

INO-CNR Istituto Nazionale di Ottica

*also at Dipartimento di Fisica "Enrico Fermi", Largo Bruno Pontecorvo 3, 56127 Pisa, Italy www.andreamacchi.eu Radiation Friction Modeling and Effects in Laser-Plasma Interaction at Extreme Intensities

Andrea MACCHI *

Seminar, Institute of Physics, University of Rostock, January 25, 2011

INO Research Unit "Adriano Gozzini" CNR Research Area, Pisa, Italy



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Seminar, Department of Physics, University of Salamanca, March 23, 2011

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ISTITUTO NAZIONALE DI

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OUTLOOK

- 1. Motivations
- Ultra-relativistic laser-plasma interactions
- Radiation Pressure Acceleration: a route to GeV ions?
- Radiation Friction (or Reaction)
- 2. Modeling
- Landau-Lifshitz equation
- Single particle tests and inclusion in PIC codes
- 3. Simulations
- Importance of Radiation Friction for Radiation Pressure Acceleration
- Polarization, anisotropy, and numerical effects

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ULTRARELATIVISTIC LASER PLASMAS



Electron Characteristic Energy

Electron quiver motion

becomes ultrarelativistic:

- new physical phenomena come into play
- new applications can be developed
- new models are needed
 Plasma is the "only" state of matter in such fields!
 Mourou, Tajima, Bulanov,
 Rev.Mod.Phys. 78 (2006) 309

NO-CNR ISTITUTO NAZIONALE DI RELATIVISTIC ION ACCELERATION



Simulations show dominant Radiation Pressure Acceleration (RPA) in interactions at $I > 10^{23}$ W/cm² with thin plasma foils leading to efficient acceleration of relativistic (GeV) ions T.Esirkepov et al, *PRL* **92** (2004) 175003 (It may be possible at lower intensities with circularly polarized pulses:

see e.g. Macchi et al, *New J. Phys.* **12** (2010) 045013 and references therein)



TWO RPA-BASED VISIONS (1996 - 2010)

22

NATURE

JULY 2, 1966 VOL. 211

INTERSTELLAR VEHICLE PROPELLED BY TERRESTRIAL LASER BEAM

By Prof. G. MARX

Institute of Theoretical Physics, Roland Eötvös University, Budapest

PRL 104, 135003 (2010)

PHYSICAL REVIEW LETTERS

week ending 2 APRIL 2010

Unlimited Ion Acceleration by Radiation Pressure

S. V. Bulanov,^{1,*} E. Yu. Echkina,² T.Zh. Esirkepov,¹ I. N. Inovenkov,² M. Kando,¹ F. Pegoraro,³ and G. Korn⁴

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THE "LIGHT SAIL" CONCEPT

to α -Centauri

Originally proposed as a way to accelerate a massive mirror

by the Radiation Pressure of an Earth-based laser

R.L.Forward, "Roundtrip interstellar travel using laser-pushed lightsails",

J. Spacecraft and Rockets **21** (1964) 187

G.Marx, "Interstellar vehicle propelled by terrestrial laser beam", Nature **211** (1966) 22

LASER



Radiation Reaction (RR): back-action on a point-like charge (electron) of the EM fields generated by the charge itself (important for extreme accelerations and ultrarelativistic particles)

[Jackson, Classical Electrodynamics, 3rd Ed., Chap.16;* Landau & Lifshitz, The Classical Theory of Fields, Chap.9, Sec.75-76]

A "RR" term must be added to the Lorentz force to make the motion consistent with the Larmor formula for the radiated power RR is a long-lasting and controversial problem which has attracted new interest recently:

See e.g. F. Rohrlich, Phys. Lett. A 303 (2002) 307;

Gralla et al, PRD 80 (2009) 24031;

Sokolov et al, *Phys.Plasmas* **16** (2009) 93115

*"a completely satisfactory classical treatment does not exist ... the fundamental problem is not solved" (Jackson)



RR is important for ultra-relativistic particles in EM fields: in next generation experiments at ultra-high intensities RR can both play an important role and be diagnosed for the first time [see e.g. Di Piazza et al, *PRL* **102** (2009) 254802; Hadad et al, *PRD* **82** (2010) 096012]

