

# Basics of Laser-Plasma Interaction (lecture 3/3)

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# Outline of Lecture 3

## Light sail acceleration

- ▶ heating vs radiation pressure
- ▶ effects of laser polarization
- ▶ 3D effects

## Radiation friction

- ▶ foundations of the problem
- ▶ classical Landau-Lifshitz theory
- ▶ macroscopic effects: magnetic field generation

# Light Sail acceleration with lasers: a “dream bunch”?

Fast scaling and high efficiency of LS acceleration

$$\frac{\mathcal{E}_{\max}}{m_p c^2} = \frac{\mathcal{F}^2}{(2(\mathcal{F} + 1))} \quad \eta = \frac{2\beta}{1 + \beta} = 1 - \frac{1}{1 + \mathcal{F}^2} \quad \xrightarrow{I} \quad \begin{array}{c} \text{Sail} \\ \downarrow \\ \ell \end{array} \quad \begin{array}{c} V = \beta c \\ \rightarrow \end{array}$$

$$\mathcal{F} = \frac{2I\tau_p}{\rho\ell} = \frac{Z}{A} \frac{m_e}{m_p} \frac{a_0^2}{\zeta} \omega\tau_p \quad \left( \zeta = \pi \frac{n_e \ell}{n_c \lambda} \right)$$

if  $\beta \ll 1 \rightarrow \frac{\mathcal{E}_{\max}}{m_p c^2} \simeq \frac{\mathcal{F}^2}{2}, \quad \eta \simeq \mathcal{F}^2$

$\ell \simeq 10 \text{ nm}, I \simeq 10^{21} \text{ W cm}^{-2}, \tau_p \gtrsim 10 \text{ fs} \rightarrow \mathcal{F} \sim 1$

$\mathcal{F} = 1 \rightarrow \mathcal{E}_{\max} = 235 \text{ MeV}, \eta = 0.5$

coherent motion of the sail  $\rightarrow$  mononergetic ion spectrum

Optimal thickness  $a_0 \simeq \zeta$  at the threshold of transparency

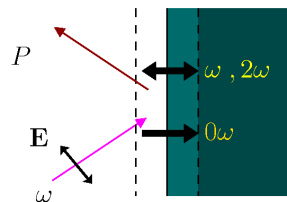
# Forces on the sail

The radiation pressure on the sail arises from the *steady* (“ $0\omega$ ”) ponderomotive force

The laser also exerts oscillating forces

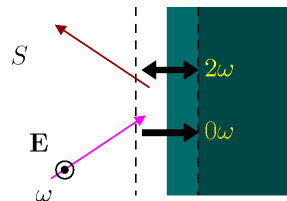
*P*-polarization:  $\mathbf{E}$ -driven,  $\Omega = \omega$

*S*-polarization:  $\mathbf{v} \times \mathbf{B}$ -driven,  $\Omega = 2\omega$



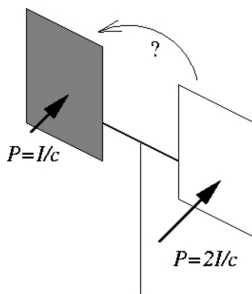
Nonlinear oscillations across the surface cause **electron heating** (the motion across a sharp gradient is non-adiabatic)

Heating is undesired (possibly detrimental) for radiation pressure acceleration





# How to make radiation pressure dominant?



The “Optical Mill” rotates in the sense *opposite* to that suggested by the imbalance of radiation pressure: *thermal* pressure due to *heating* dominates

Enforcing radiation pressure dominance requires to suppress heating of the surface

For ultraintense lasers: radiation pressure push must overcome internal pressure due to the generation of “fast” electrons

# “Vacuum heating” of electrons

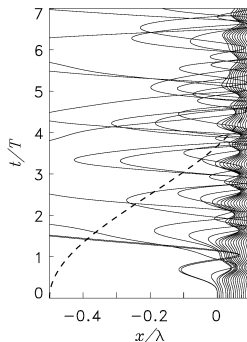
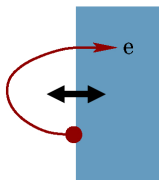
Single particle picture: oscillating forces drag electrons into the vacuum side and push them back in the plasma after an oscillation half-cycle

