

REAZIONI NUCLEARI DI INTERESSE ASTROFISICO

Laura Elisa Marcucci (Università di Pisa e INFN-Pisa)

Riassunto del corso:

- teoria del momento angolare → costruzione delle funzioni d'onda
- teoria perturbativa dipendente dal tempo: calcolo della sezione d'urto (e fattore astrofisico)
- funzioni d'onda: stati legati (d , ^3He , ^3H) e stati di scattering (pp , np , Nd) anche con potenziali realistici
- corrente nucleare: termine one-body e meson-exchange currents
- reazioni considerate in dettaglio:



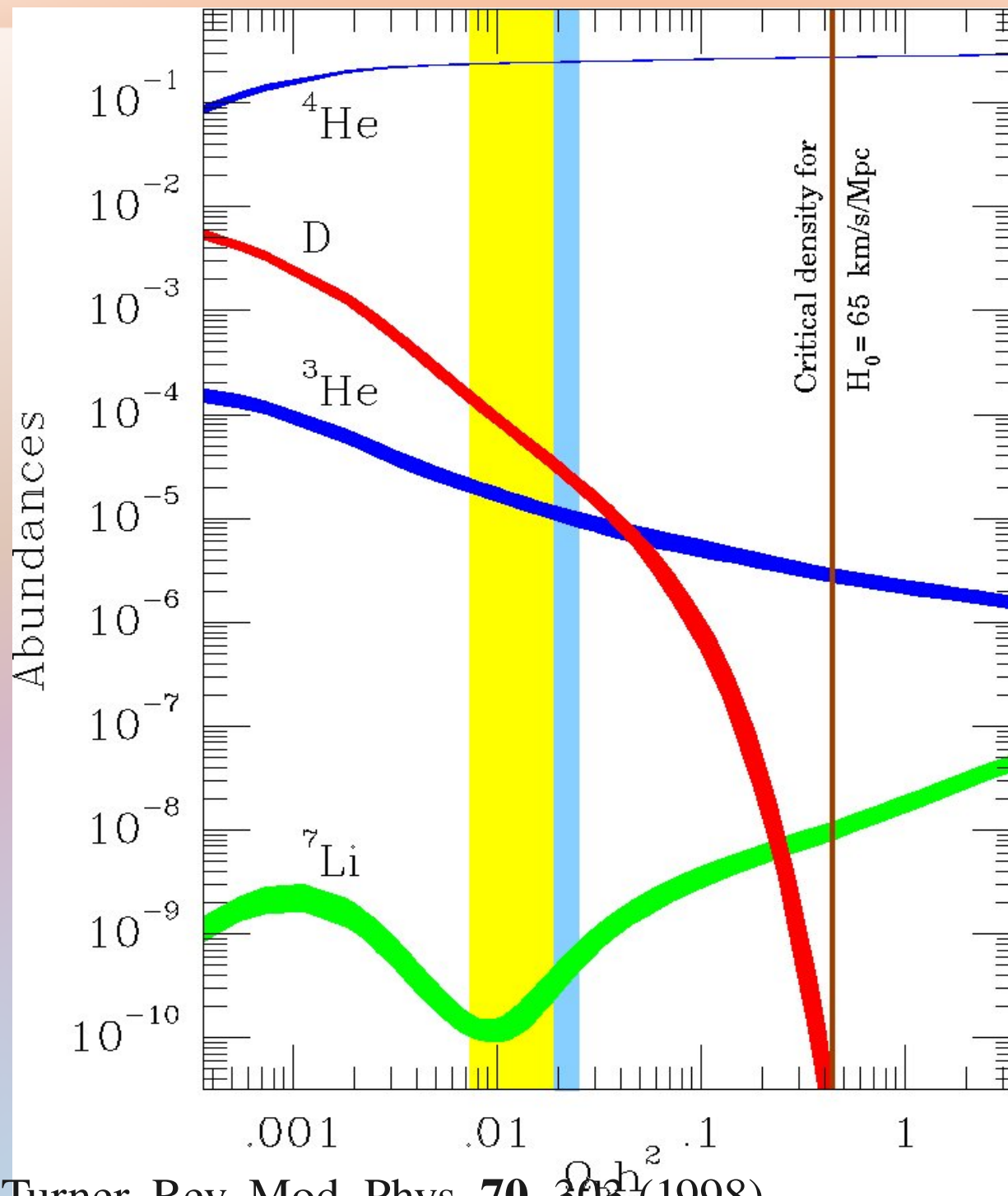
Campi di applicazione

- Big Bang nucleosynthesis (BBN)
- Produzione solare di energia attraverso una catena di reazioni nucleari

Big Bang nucleosynthesis (BBN)

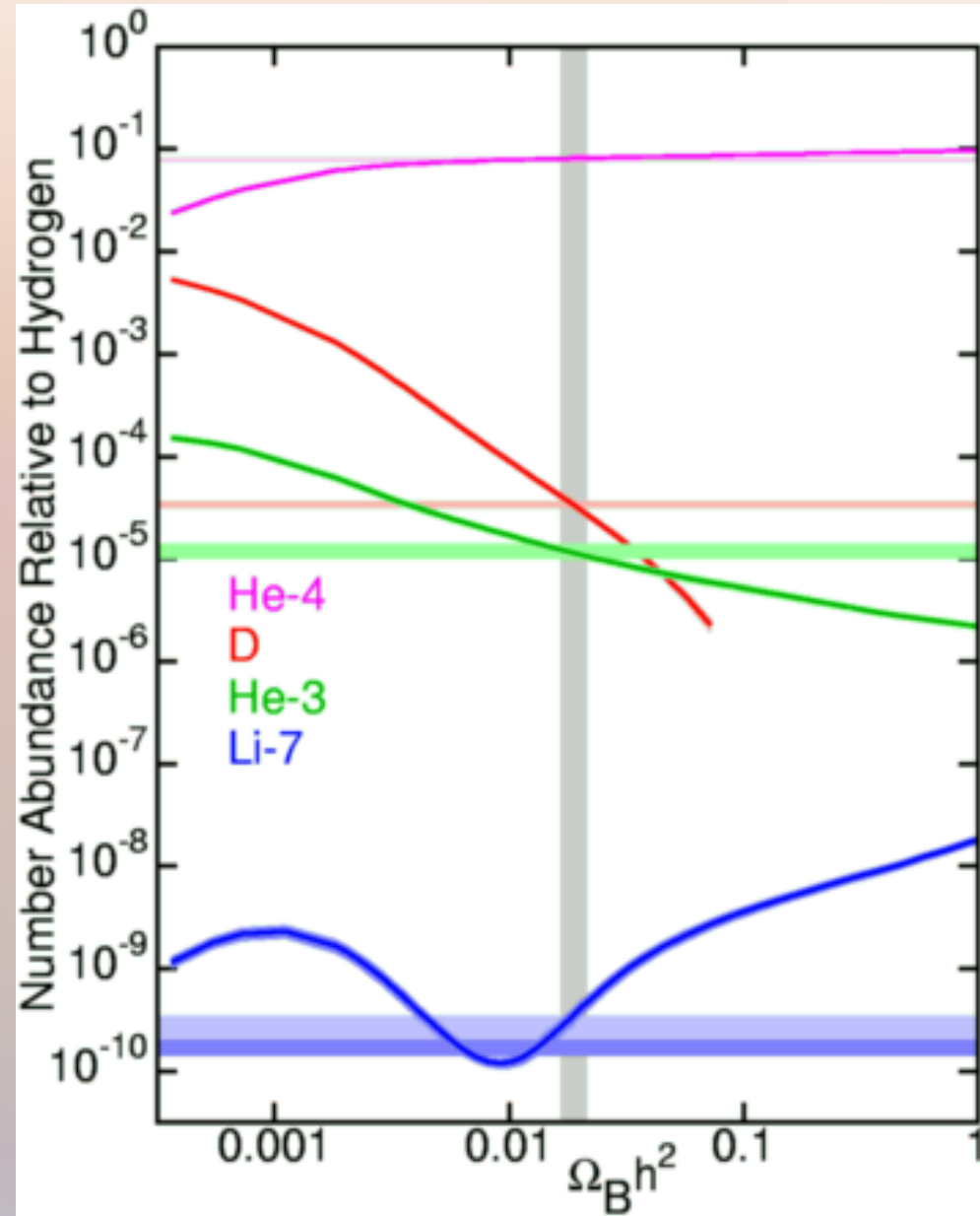
(naive picture)

- Step 1 ($kT < \text{few MeV}$): thermal eq.; $n/p \sim 1$
 - Step 2 ($kT \sim 0.7 \text{ MeV}$): weak int. freeze-out, $n/p \sim 1/6 \rightarrow 1/7$
 - Step 3 ($kT \sim 0.5 \text{ MeV}$): nuclear reactions, which form d , ${}^3\text{He}$, ${}^4\text{He}$, ${}^7\text{Li}$
- 11 key nuclear reactions, among which:
- $n + p \rightarrow d + \gamma$
 - $p + d \rightarrow {}^3\text{He} + \gamma$
 - ${}^3\text{H} + \alpha \rightarrow {}^7\text{Li} + \gamma$
 - ${}^3\text{He} + \alpha \rightarrow {}^7\text{Be} + \gamma$
 - ${}^7\text{Be} + n \rightarrow {}^7\text{Li} + p$

