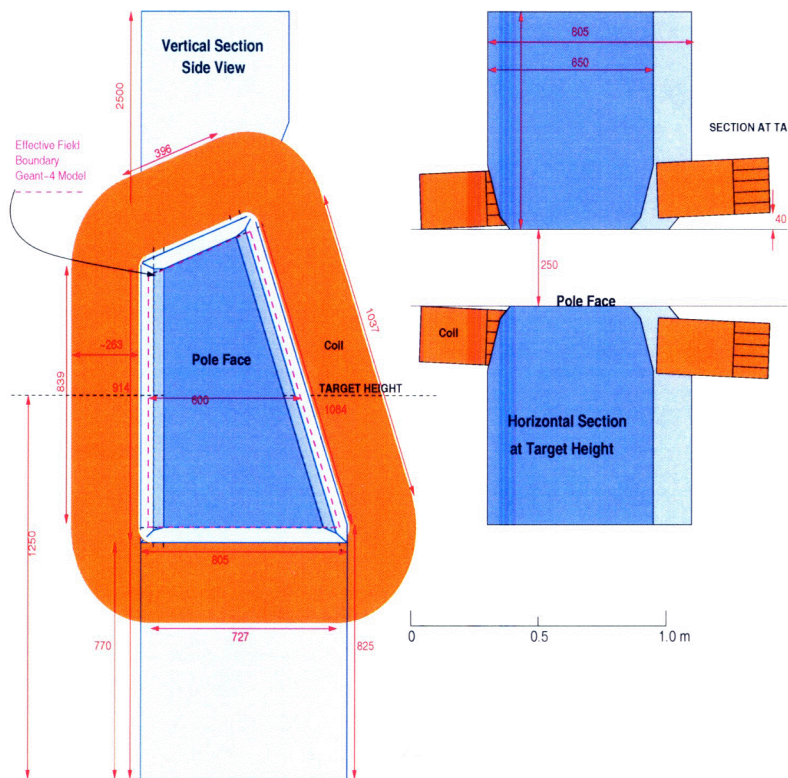


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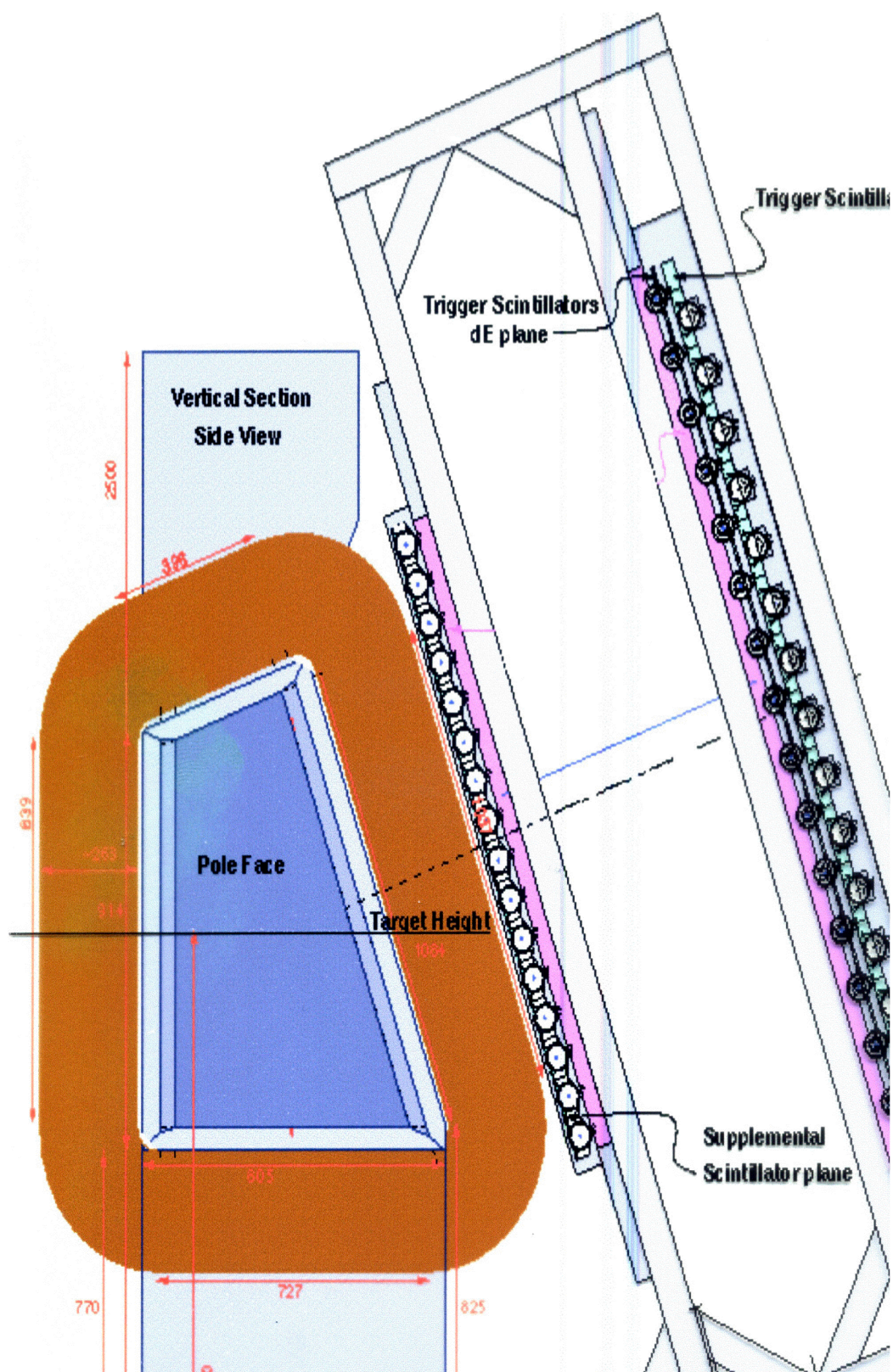


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## The BigBite Magnet



- Angular acceptance of 96 msr.
- Magnetic field strength of up to 1.2 T; experiment will use a field strength of 0.92 T.
- Nominal momentum acceptance of 250 - 900 MeV/c



