

Radiation Reaction and Laser Polarization Effects on Ultraintense Laser Acceleration of Thin Foils

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Coworkers

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Motivations

- ▶ Radiation Pressure Dominant Acceleration (RPDA) of thin ($\ell \lesssim 1 \mu\text{m}$) solid foils by ultra-relativistic laser pulses ($a_0 > (m_p/m_e)/2\pi$, $I\lambda^2 > 10^{23} \text{ W cm}^{-2} \mu\text{m}^2$) has been suggested as a route to “unlimited” acceleration towards the GeV/nucleon limit (relativistic ions)

[Esirkepov 04, Bulanov 10]

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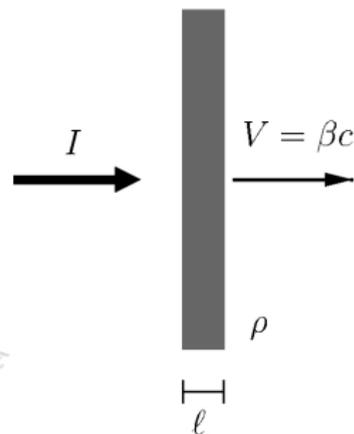
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Physics background 1: Light Sail model

$$E_{\text{ion}}(t) \simeq (2It/\rho\ell c^2)^{1/3} \quad (t \rightarrow \infty)$$

$$E_{\text{max}} \simeq m_p c^2 \mathcal{F} / 2$$

$$\mathcal{F} = 2(\rho\ell)^{-1} \int_0^\infty I(t') dt'$$



Favorable scaling with laser pulse fluence \mathcal{F}

100% efficiency in the relativistic limit

“Perfect” monoenergeticity for “rigid”, coherent motion of the foil

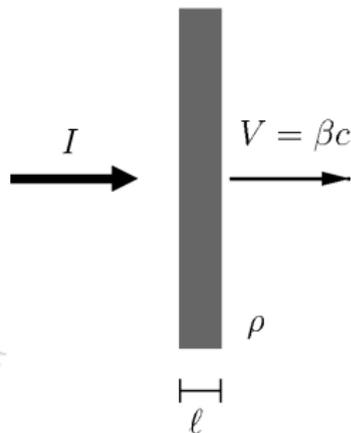
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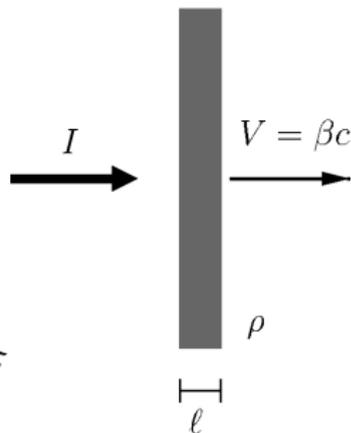
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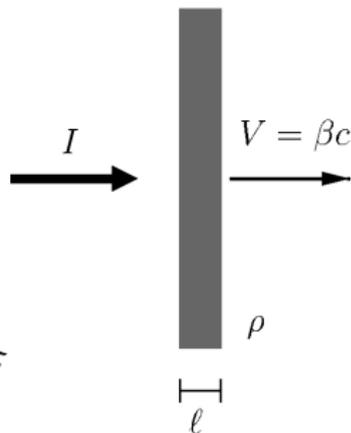
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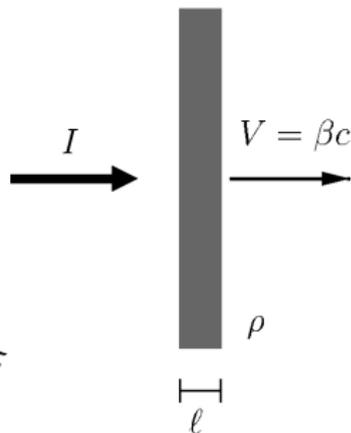
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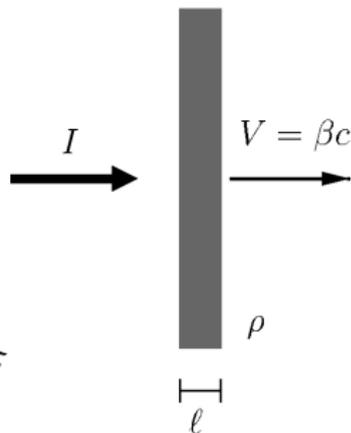
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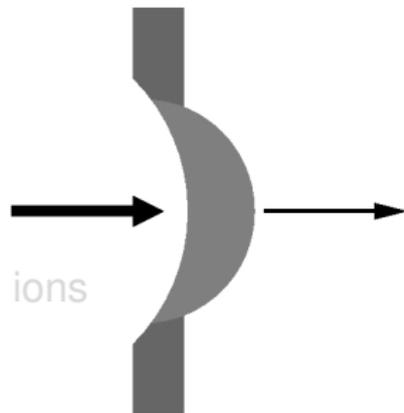
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Physics background 2: “unlimited” acceleration