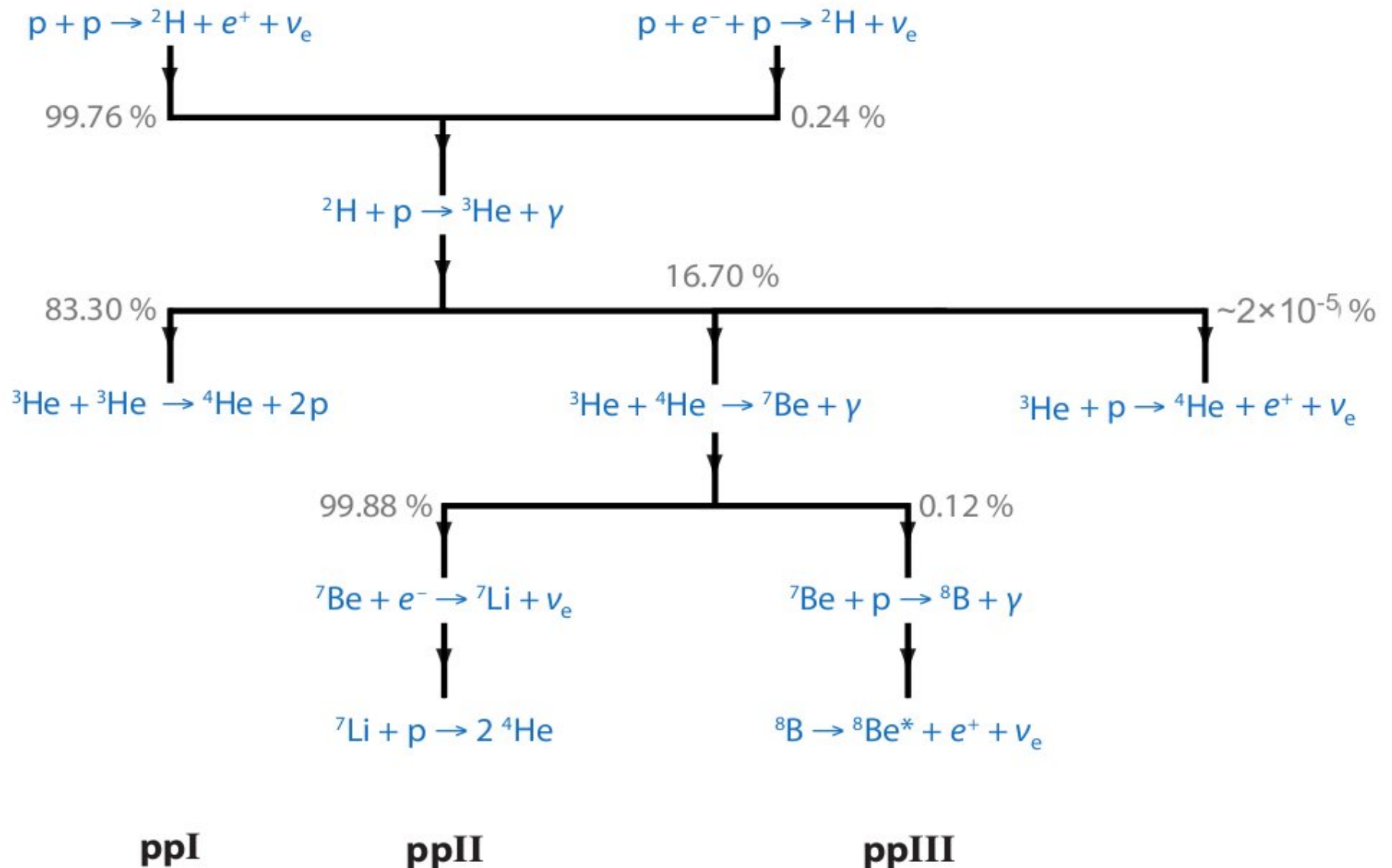


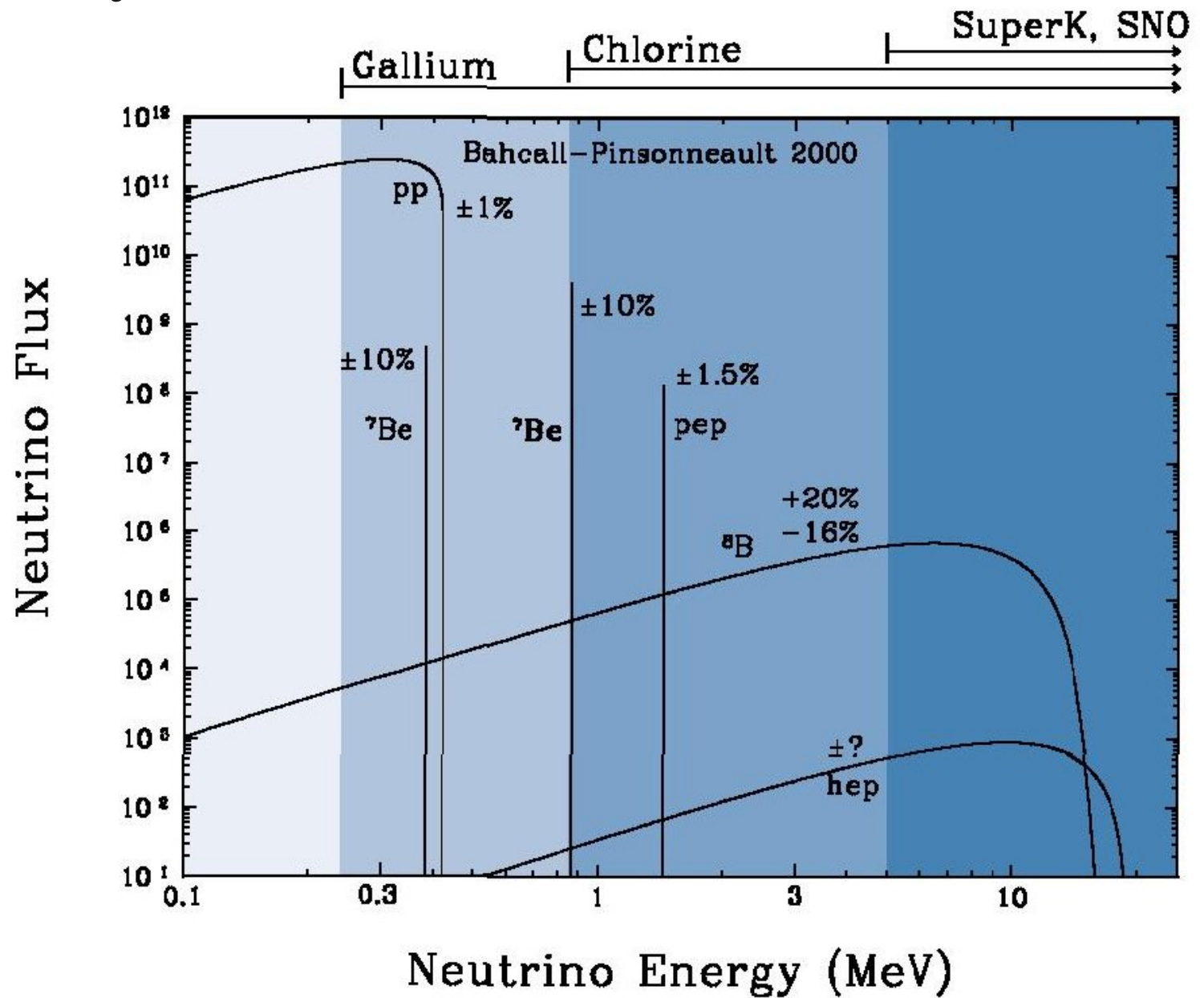
Schramm and Turner, Rev. Mod. Phys. **70**, 303 (1998)

But at present ...