[Brunel, Phys. Rev. Lett. **59** (1987) 52;

Phys. Fluids **31** (1988) 2714]

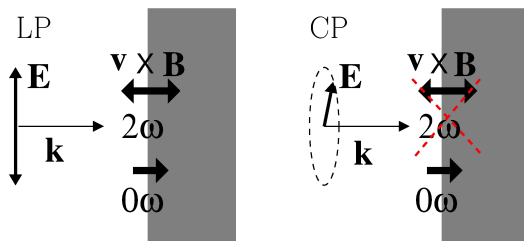
Collective picture: driven plasma oscillations across a sharp gradient “break” and give energy to particles

Electrostatic simulation with Dawson’s sheet model: self-intersection (*wavebreaking*) of fluid elements and generation of “fast” electron bunches



## Circular polarization quenches heating

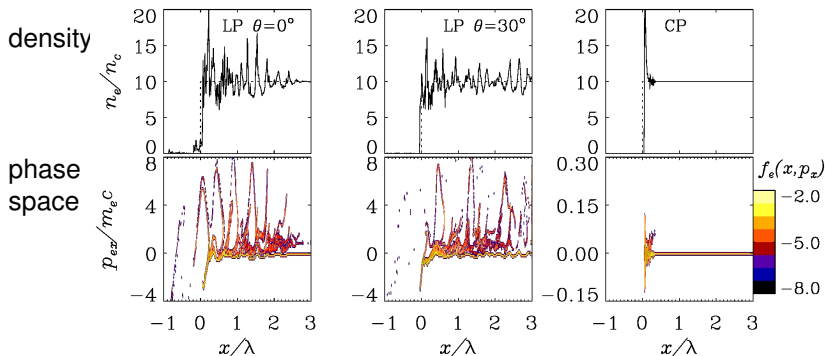
For Circular Polarization (CP) at normal incidence the  $2\omega$  component of the  $\mathbf{v} \times \mathbf{B}$  force vanishes  $\rightarrow$  longitudinal oscillations and heating of electrons are suppressed



Ions respond “smoothly” to steady component:  
radiation pressure dominates the interaction  
[Macchi et al, Phys. Rev. Lett. **95** (2005) 185003]

# Fast electron generation: effect of polarization

1D simulations of laser interaction with solid-density plasma



Linear Polarization: fast electron bunches

at rate  $\omega$  (for  $\theta = 30^\circ$ , P-pol.) or  $2\omega$  (for  $\theta = 0^\circ$ )

Circular Polarization at  $\theta = 0^\circ$ : **no fast electrons** ( $(\mathbf{v} \times \mathbf{B})_{2\omega} = 0$ )

## Fast gain Light Sail in 3D

Transverse expansion of the target  
reduces on-axis surface density  $\rho\ell$

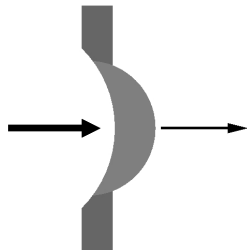
$\Rightarrow$  *light sail gets "lighter"*:

boost of energy gain

at the expense of the number of ions

[S.V.Bulanov et al, PRL **104** (2010) 135003]

LS equations accounting for self-similar transverse dilatation of target in  $D$ -dimensions ( $D = 1, 2, 3$ )



$$r_{\perp}(t) = \Lambda(t)r_{\perp}(0), \quad \sigma = \sigma(t) = \frac{\sigma(0)}{\Lambda^{D-1}(t)}$$

$$\frac{d}{dt}(\gamma\beta_{\parallel}) = \frac{2I}{\sigma(0)c^2} \Lambda^{D-1}(t) \frac{1 - \beta_{\parallel}}{1 + \beta_{\parallel}}$$

## Model for target dilatation

Model: transverse kick due to ponderomotive force

$$\frac{dp_{\perp}(t)}{dt} \simeq -m_e c^2 \partial_r (1 + a^2(r, t))^{1/2} \simeq 2m_e c^2 a_0 r / w \quad (a_0 \gg 1, r \ll w)$$