The typical intensity for relevant RR effects is estimated to be $\sim 10^{23}$ W/cm². This corresponds, to the foreseen regime of RPA dominance (for Linear Polarization) [Esirkepov et al, PRL **92** (2004) 175003]

Two RPA simulation studies (for Circular Polarization at lower intensity) suggested a "beneficial" RR effect of "electron cooling" [Schlegel et al, PoP **16** (2009) 083103;

Chen et al, Plasma Phys. Contr. Fus. 53 (2011) 014004]



Search for an approach suitable for inclusion in laser-plasma Particle-In-Cell (PIC) simulations:

- Consistent with a classical, mean field approach (i.e. Vlasov-Maxwell system)
- Reasonable compromise between simplicity and accuracy
- Possible benchmark with some exact solutions
- Inclusion in PIC in a modular way no strong modification of the code needed
- Computationally cheap (not to let CPU time explode ...)

Our "textbook" choice: Landau-Lifshitz approach



"Naivest" approach to RR leads to the Lorentz-Abraham-Dirac equation with pathological solutions

LL approach: approximate (iterative) procedure to write the RR force as a function of the EM fields only

$$f^{\mu}_{\rm RR} = \frac{2e^3}{3mc^2} \left(\partial_{\alpha} F^{\mu\nu} u_{\nu} u^{\alpha} \right) + \frac{2e^4}{3m^2 c^4} \left(F^{\mu\nu} F_{\nu\alpha} u^{\alpha} + (F^{\nu\beta} u_{\beta} F_{\nu\alpha} u^{\alpha}) u^{\mu} \right)$$

Notice: in relativistic regimes in principle one has also to take the coupling with the electron *spin* into account

$$egin{array}{ll} f^{\mu}_{S} &=& -rac{1}{2}Q^{\gamma\delta}\partial^{\mu}F_{\gamma\delta} + rac{1}{2}\left(Q^{\gamma\delta}\partial_{\lambda}F_{\gamma\delta}u^{\lambda}
ight)u^{\mu} \ Q^{\gamma\delta} &=& arepsilon^{\gamma\deltalphaeta}u_{lpha}m_{eta}\,, \qquad m_{eta} ext{ magnetic moment} \end{array}$$

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Equation of Motion with LL force in non-covariant notation (and dimensionless units)

$$\begin{aligned} \frac{d\mathbf{p}}{dt} &= -\left(\mathbf{E} + \mathbf{v} \times \mathbf{B}\right) + \mathbf{F}_{\mathrm{RR}} \\ \mathbf{F}_{\mathrm{RR}} &= -\left(\frac{4\pi r_e}{3 \lambda}\right) \times \\ &\left\{\gamma^2 \left[\left(\mathbf{E} + \mathbf{v} \times \mathbf{B}\right)^2 - \left(\mathbf{v} \cdot \mathbf{E}\right)^2\right] \mathbf{v} \\ &- \left[\left(\mathbf{E} + \mathbf{v} \times \mathbf{B}\right) \times \mathbf{B} + \left(\mathbf{v} \cdot \mathbf{E}\right) \mathbf{E}\right] \\ &+ \gamma \left[\left(\partial_t + \mathbf{v} \cdot \nabla\right) \mathbf{E} + \mathbf{v} \times \left(\partial_t + \mathbf{v} \cdot \nabla\right) \mathbf{B}\right] \right\} \end{aligned}$$

The first "friction" term ($\sim -\gamma^2 \mathbf{v}$) is usually the dominant one

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$$egin{aligned} \dot{\mathbf{p}}_e &= -e(\mathbf{E} + \mathbf{v} imes \mathbf{B}) + \mathbf{F}_{ ext{RR}}, & \dot{\mathbf{x}}_e &= rac{\mathbf{p}_e}{m_e \gamma_e} = rac{\mathbf{p}_e}{\sqrt{\mathbf{p}_e^2 + m_e^2}}, \ & \mathbf{
abla}_{ extbf{p}} \cdot \left(\mathbf{F}_{ ext{RR}} f_e\right)
eq \mathbf{F}_{ ext{RR}} \cdot \mathbf{
abla}_{ extbf{p}} f_e \end{aligned}$$

This is *not* the usual Vlasov (collisionless) equation, but the PIC method provides a solution anyway