Solar neutrinos: the *pp* chain



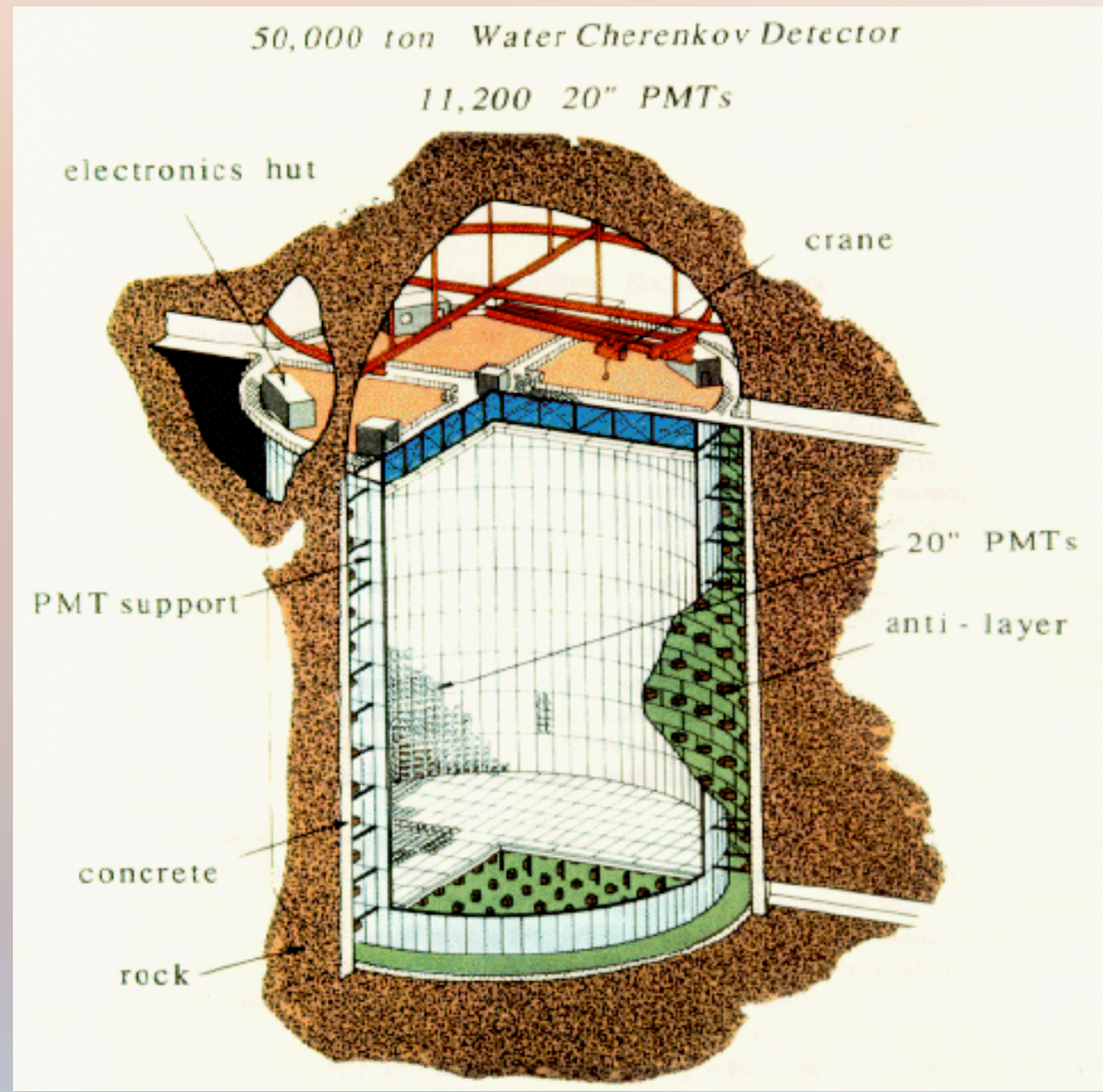


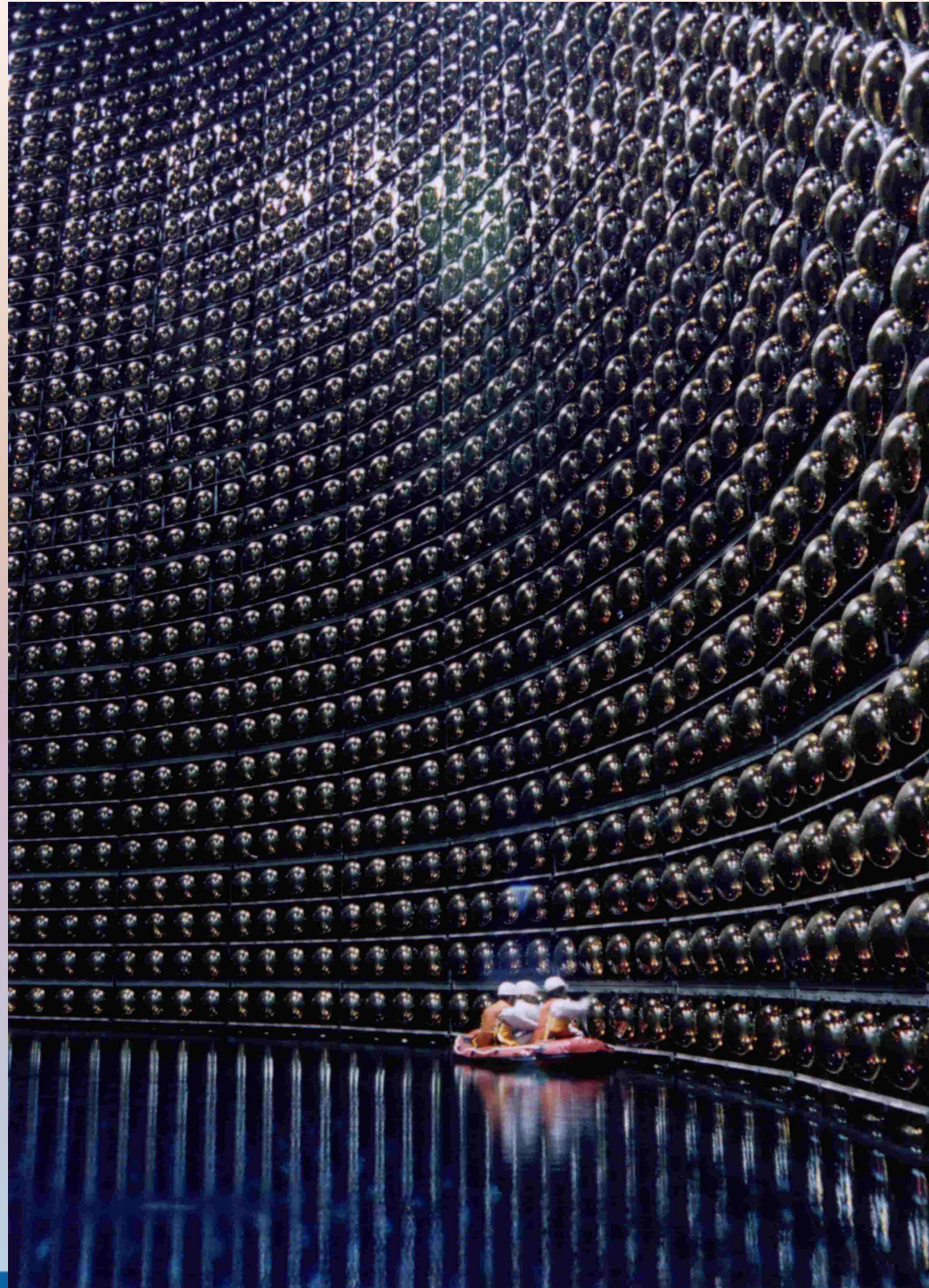
The SuperKamiokande (SK) experiment

Elastic scattering

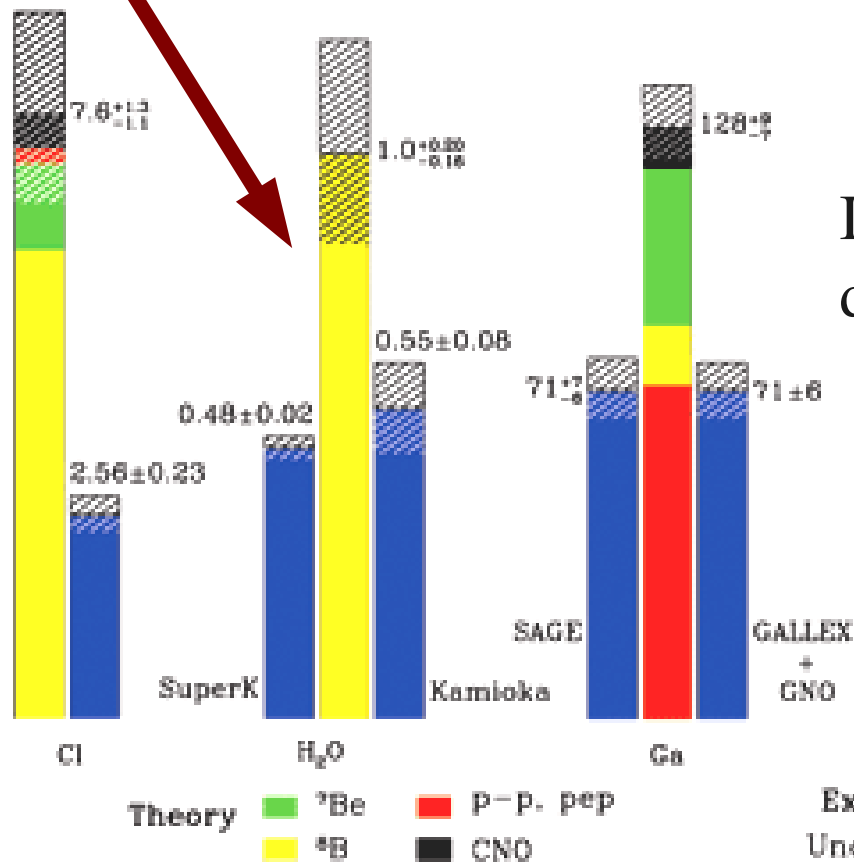
$$\nu + e \rightarrow \nu + e$$

Sensitive to all the ν ,
but in fact particularly
to ν_e



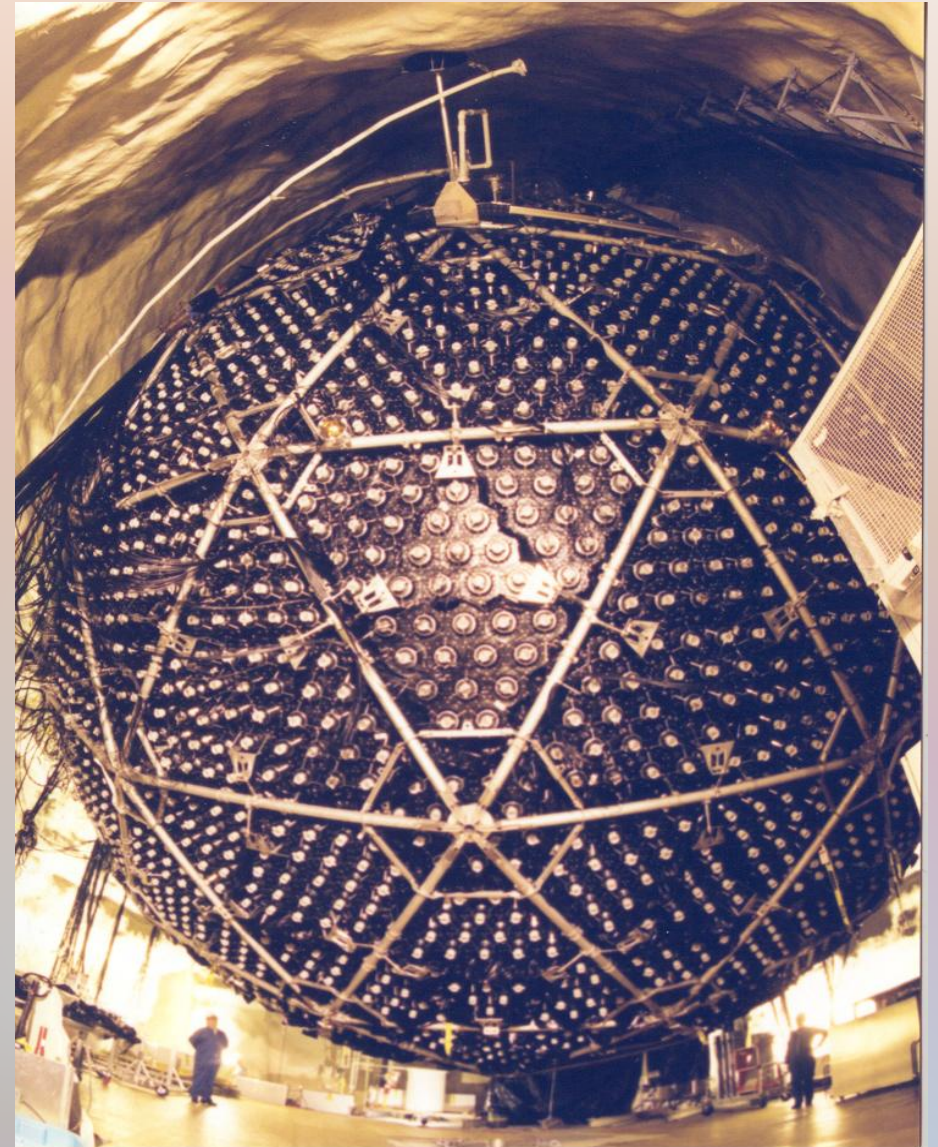
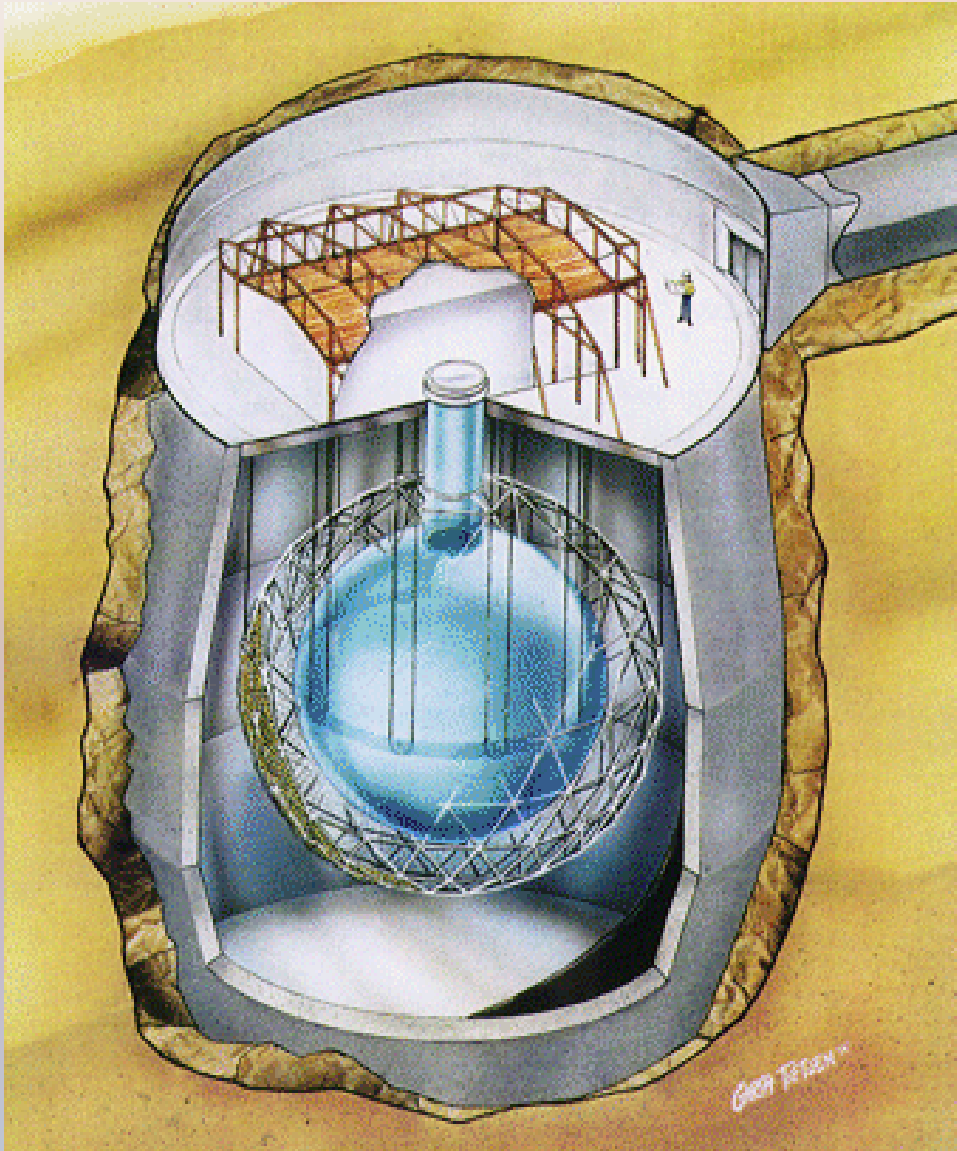