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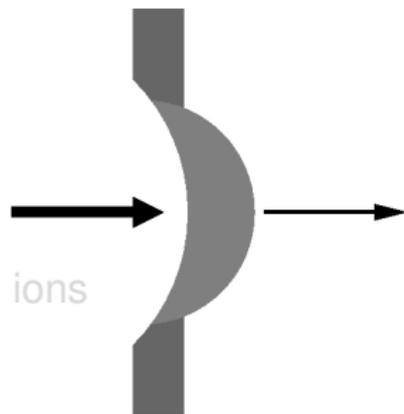
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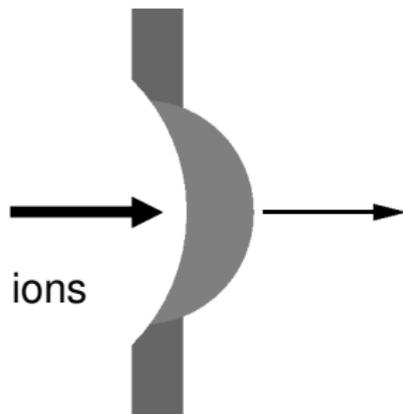
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- ▶ Early numerical demonstration of RPDA [Esirkepov 04] by 3D simulations suggests polarization is inessential
 - ▶ Unlimited acceleration first demonstrated by 2D simulation and circular polarization (CP) [Bulanov 10]
 - ▶ Several studies after [Macchi 05] showed that CP enforces RPDA also at low intensities, although more recent work suggests a regime where also Linear Polarization (LP) works well [Qiao 12]
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Open issues II: radiation friction

- ▶ Radiation Friction (or Radiation Reaction - RR) effects are expected to play an important role in ultrarelativistic laser-plasma dynamics
- ⇒ address role of RR on RPDA
- ▶ Effect of RR on ion acceleration (both in thin and thick targets) investigated by several authors [Schlegel 09, Chen 11, Capdessus 12]
- ▶ Collective laser-plasma acceleration also of interest as the context for first direct observation of RR [Di Piazza 09, Hadad 10]
- ⇒ use RPDA as a test and benchmark case to develop an adequate modeling of RR in laser-plasma interactions

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- ▶ “Feasible” 3D Particle-In-Cell simulations are at the limit of present-day computational resources: hard to check numerical convergence
- ▶ RPDA simulations further challenging because of high density and long times to reach asymptotic regime
- ▶ when including RR the high-energy, low-density tail of the electron distribution needs to be resolved properly
- ⇒ check effects of limited resolution with simulations in lower dimensionality (2D)
- ⇒ upgrade the code for more efficiency, use larger supercomputers . . . and do what you can

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“Reduced” Landau-Lifshitz equation for electrons

$$\begin{aligned}\frac{d\mathbf{p}}{dt} &= -e \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right) + \mathbf{F}_{\text{rad}} \\ \mathbf{F}_{\text{rad}} &= - \left(\frac{2r_c^2}{3} \right) \times \left\{ \gamma^2 \left[\left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right)^2 - \left(\frac{\mathbf{v}}{c} \cdot \mathbf{E} \right)^2 \right] \frac{\mathbf{v}}{c} \right. \\ &\quad \left. - \left[\left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right) \times \mathbf{B} + \left(\frac{\mathbf{v}}{c} \cdot \mathbf{E} \right) \mathbf{E} \right] \right\}\end{aligned}$$

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Radiation Reaction modeling - II

Kinetic equation for electrons and some properties

$$\partial_t f + \nabla_{\mathbf{r}} \cdot (\mathbf{v}f) + \nabla_{\mathbf{p}} \cdot (\mathbf{F}f) = 0, \quad f = f(\mathbf{r}, \mathbf{p}, t)$$

$$\mathbf{F} = -e(\mathbf{E} + \mathbf{v} \times \mathbf{B}/c) + \mathbf{F}_{\text{rad}}, \quad \nabla_{\mathbf{p}} \cdot (\mathbf{F}_{\text{rad}}f) = 0 \neq \mathbf{F}_{\text{rad}} \cdot \nabla_{\mathbf{p}} f$$

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Radiation Reaction modeling - III