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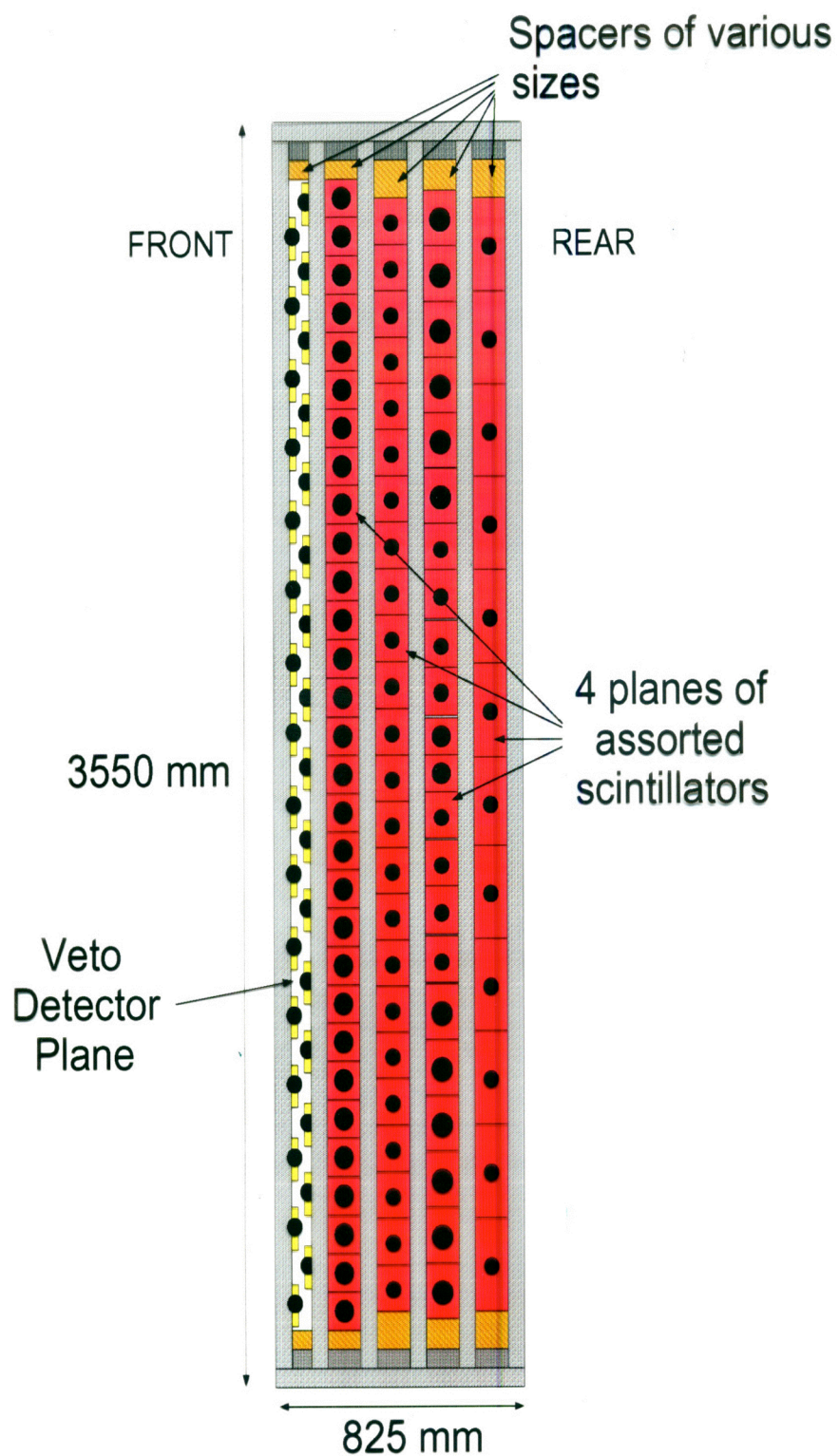