Total Rates: Standard Model vs. Experiment Bahcall-Pinsonneault 2000



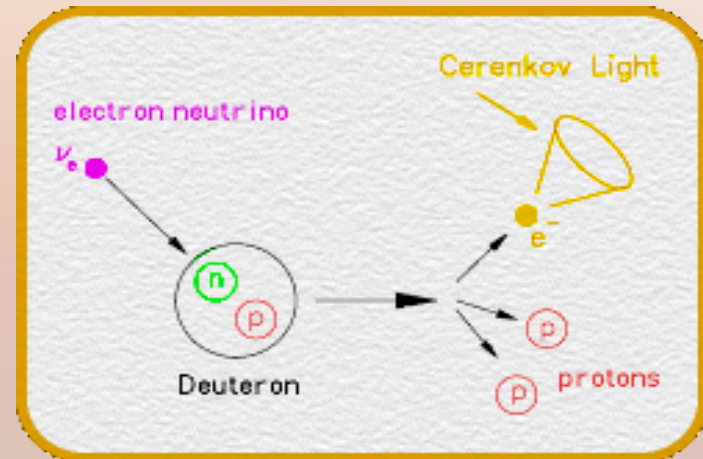
In 2001 big accident: SK detector half-destroyed!

The Sudbury Neutrino Observatory (SNO)

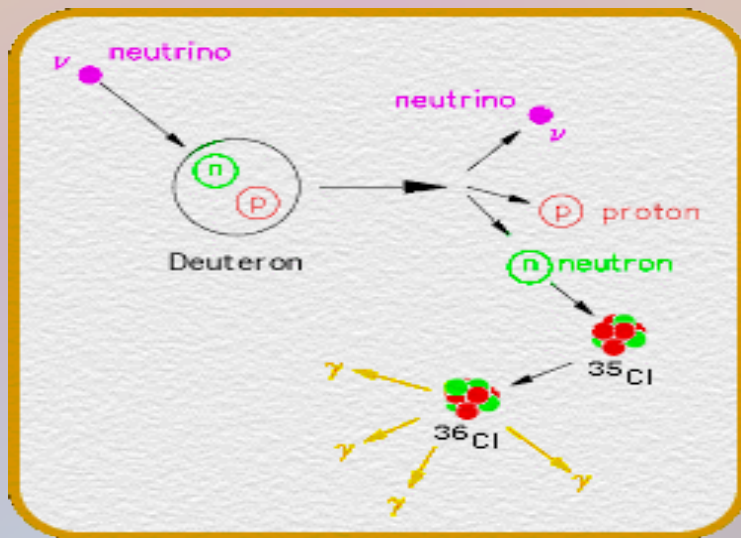


Neutrino interactions in D_2O

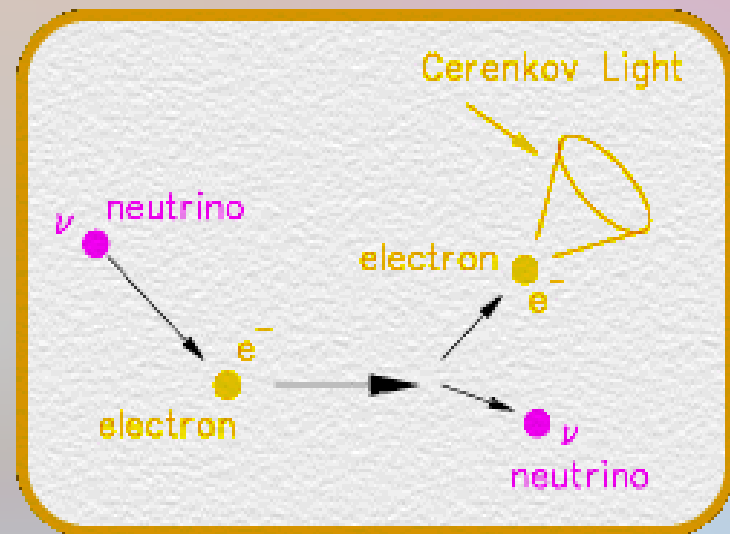
Charged Current Reaction (CC)