→ transverse momentum scales linearly with position

$$\frac{d\Lambda}{dt} = \frac{\dot{r}_{\perp}(t)}{\dot{r}_{\perp}(0)} = \frac{\alpha}{\gamma(t)}, \quad \gamma(t) \simeq (p_{\parallel}^2 + m_i^2 c^2)^{1/2}, \quad \alpha \simeq 2 \frac{m_e a_0 c^2 \Delta t}{m_p w^2}$$

Solution in the  $\gamma \gg 1$  limit  $\gamma = \left( \frac{t}{\tau_k} \right)^k, \quad k = \frac{D}{D+2}$

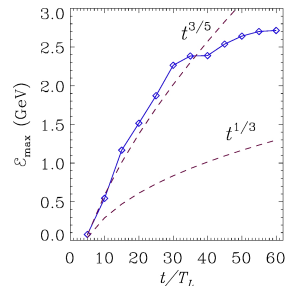
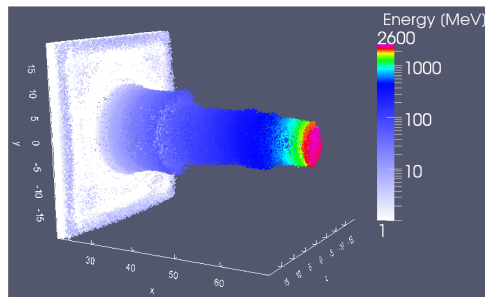
Fastest gain in 3D  $\sim t^{3/5}$  with  $\tau_{3/5} = (48/125\Omega\alpha)^{1/3}$

(note: mechanism is efficient in the relativistic regime).

# High energy gain in 3D LS simulations

Laser: 24 fs, 4.8  $\mu\text{m}$  spot,  $I = 0.85 \times 10^{23} \text{ W cm}^{-2} \Rightarrow 1.5 \text{ kJ}$

Target:  $d = 1 \mu\text{m}$  foil,  $n_e = 10^{23} \text{ cm}^{-3}$

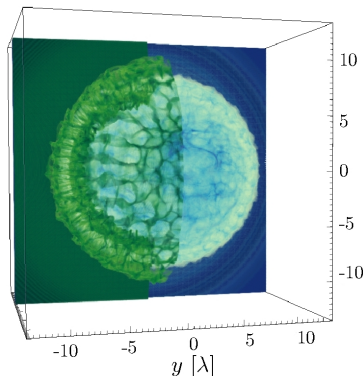


$\mathcal{E}_{\text{max}} \simeq 2.6 \text{ GeV} > 4X \text{ 1D model prediction}$

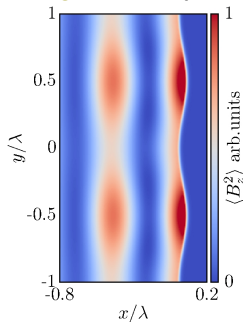
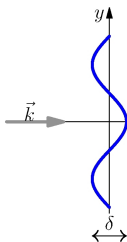
Macchi et al, Plasma Phys. Contr. Fus. **55** (2013) 124020;

Sgattoni et al, Appl. Phys. Lett. **105** (2014) 084105

# Rayleigh-Taylor instability in LS acceleration



target breakup into **net-like structures** with size  $\sim \lambda$  (laser wavelength) and  $\sim$  **hexagonal** shape