## The Proton Detector



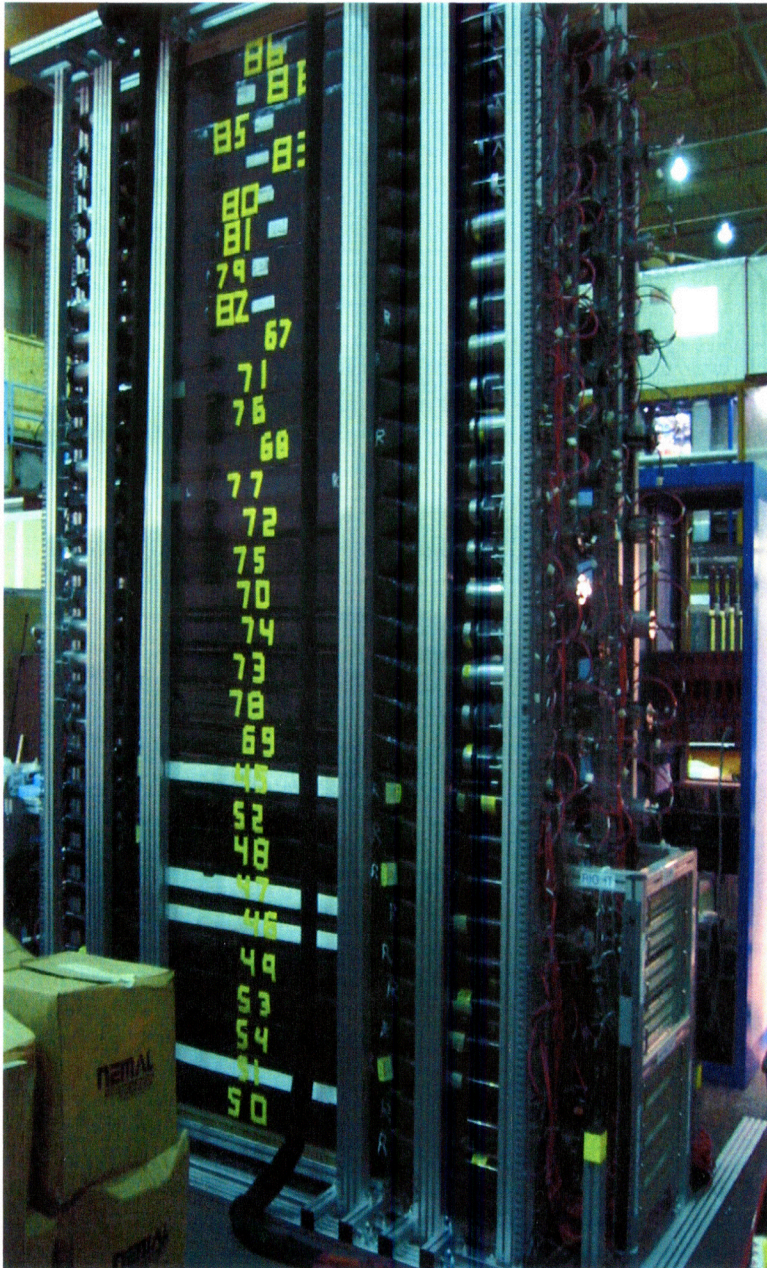
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## Neutron Detector – Side View