Neutral Current Reaction (NC)

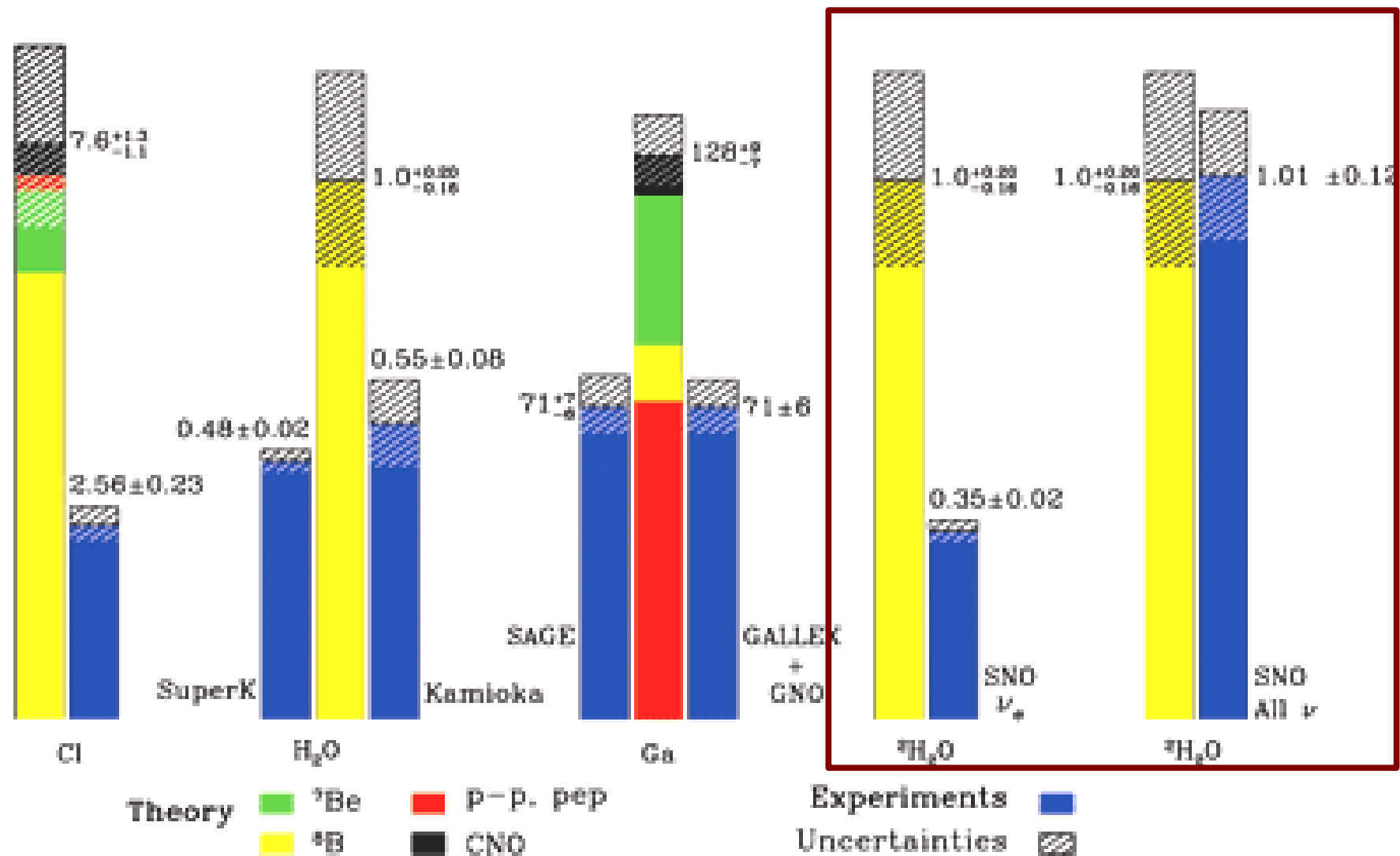


Elastic Scattering (ES)



Total Rates: Standard Model vs. Experiment

Bahcall-Pinsonneault 2000



Theoretical calculations: state-of-the-art

- 1) Realistic description of initial and final nuclear bound- and scattering states (*realistic Hamiltonians: two- and three-nucleon interactions*)
- 2) Realistic description of the electro-weak nuclear current (*one-body and meson-exchange currents*)

For both 1) and 2):

- **high accuracy**
- **widely tested especially in the electromagnetic sector (electron scattering)**

Marcucci *et al.*, Nucl. Phys. A **777**, 111 (2006)

Adelberger *et al.*, Rev. Mod. Phys. **83**, 195 (2011)

$$n + p \rightarrow d + \gamma$$

Total cross section [mb] with the AV18

One-body	304.6
Full	332.7
Expt.	332.6(7)

$$p + p \rightarrow d + e^+ + \nu_e$$

$$S(E) = E \sigma(E) \exp(2 \pi Z_1 Z_2 \alpha / v)$$

$$S(E) \approx \Lambda(E)^2$$

NN model	AV18	CD-Bonn
One-body	6.965	6.985
Full	7.076	7.060

H.A. Bethe and C.L. Critchfield, Phys. Rev. **54**, 248 (1938)

TABLE I. *Numerical results for two values of the radius.*

	$r_0 = e^2/mc^2$	$r_0 = e^2/2 mc^2$
x_0	0.645	0.322
V_0 (Mev)	20.9	66.5
D (Mev)	10.3	47.0
μ	2.94	5.45
ν	2.18	4.65
$(rd \log w/dr)$	0.236	0.110
$\Phi(r_0)$	1.050	1.025
$\Theta(r_0)$	0.769	0.854
$(rd \log \Phi/dr)$	0.050	0.025
ξ	0.814	0.915
λ	2.63	4.80
Λ_1	0.689	0.277
Λ_2	1.949	1.547
Λ_3	1.205	1.030
$(1+x_0)(1+\mu^{-2})$	1.835	1.367
Λ	2.84	2.44
Λ^2	8.08	5.93

¹³ Breit, Condon and Present, Phys. Rev. 50, 825 (1936).



Total cross section [mb] (AV18/UIX)

One-Body

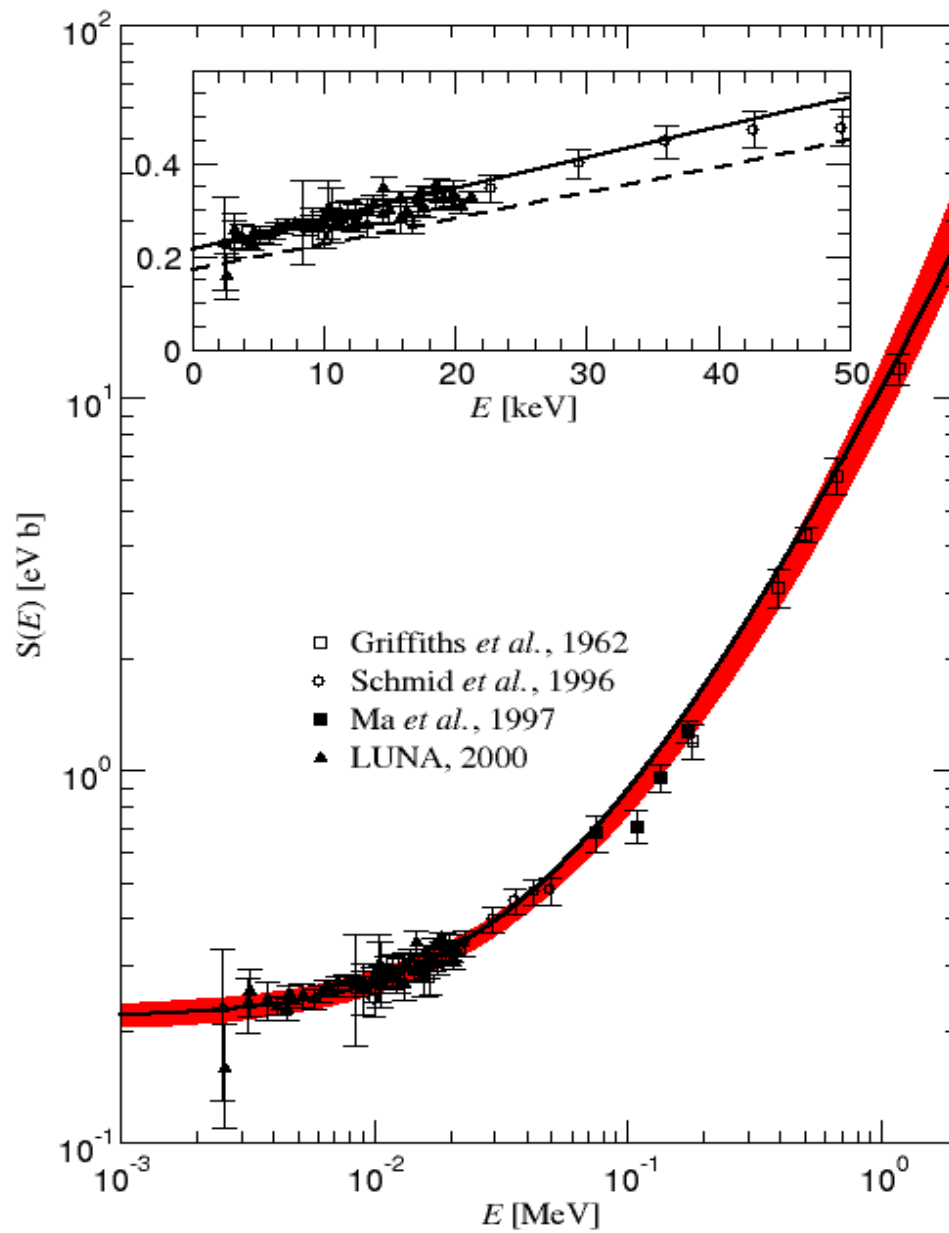
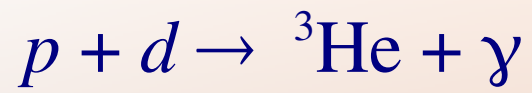
0.227