- ▶ Simple, modular and computationally cheap algorithm for inclusion in standard PIC codes has been developed [Tamburini et al. NJP **10**, 123005 (2010)]
- ▶ Numerical benchmark of single particle motion with exact solution in a plane wave [Di Piazza 08]
- ▶ High-frequency radiation is assumed consistently to be incoherent and to escape from the plasma; it appears as energy dissipation
- ▶ Dominant term in reduced LL force identical to other models and approximations [Schlegel 09, Chen 11]
- ▶ Classical approach to RR estimated to be valid up to intensities $< 10^{24} \text{ W cm}^{-2}$ (open issue)

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Quoting an anonymous referee:

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Set-up of 3D simulations

- ▶ Laser pulse: $(9T) \times (10\lambda)^2$ (FWHM) [$T = \lambda/c$]
 $\sin^2 \times$ Gaussian shape, $a_0 = 280$ (198) for LP (CP),
 $\lambda = 0.8 \mu\text{m}$
- ▶ Plasma: $\ell = 1\lambda$, $n_0 = 64n_c$, $Z = A = 1$
Note: $a_0 \simeq \zeta = \pi(n_e/n_c)(\ell/\lambda)$
- ▶ Numerical: $1320 \times 896 \times 896$ grid, $\Delta x = \Delta y = \Delta z = \lambda/44$,
 $\Delta t = T/80 = \lambda/80c$, 216 particles per cell (for both e and p),
 1.526×10^{10} in total

Runs performed on 1024 processors (1.7 GBytes each) of IBM-SP6 at CINECA (Italy)

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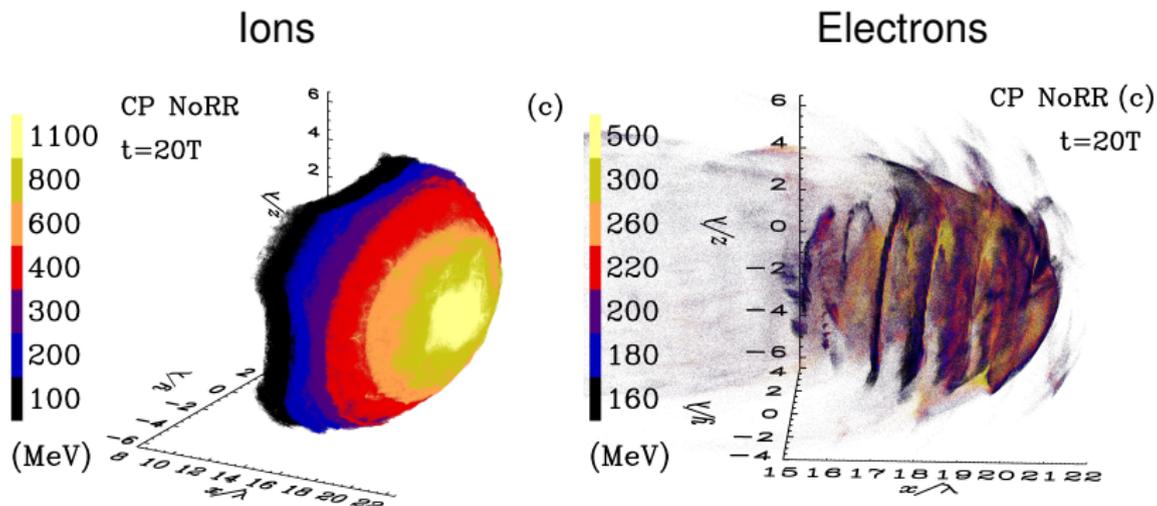
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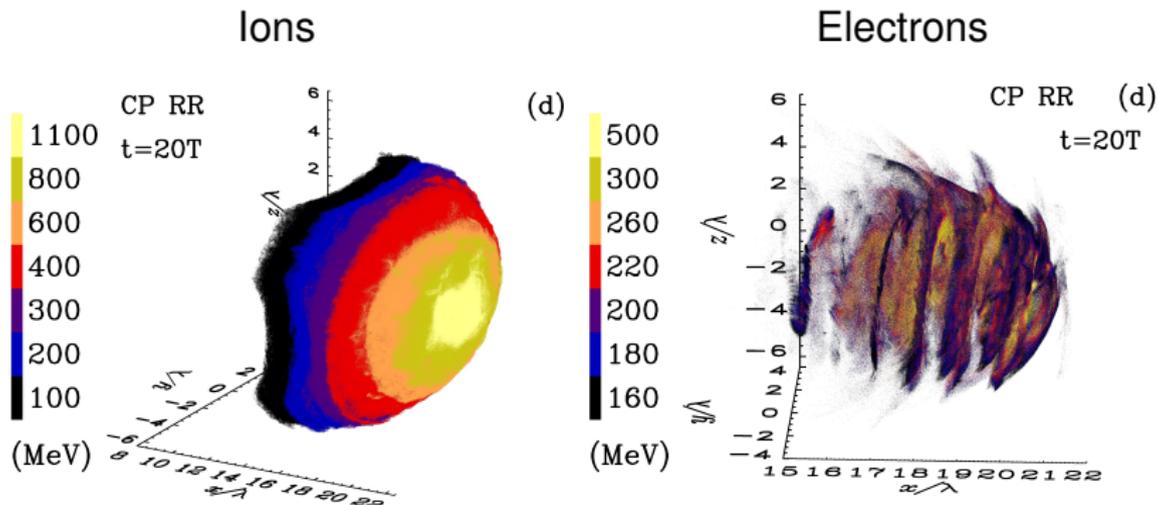
Space-energy distribution: CP, no RR