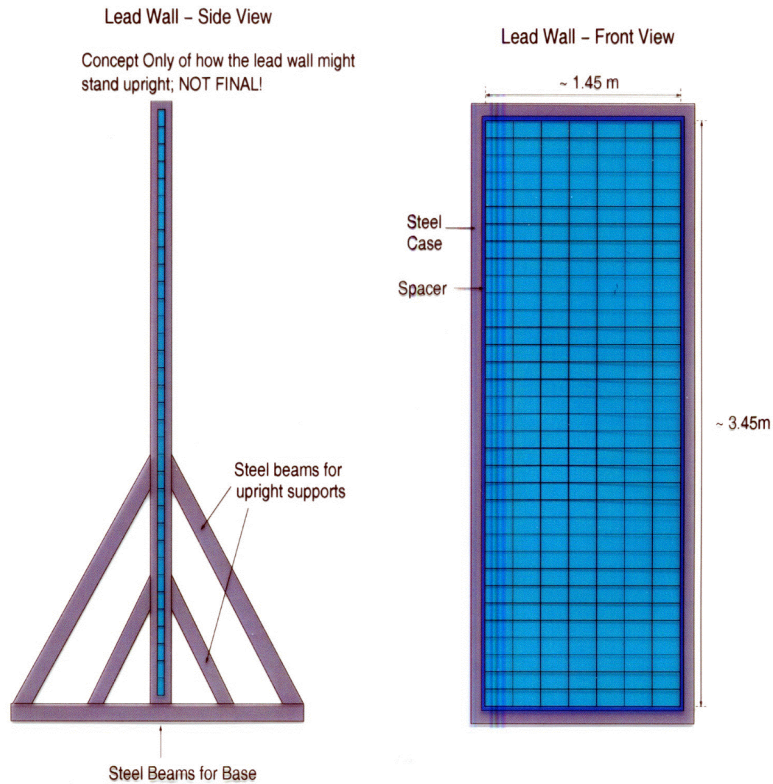


## The Neutron Detector - 2



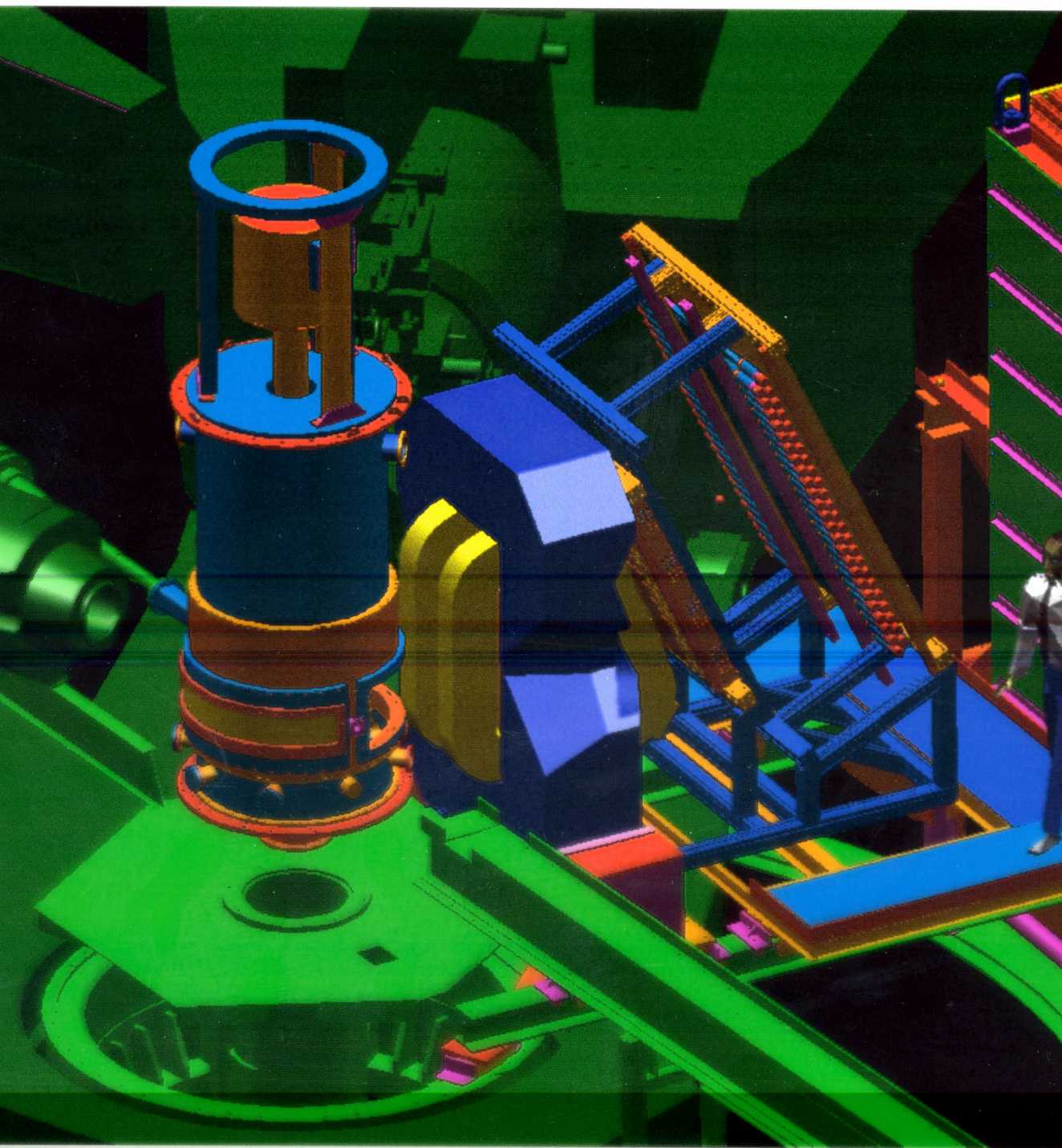
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## Lead Wall



- Require a 2 inch thick lead wall in front of neutron detector to provide radiation shielding.
- Propose to build a wall 3.45m high and 1.45m wide using 238 2 x 4 x 8 inch lead bricks as illustrated.





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