Full

0.556

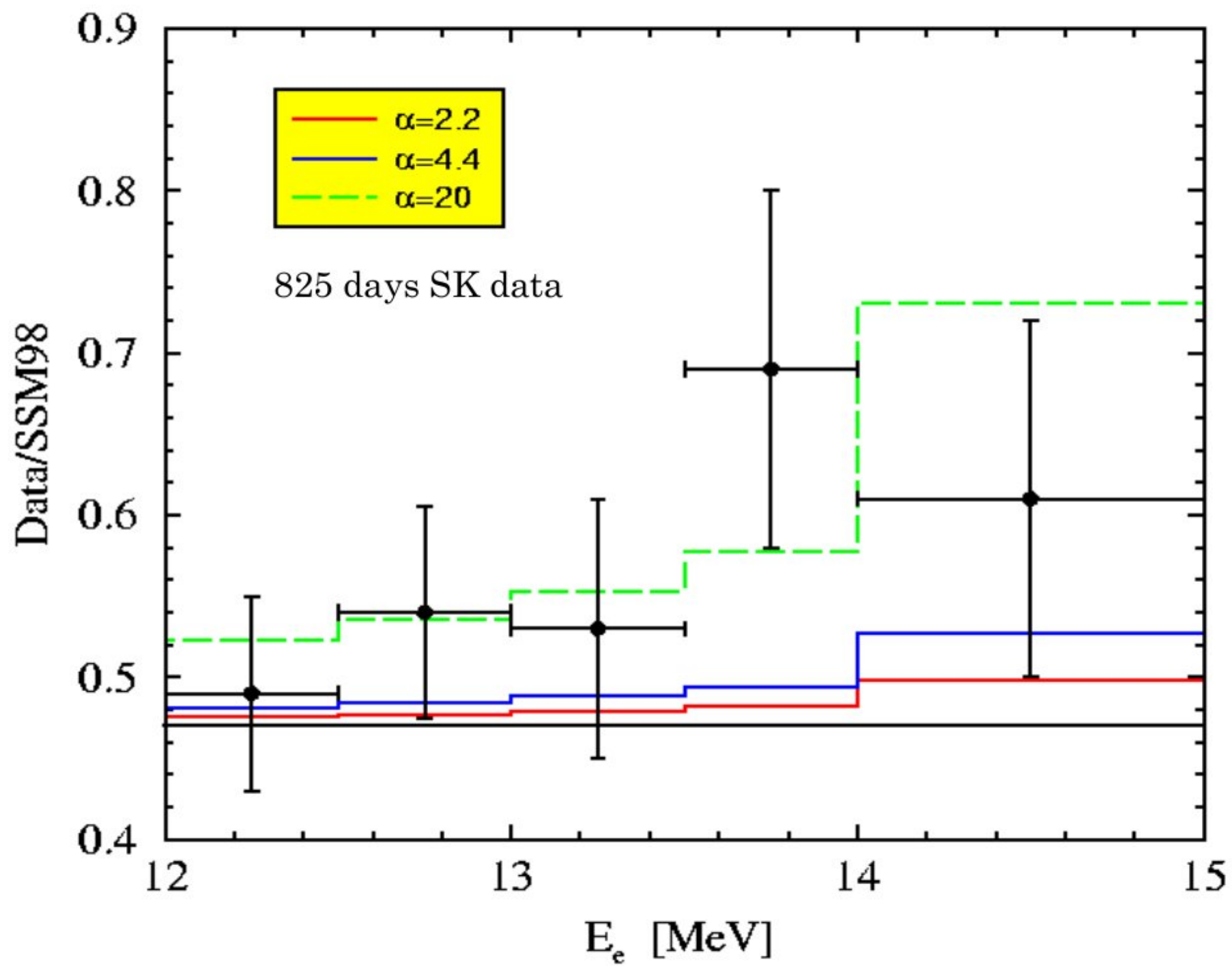
Expt.

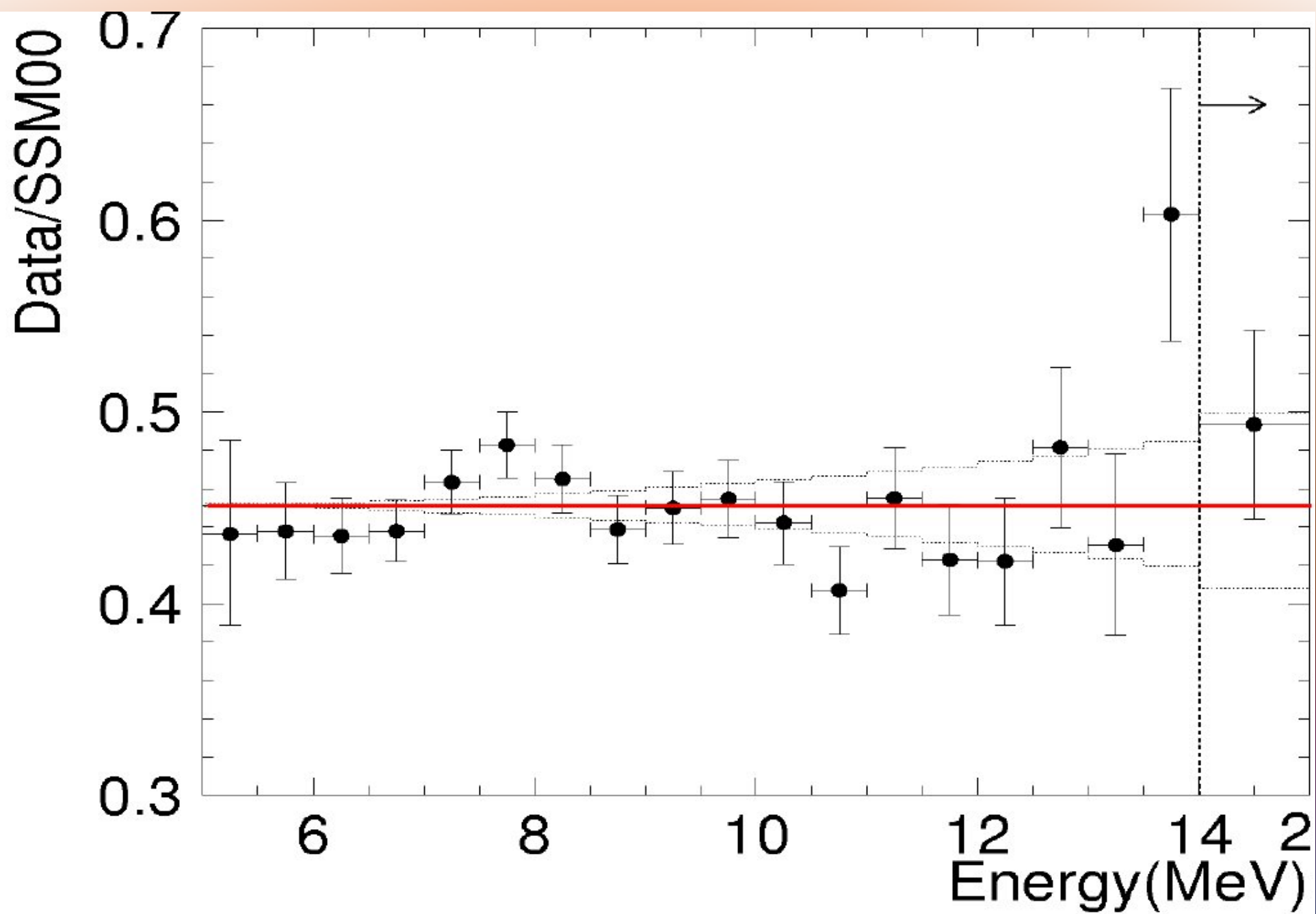
0.508(15)