It can be shown that $\nabla_{\mathbf{p}} \cdot \mathbf{F}_{\mathrm{RR}} < 0$ and leads to phase space volume "contraction", i.e. "cooling"

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OTHER APPROACHES - I

Sokolov et al, *Phys.Plasmas* **16** (2009) 93115

$$d_t \mathbf{p} = \mathbf{F}_L - \delta \mathbf{v} \times \mathbf{B} - \gamma^2 (\delta \mathbf{v} \cdot \mathbf{F}_L) \mathbf{v}, \qquad d_t \mathbf{x} = \mathbf{v} + \delta \mathbf{v}$$
$$\mathbf{F}_L = -(\mathbf{E} + \mathbf{v} \times \mathbf{B}), \qquad \delta \mathbf{v} = \tau_0 \frac{\mathbf{F}_L - \mathbf{v} (\delta \mathbf{v} \cdot \mathbf{F}_L)}{1 - \tau_0 (\delta \mathbf{v} \cdot \mathbf{F}_L)}$$

Equations of Motion for "'particles' consisting of a large number of electrons, radiating independently and incoherently" notice: $d_t \mathbf{x} \neq \mathbf{v}$

- The EoMs are solved for the *computational* particles in the PIC approach

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OTHER APPROACHES - II

Chen et al, Plasma Phys. Contr. Fus. 53 (2011) 014004

$$\mathbf{F}_{\text{RR}} = d_t \mathbf{p}_{\text{RR}} = -\frac{2r_c}{3\lambda} \gamma^2 \left(d_t \mathbf{p}\right)^2 \frac{\mathbf{v}}{v}, \qquad d_t \mathbf{p} = -(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

"Synchrotron" approximation for the emitted radiation, equivalent to the main "force" term in Sokolov et al.'s

$$d_t \mathbf{p} \simeq -\gamma^2 (\delta \mathbf{v} \cdot \mathbf{F}_L) \mathbf{v}$$

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Exact solution of the Landau-Lifshitz equation in a plane wave [A.Di Piazza, Lett.Math.Phys. **83** (2008) 305]

Based on this test case we identify suitable approximations to the electron EoM with RR included:

- the spin force is $\sim 137 \gamma$ X the last LL term in the RR force
- the first term is $\sim a_0 \omega \tau / 137$ X the spin force

→ for intensities >> 10^{22} W/cm² it is consistent to neglect both the last term and the spin force ; we keep only two terms (which include Chen et al's term and conserve the *mass-shell* condition) *Warning*: at ~ 10^{24} W/cm² quantum effects begin to play a role



The advancement of electron momentum ("particle pushing") is split into two "leap-frog" steps : one for the Lorentz force and one for the RR

 $\frac{\mathbf{p}^{(n+1/2)} - \mathbf{p}^{(n-1/2)}}{\Delta t} = \mathbf{f}^{(n)} = \mathbf{f}_{L}^{(n)} + \mathbf{f}_{RR}^{(n)}$ $\mathbf{p}_{L}^{(n+1/2)} \equiv \mathbf{p}^{(n-1/2)} + \mathbf{f}_{L}^{(n)} \Delta t , \quad \mathbf{p}_{RR}^{(n+1/2)} \equiv \mathbf{p}^{(n-1/2)} + \mathbf{f}_{RR}^{(n)} \Delta t$ $\mathbf{p}^{(n+1/2)} = \mathbf{p}_{L}^{(n+1/2)} + \mathbf{p}_{RR}^{(n+1/2)} - \mathbf{p}^{(n-1/2)}$

The Lorentz step is based on the standard PIC integrator ("Boris pusher") In the RR step, we use the momentum updated by the Lorentz contribution to estimate the velocity at intermediate step

The approach is simple, modular, and suitable for all spatial dimensions (the momentum space is three-dimensional in all PIC codes)



TEST OF PARTICLE PUSHER - I

A numerical solution of motion in a plane wave based on simple 2nd order leap-frog method has been compared with the exact solution and with 4th order Runge-Kutta integration

excellent agreement for intensities up to 10²⁴ W/cm²
straightforward to include in a "standard" PIC code (based on Boris particle pusher)
only ~10% increase in CPU time

[M.Tamburini, F.Pegoraro, A. Di Piazza, C.H.Keitel, A.Macchi, New J. Phys. **10** (2010) 123005]





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Black – with RR

Red \rightarrow without RR





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[M.Tamburini, F.Pegoraro, A. Di Piazza, C.H.Keitel, A.Macchi, New J. Phys. **10** (2010) 123005] Black – Leap Frog Red \rightarrow Runge-Kutta $\lambda = 0.8 \ \mu m, \ a_0 = 350$





THE ENERGY BALANCE

The RR force acts a a friction: energy is *not* conserved in the system.