Symmetric, collimated distribution of ions

Cut-off energy of ~ 1.6 GeV at $t = 20T$

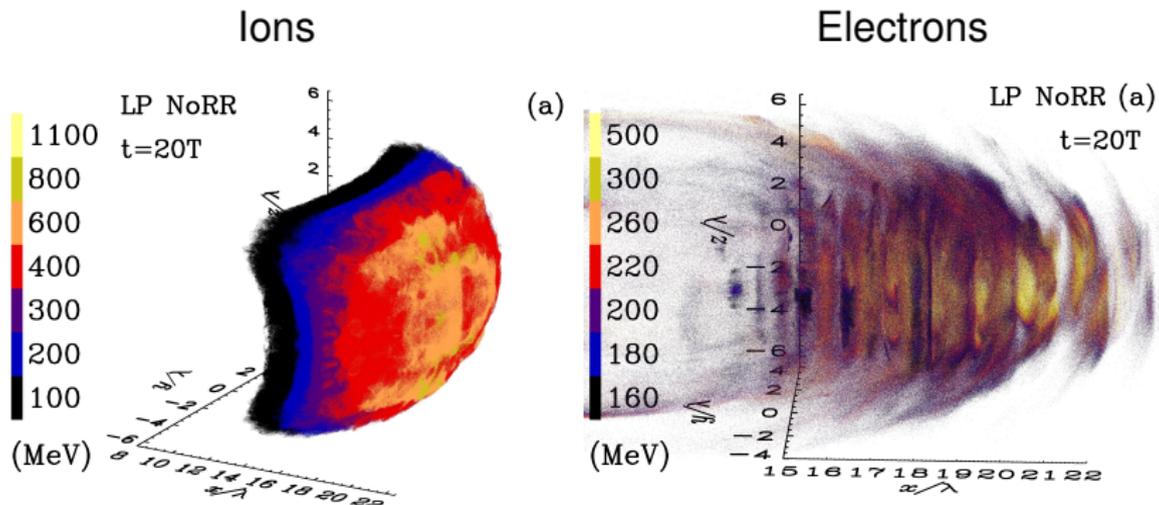
Space-energy distribution: CP, with RR



Ion distribution unchanged by RR

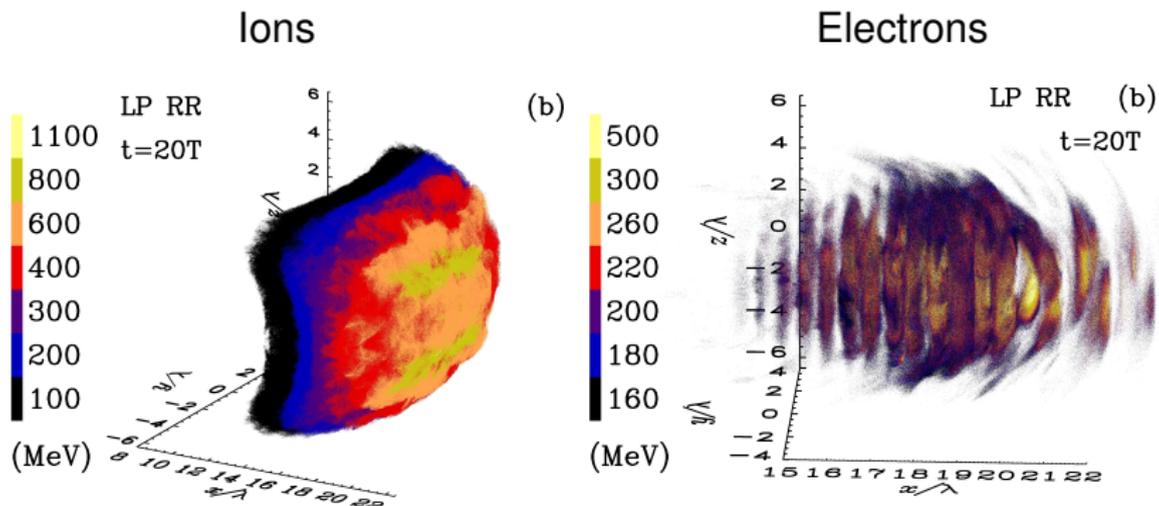
Cooling of electrons in pulse tail due to radiative losses