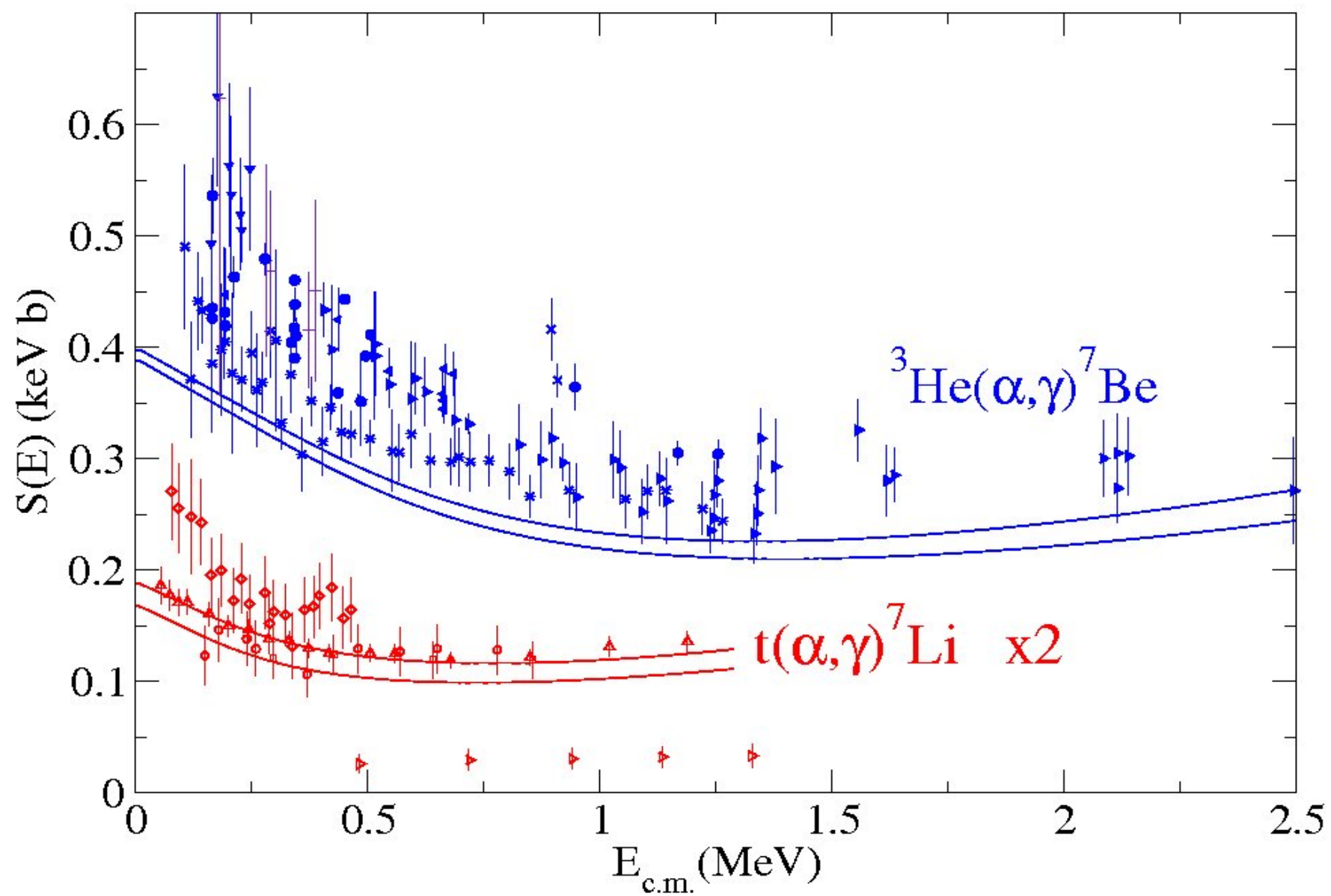
$p+{}^3\text{He} \rightarrow {}^4\text{He}+e^++\nu_e$: the hep reaction

- $S_{\text{SSM98}} = 2.3 \times 10^{-20} \text{ keV b}$
- New calculation (Marcucci *et al.*, PRL **84**, 5959 (2000); PRC **63**, 015801 (2001)):
 1. $S(10 \text{ keV}) = 10.1 \times 10^{-20} \text{ keV b}$
 2. no c.m. energy dependence
 3. no Hamiltonian model dependence (if H reproduces accurately the initial and final state w.f.'s)
 4. importance of the P-waves (40%)
 5. importance of MEC (Δ)
- SSM revisited (Bahcall *et al.*, Astr.J. **555**, 990 (2001)):
 $S_{\text{SSM00}} = 10.1 \times 10^{-20} \text{ keV b}$



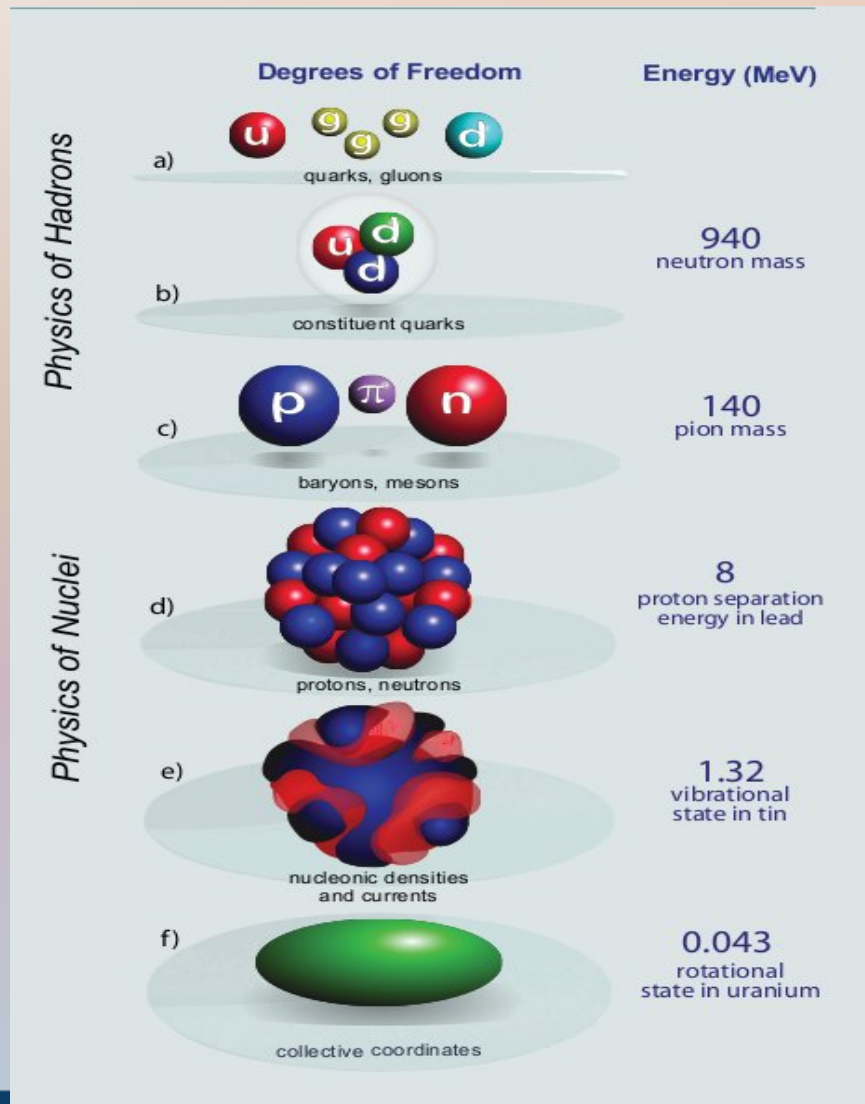


The SK collaboration, PRL **86**, 5651 (2001)



Limits

- No clear connection with QCD $\rightarrow$ model-dependence
- No clear determination of theoretical uncertainty



Chiral Effective Field Theory (χ EFT)

Chiral Effective Field Theory (χ EFT)

- QCD $\rightarrow$ quark and gluons (“heavy” degrees of freedom)
- Nuclear physics $\rightarrow$ nucleons and pions (“light” degrees of freedom)
- EFT $\rightarrow$ processes with $E \sim p \sim m_\pi \ll \Lambda_{\text{QCD}} \sim 1 \text{ GeV}$
 - ▶ “heavy” d.o.f. integrated out $\rightarrow$ contact interactions with “light” d.o.f. and low-energy constants (LECs) obtained from experiment
 - ▶ perturbative theory: matrix elements $\propto O(p/\Lambda_{\text{QCD}})^v$

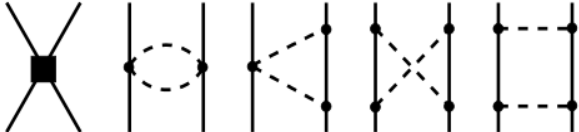
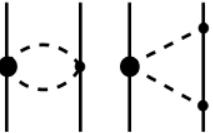
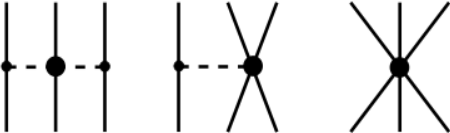
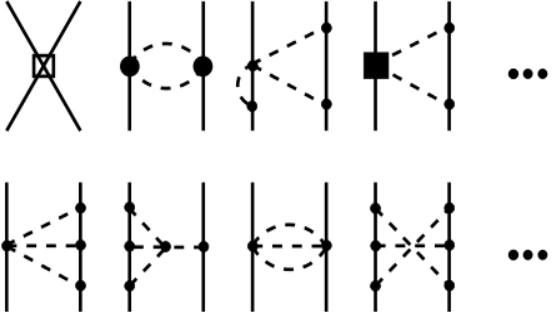
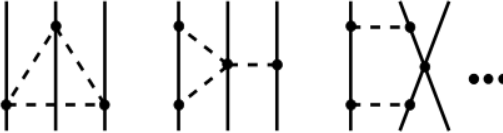
χ EFT $\rightarrow$ implement EFT and spontaneous breaking of QCD's chiral symmetry

Advantages: a) “right” treatment of π N interaction

b) nuclear force “hierarchy” $\rightarrow$ accurate $V_{\text{NN}} + V_{\text{NNN}}$

Disadvantage: limited to processes occurring at low-energy $E \sim 1\text{-}2 m_\pi$