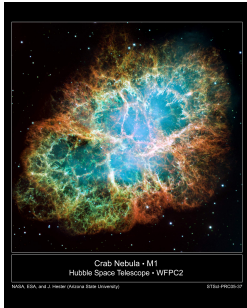


Explanation: **Rayleigh-Taylor** instability stimulated by **radiation pressure modulation**  
 Sgattoni et al, Phys. Rev. E **91** (2015) 013106

field enhancement in surface ripple valleys



# Rayleigh-Taylor Instability in space and lab



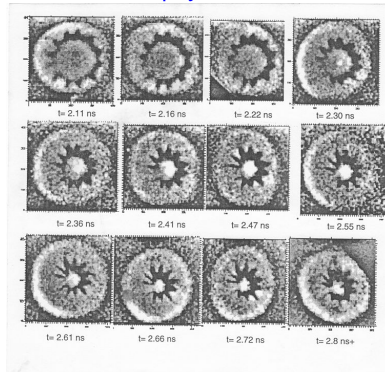
Crab Nebula,  
Hubble Space  
Telescope

**Heavy** fluid over a **light** fluid  
is unstable  
(↑ gravity ↓ acceleration)

Laser-driven  
implosion for  
Inertial  
Confinement  
Fusion studies,  
1995  
(Wikipedia)



[physicscentral.com](http://physicscentral.com)



# Introducing radiation friction - I

Example:

electron in a magnetic field  $\mathbf{B}_0$

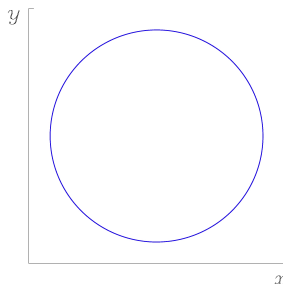
$\mathbf{f}_L = -e(\mathbf{E} + \mathbf{v} \times \mathbf{B}/c)$  Lorentz force

$$m_e \frac{d\mathbf{v}}{dt} = \mathbf{f}_L = -\frac{e}{c} \mathbf{v} \times \mathbf{B}_0$$

Solution: uniform circular motion

$$|\mathbf{v}| = v = \text{const.}$$

$$K = \frac{1}{2} m_e v^2 = \text{constant} \quad \omega_c = \frac{eB_0}{m_e c} \quad r = \frac{v}{\omega_c}$$



## Introducing radiation friction - II

But the electron radiates:

$$P_{\text{rad}} = \frac{2e^2}{3c^3} \left| \frac{d\mathbf{v}}{dt} \right|^2 = \frac{2e^2}{3c^3} \omega_c^2 v^2$$

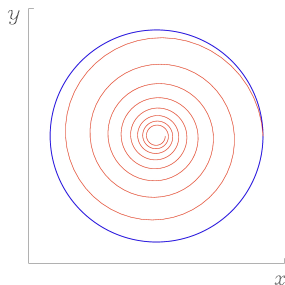
(Larmor's formula for radiated power)

Energy loss due to radiation:

$$\frac{dK}{dt} = -P_{\text{rad}} \quad \longrightarrow \quad v(t) = v(0)e^{-t/\tau}$$

$$\tau = \frac{3m_e c^3}{2e^2 \omega_c^2} = \frac{3c}{2r_c \omega_c^2} \quad r_c = \frac{e^2}{m_e c^2}$$

If  $r(t) \simeq v(t)/\omega_c$ , electron “falls” along a spiral



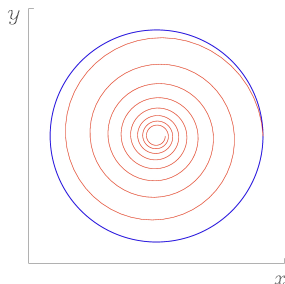
## Introducing radiation friction - III

The Lorentz force does not describe the electron motion consistently:  
need to include an extra force

$$m_e \frac{d\mathbf{v}}{dt} = \mathbf{f}_L + \mathbf{f}_{\text{rad}}$$

Work done by extra force = energy loss

$$\int_0^t \mathbf{f}_{\text{rad}} \cdot \mathbf{v} dt = - \int_0^t P_{\text{rad}} dt \longrightarrow \mathbf{f}_{\text{rad}} = - \frac{2e^2}{3c^3} \frac{d^2\mathbf{v}}{dt^2}$$



Physical interpretation: the electron is affected by the self-generated radiation field (radiation *reaction* or *self-force*)

## Landau-Lifshitz classical approach

$$\mathbf{f}_{\text{rad}} = -\frac{2e^2}{3c^3} \frac{d^2 \mathbf{v}}{dt^2} \text{ is unsatisfying:}$$