Space-energy distribution: LP, no RR



Asymmetric distribution with highest energy ions off-axis
Cut-off energy of ~ 0.9 GeV much lower than for CP

Space-energy distribution: LP, with RR

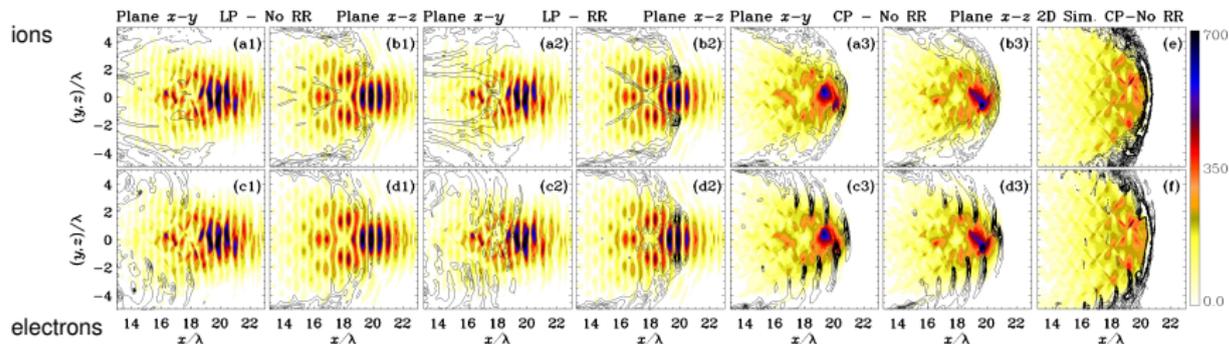


Strong cooling of electrons by radiative losses

Cut-off energy is *increased* up to ~ 1.1 GeV by RR

Pulse self-wrapping by the foil

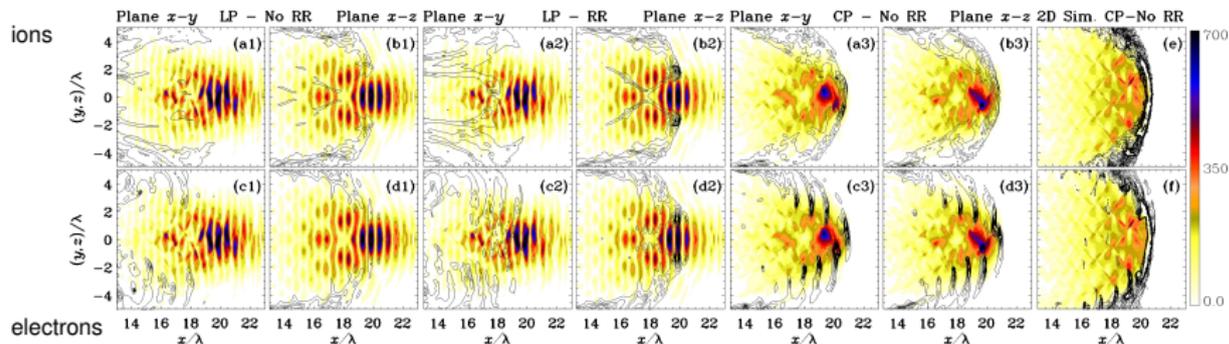
Sections of 3D fields [a1)-d3)] vs 2D simulations [e)-f)]