The friction effect physically corresponds to the emission of high-frequency radiation by ultra-relativistic electrons.

The high-frequency radiation is consistently assume to be incoherent and escape from the plasma

The "energy loss by radiative effects" is evaluated by comparing the energy balance in simulations with and without RR (energy is typically conserved by $\sim 1\%$ in the 1D PIC code without RR)

Note: energy and momentum are *not* conserved exactly in the LL EoM for the *single* electron, but the neglected terms are smaller than quantum contributions



Radiation Pressure Acceleration of a thin foil (0.2-1.0)x 10^{24} W/cm², 11 cycles pulse, 1µm foil, 100n

linear polarization (LP)

Lower energy, narrower spectrum when RR included

Warning: highest intensity case (10^{24} W/cm^2) possibly beyond classical limit





2.3x 10^{23} W/cm², 11 cycles pulse, 1µm foil, 100 n_{a} , LP



~25% reduction in "peak" ion energy " due to RR effects

~20% pulse energy "radiated away" when RR is included



CIRCULAR POLARIZATION

Same parameters as Linear Polarization (0.2-1.0)x 10^{24} W/cm², 11 cycles pulse, 1µm foil, 100n

- circular polarization
- below threshold for pulse breakthrough
- Negligible RR effects on spectrum
- Higher ion energy than in LP case





At normal incidence, for Linear Polarization the vXB force has a 2ω longitudinal component driving a push-and-pull motion of electrons across the surface, with strong heating

For Circular Polarization, the 2ω force is absent: steady push of the target





DISCUSSION: CP VS LP

Conjecture by Esirkepov et al: RR effects are not important in relativistic RPA because the RR strength parameter $\sim r/\lambda$ decreases in the frame of the foil target

For CP the foil moves coherently at $v_x \sim c$ The EM field is similar to a copropagating plane wave (reflection is small) and the LL force vanishes when $v_x = c$

For LP the $\bigvee XB$ force at 2ω drives strong longitudinal oscillations of electrons increasing the RR effect (the LL force in a plane wave is maximum for

counterpropagating electrons: $v_r = -c$)



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CASE OF PULSE BREAKTHROUGH

 $2.3x\;10^{23}\;W/cm^2$, 11 cycles pulse, $0.3\mu m$ foil, 100*n* ,

The pulse now penetrates through the thinner foil due to "relativistic" Self-Induced Transparency, driving strong longitudinal motion also for CP

RR effects are now important for CP and *increase* the ion energy, but the parameters are not optimal (thicker foil has higher energy and narrower spectrum



CP



$10^{23}\ W/cm^2$, 11 cycles pulse, 0.5µm foil, 169 $n_c^{}$, Circular Polarization



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"Best" case for CP (higher cutoff energy)

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For LP differences between *S* and *P* suggest strong anisotropy in the "real" 3D case





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NUMERICAL EFFECTS

Some "convergence tests" preliminary to 3D simulations

ppc= particles per cell $\lambda/\Delta x = (35, 60, 80)$

Results are sensitive to the total number of particles!!!



(RR effects *emphasize* the differences)

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3D SIMULATIONS (PRELIMINARY) - LP ISTITUTO NAZIONALE DI



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- A relatively "simple and cheap" model for inclusion of Radiation Reaction in PIC codes via the Landau-Lifshitz equation has been developed and tested

- in 1D, RR effects on Radiation Pressure Acceleration at ultrahigh intensities are important for Linear Polarization or in the Self-Induced Transparency regime; RR is negligible for Circular Polarization and "optimal" target thickness

- 2D simulations suggest strong anisotropy and polarization effects

- on the route to 3D simulations, numerical effects for too low number of particles must be considered with care



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www.df.unipi.it/~macchi/TALKS/