- unphysical “runaway” solutions  $\mathbf{a}(t) = \mathbf{a}(0)e^{t/\tau}$
- need of “extra” initial condition  $\mathbf{a}(0)$

$$\left( \mathbf{a} = \frac{d\mathbf{v}}{dt} \right)$$

LL iterative approach brings  $\mathbf{f}_{\text{rad}} = \mathbf{f}_{\text{rad}}(\mathbf{E}, \mathbf{B})$ :

$$\mathbf{f}_{\text{rad}} = -\frac{2e^2}{3c^3} \frac{d}{dt} \left( \frac{d\mathbf{v}}{dt} \right) \simeq -\frac{2e^2}{3c^3} \frac{d}{dt} \left( -\frac{e}{m_e} \mathbf{f}_L \right) = \frac{2e^3}{3m_e c^3} \left( \frac{d\mathbf{E}}{dt} - \frac{e}{m_e c} \mathbf{E} \times \mathbf{B} \right)$$

in the “instantaneous” frame where  $\mathbf{v} = 0$  (note:  $\frac{d\mathbf{E}}{dt} = (\partial_t + \mathbf{v} \cdot \nabla) \mathbf{E}$ )

Note 2<sup>nd</sup> term  $\sim \frac{2}{3} \left( \frac{e^2}{m_e c^2} \right) \mathbf{E} \times \mathbf{B} = \frac{8\pi}{3} r_c^2 \frac{\mathbf{S}}{c} \propto \sigma_T I$  “Thomson drag”

Landau & Lifshitz, *The Classical Theory of Fields*, 2nd Ed., par.76

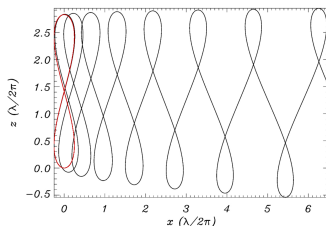
# Relativistic Landau-Lifshitz RF force

Necessary generalization to relativistic regime yields

$$\mathbf{f}_{\text{rad}} = -\frac{2r_c^2}{3} \left\{ \gamma^2 \left[ \left( \mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right)^2 - \left( \frac{\mathbf{v}}{c} \cdot \mathbf{E} \right)^2 \right] \frac{\mathbf{v}}{c} - \left[ \left( \mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right) \times \mathbf{B} + \left( \frac{\mathbf{v}}{c} \cdot \mathbf{E} \right) \mathbf{E} \right] + \gamma \frac{m_e c}{e} \left( \frac{d}{dt} \mathbf{E} + \frac{\mathbf{v}}{c} \times \frac{d}{dt} \mathbf{B} \right) \right\}$$

Dominant term ( $\sim -\gamma^2 \mathbf{v}$ ) acts as a nonlinear friction force

Effect of including  $\mathbf{f}_{\text{rad}}$  on the motion in a plane wave: accelerating drift of the figure-of-eight (constraints of “no-acceleration” theorem are broken)



# Including radiation friction in plasma modeling

- ▶ The electrodynamics of continuous media (a mean field theory) considers only **coherent** emission ( $\lambda \gg n_e^{-1/3}$ ) that governs the **collective** dynamics
- ▶ Electrons also emit **incoherent** radiation ( $\lambda \ll n_e^{-1/3}$ ) which mostly escapes from the medium ( $\omega \gg \omega_p$ )
- ▶ The RF force accounts for the back-reaction of radiation emission at *all*  $\omega$ 's, but in practice only very high  $\omega$ 's are relevant (radiation power strongly scales with  $\omega$ )
- ▶ Including RF in the modeling makes radiation losses consistent with plasma dynamics
- ▶ (All of this is only relevant for high fields and strongly relativistic electrons . . . which is where we are going!)