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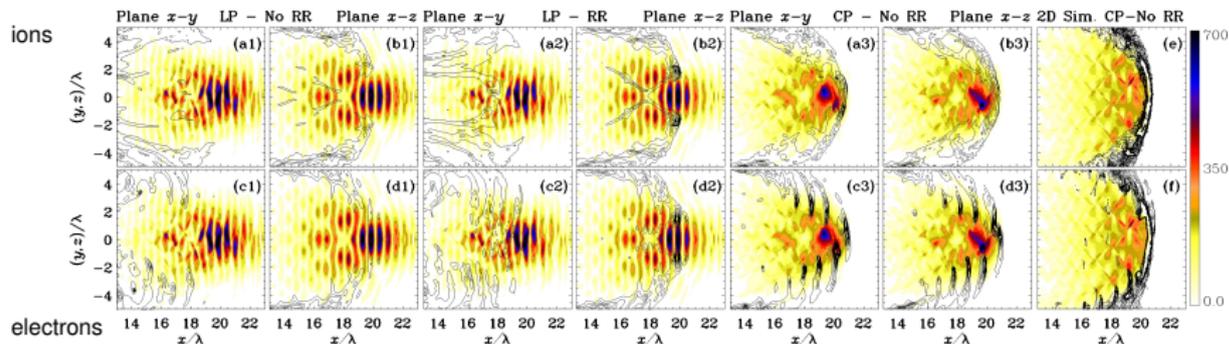
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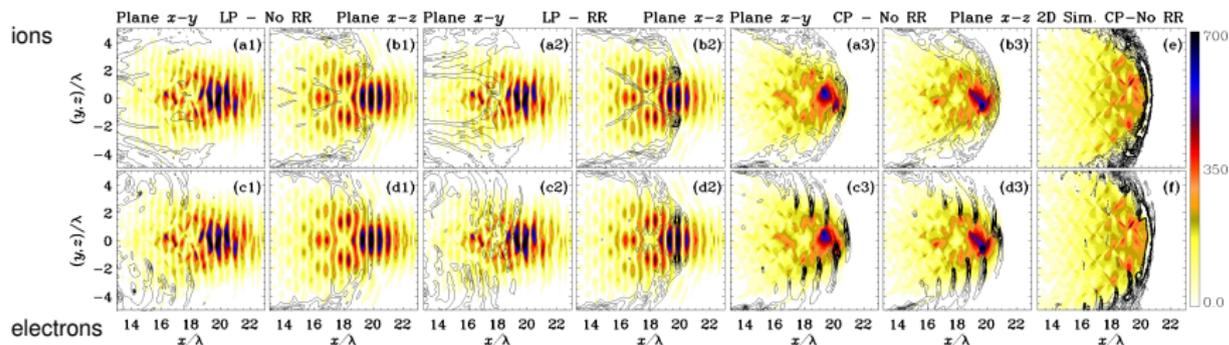
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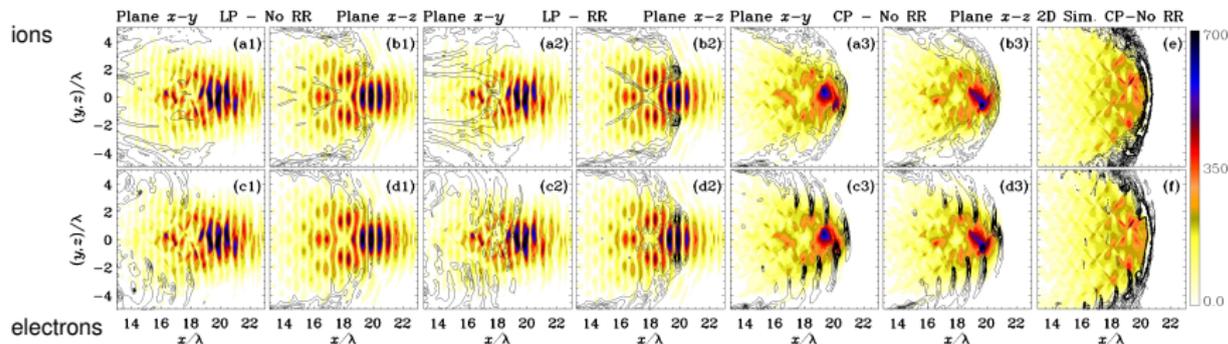
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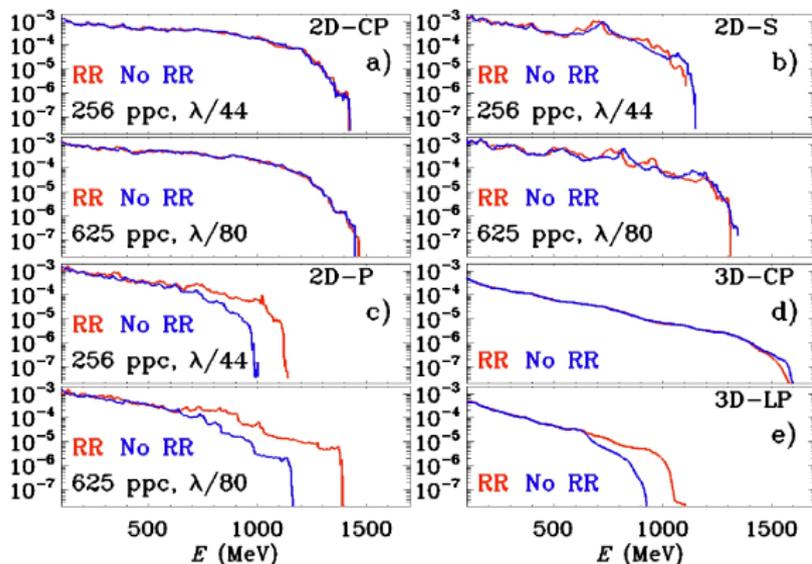
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Effects of reduced dimensionality and resolution

Comparison of 3D ion spectra with 2D results (both S and P for LP) for both the same and higher resolution

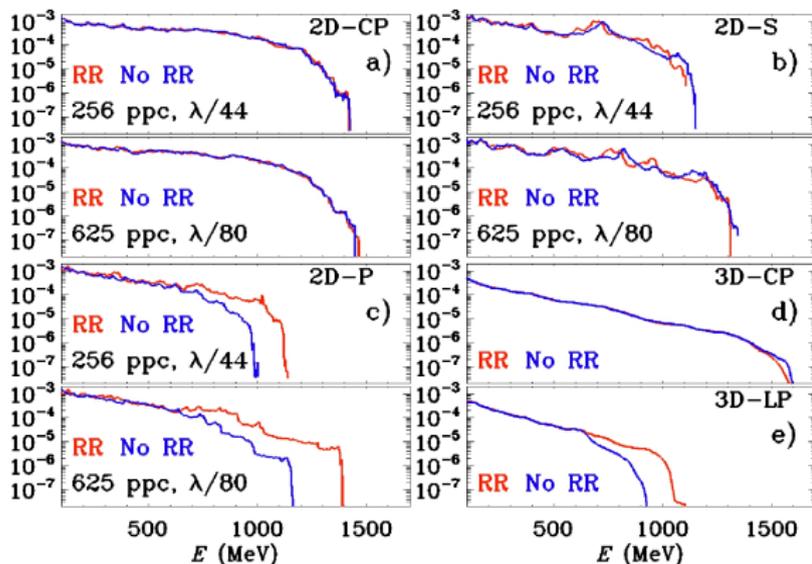


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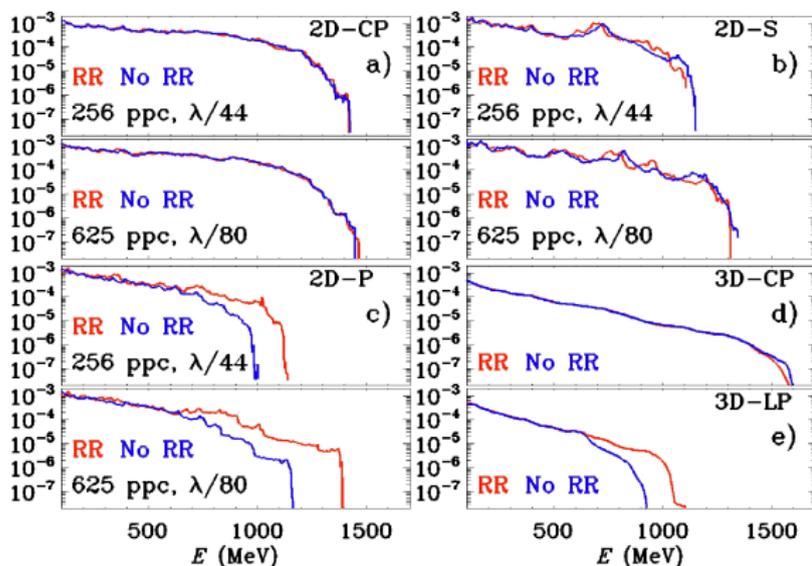


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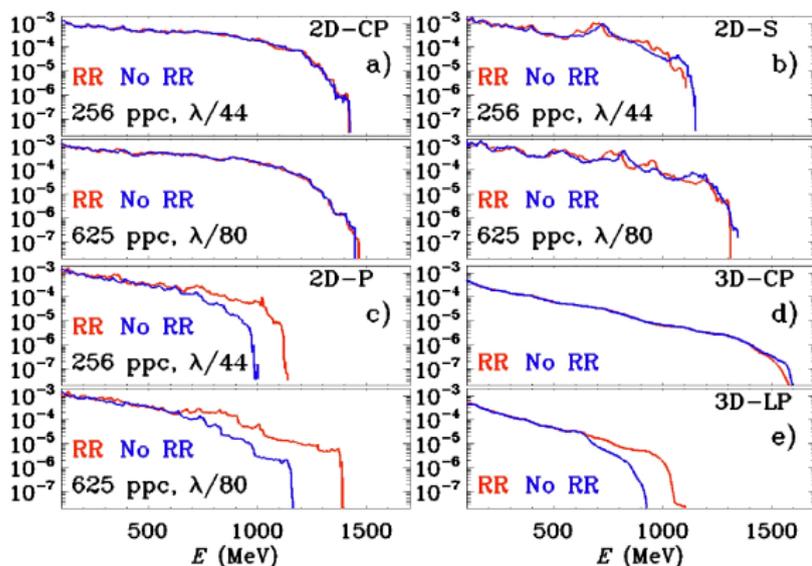