# RF-induced angular momentum absorption

- ▶ A CP laser pulse carries “spin” angular momentum (AM)  
classical expression:

$$L_z = \int_0^\infty \ell_z(r) 2\pi r dr = - \int_0^\infty \frac{r}{2c\omega} \partial_r I(r) 2\pi r dr$$

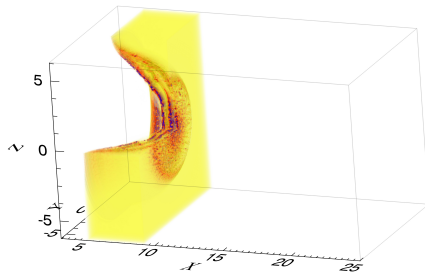
- ▶ in QM, each photon has spin  $\hbar$  independently of  $\omega$
- absorption of photons leads to AM absorption (AMA)
- ▶ Strong radiation emission from a laser plasma
- (many) **low-frequency** (laser) photons are converted into (few) **high-frequency** ( $\gamma$ -ray) photons
- RF inclusion should induce strong AMA in the plasma
- mechanical torque on electrons



# RF-induced “inverse Faraday” effect

- ▶ The AMA-induced torque on electrons drive a solenoidal current
- generation of an axial magnetic field
- ▶ note 1: inverse Faraday effect (IFE) is somewhat a misnomer, but used since its discovery
- ▶ note 2: circular electron orbits in a CP pulse do *not* generate a steady axial field! Note also that the physics is at the edge of the beam ( $\ell_z \propto \partial_r I(r)$ )
- ▶ model for IFE in a plasma, with criticism of earlier theories: M. Haines, PRL **87** (2001) 135005
- ▶ Idea: use IFE-generated magnetic field as a RF signature in (extremely intense) laser-plasma interactions

# Searching for IFE in 3D thick target simulations



$$\lambda = 0.8 \mu\text{m}$$

$$n_e = 90 n_c = 1.6 \times 10^{23} \text{ cm}^{-3}$$

$$a_0 = (200 - 600)$$

$$I = (0.9 - 7.8) \times 10^{23} \text{ W cm}^{-2}$$

$$U = (0.4 - 4) \times 10^3 \text{ J}$$

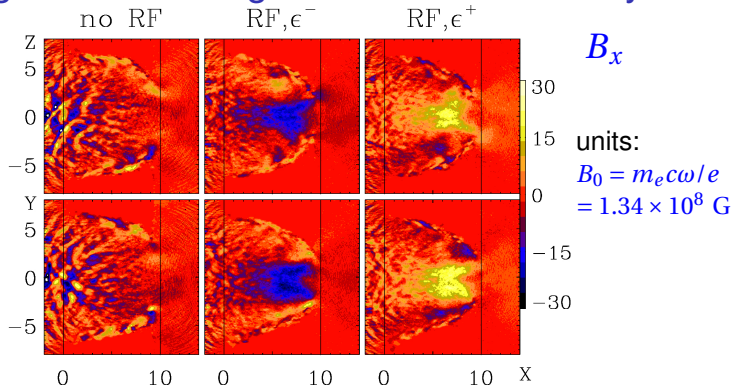
Laser pulse at waist (target boundary)

$$\mathbf{a}(x=0, r, t) = a_0 (\hat{\mathbf{y}} \cos(\omega t) \pm \hat{\mathbf{z}} \sin(\omega t)) e^{-(r/r_0)^n - (ct/r_l)^4}$$

$n = 2$  (Gaussian profile) or  $n = 4$  (super-Gaussian)

$$r_l = 3\lambda, \quad r_0 = 3.8\lambda$$

# Gigagauss axial magnetic fields induced by RF



No axial field without RF

Sign of  $B_x$  changes with laser pulse helicity

T. V. Liseykina, S. V. Propruzhenko, A. Macchi, New J. Phys. **18** (2016) 072001

# Unexpected (and embarrassing) hype ...

physicsworld.com

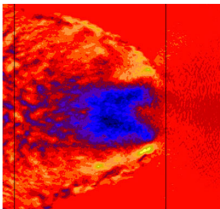
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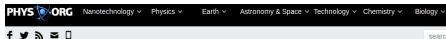
## 'Radiation friction' could make huge magnetic fields with lasers

Jul 19, 2016 @ 2 comments



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August 10, 2016



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Stronger than any magnetic field on Earth.