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Explanations for “3D increase”:

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- ▶ M. Tamburini, F. Pegoraro, A. Di Piazza, C. H. Keitel, T. V. Liseykina, A. Macchi, “Radiation Reaction Effects on Electron Nonlinear Dynamics and Ion Acceleration in Laser-Solid Interaction”, Nucl. Inst. Meth. Phys. Res. A **653**, 181 (2011)
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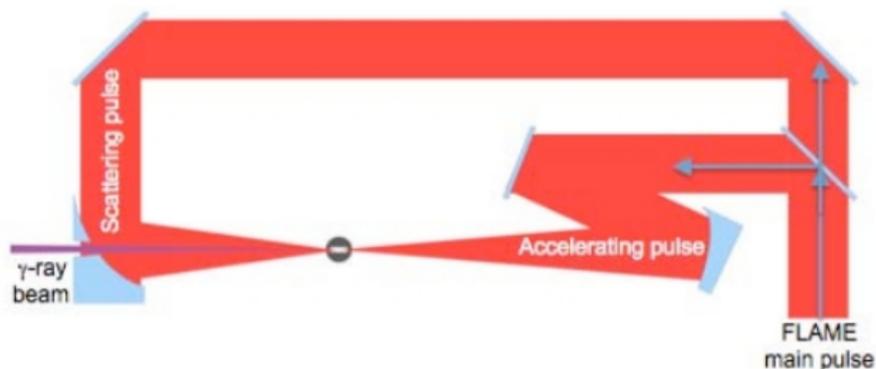
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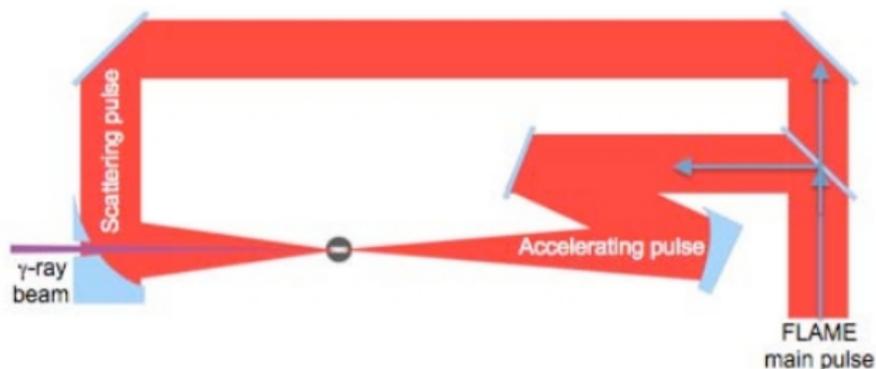
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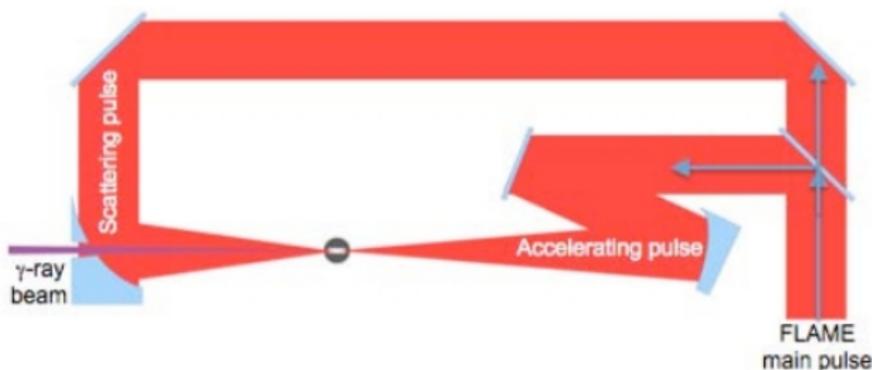
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Acknowledgments

- ▶ Thanks to A. Di Piazza and C. H. Keitel for early collaboration on the Radiation Friction modeling
- ▶ Work sponsored by the FIRB-MIUR (Italy) project SULDIS (“Superintense Ultrashort Laser-Driven Ion Sources”)
- ▶ Use of supercomputing facilities at CINECA (Italy) sponsored by the ISCRA project TOFUSEX (“TOwards FULL-Scale simulations of laser-plasma EXperiments”) award N.HP10A25JKT-2010