Note: renormalization functions $\rightarrow$ Gaussians with cutoff Λ ($\sim 500\text{-}600 \text{ MeV}$)

	2N force	3N force	4N force
LO			
NLO			
N ² LO			
N ³ LO			

First steps (~ 2001): “hybrid” χ EFT

- Nuclear wave functions from realistic phenomenological potentials (AV18, etc)
- Nuclear electroweak current from χ EFT



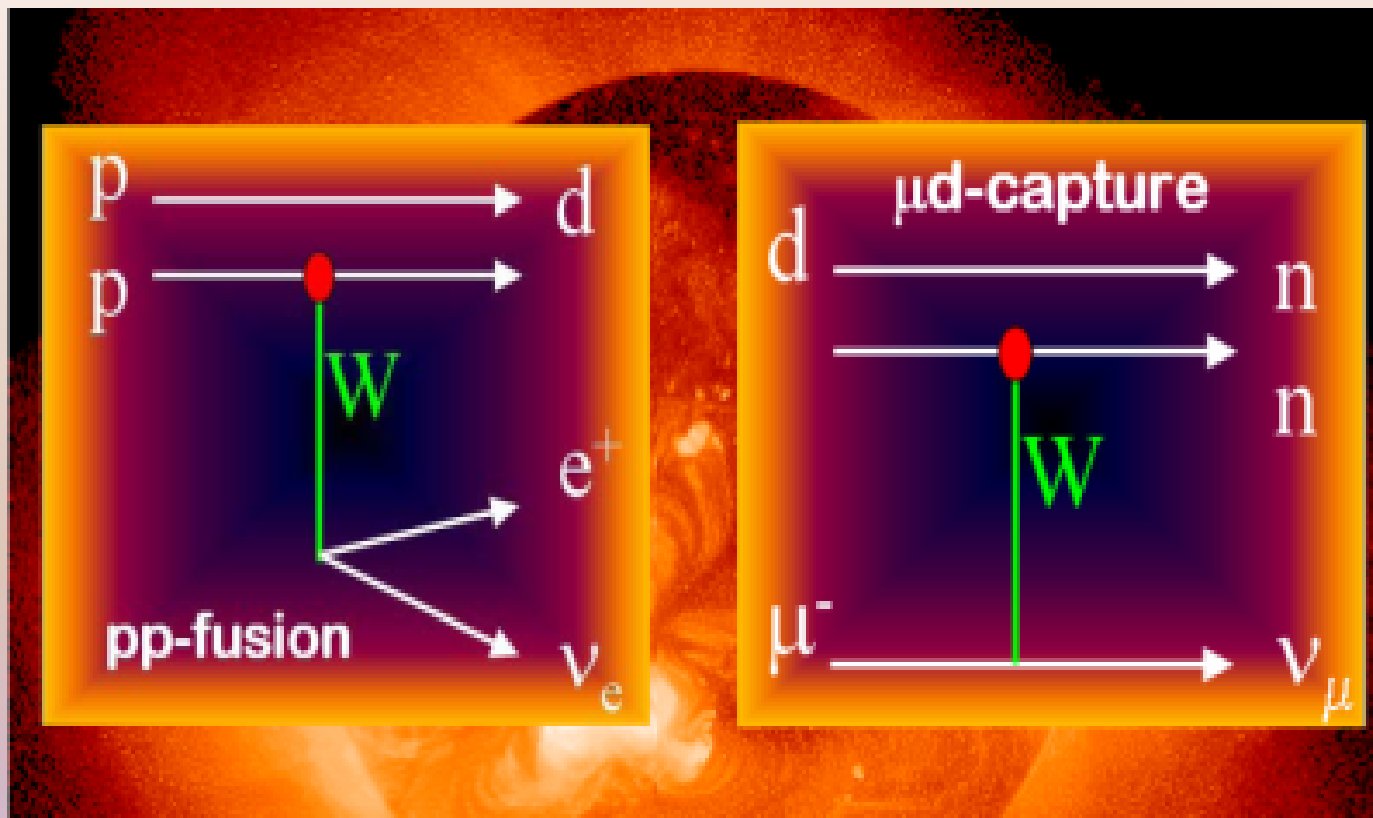
Study of the pp and hep reactions in agreement with “old” phenomenological ones

T.S. Park *et al.*, Phys. Rev. C **67**, 055206 (2003)

On-going work toward a fully consistent χ EFT calculation

Fully consistent χ EFT calculation

- Nuclear interactions and currents in χ EFT at N3LO (three-nucleon interaction at N2LO)
- First χ EFT calculation for $\mu^- + d \rightarrow n + n + \nu_\mu$ and $\mu^- + {}^3\text{He} \rightarrow {}^3\text{H} + \nu_\mu \rightarrow$ test of the framework
- First χ EFT calculation for $p + p \rightarrow d + e^+ + \nu_e$
- Future work for
 - $p + {}^3\text{He} \rightarrow {}^4\text{He} + e^+ + \nu_e$
 - $p + d \rightarrow {}^3\text{He} + \gamma$ (on-going)



Muon-captures: weak processes experimentally accessible

Results (with RC)

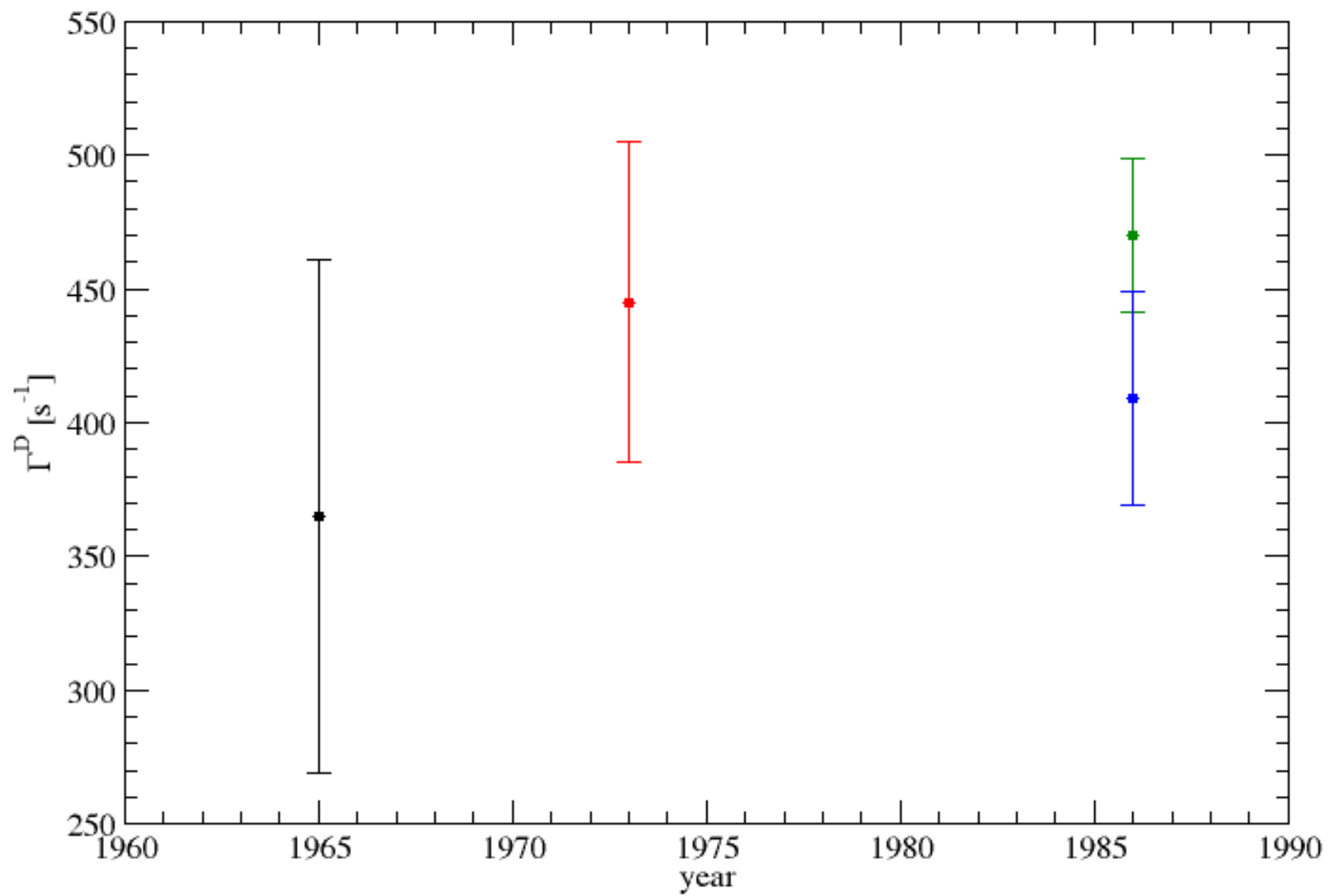
	1S_0	3P_0	3P_1	3P_2	Γ^D	Γ_0
IA – $\Lambda = 500$ MeV	238.8	21.1	44.0	72.4	381.7	1362
IA – $\Lambda = 600$ MeV	238.7	20.9	43.8	72.0	380.8	1360
FULL – $\Lambda = 500$ MeV	254.4(9)	20.5	46.8	72.1	399.2(9)	1488(9)
FULL – $\Lambda = 600$ MeV	255(1)	20.3	46.6	71.6	399(1)	1499(9)
χ EFT* – $\Lambda = 500$ MeV	251.5(7)	20.0	46.6	71.8	395.1(7)	1489(9)

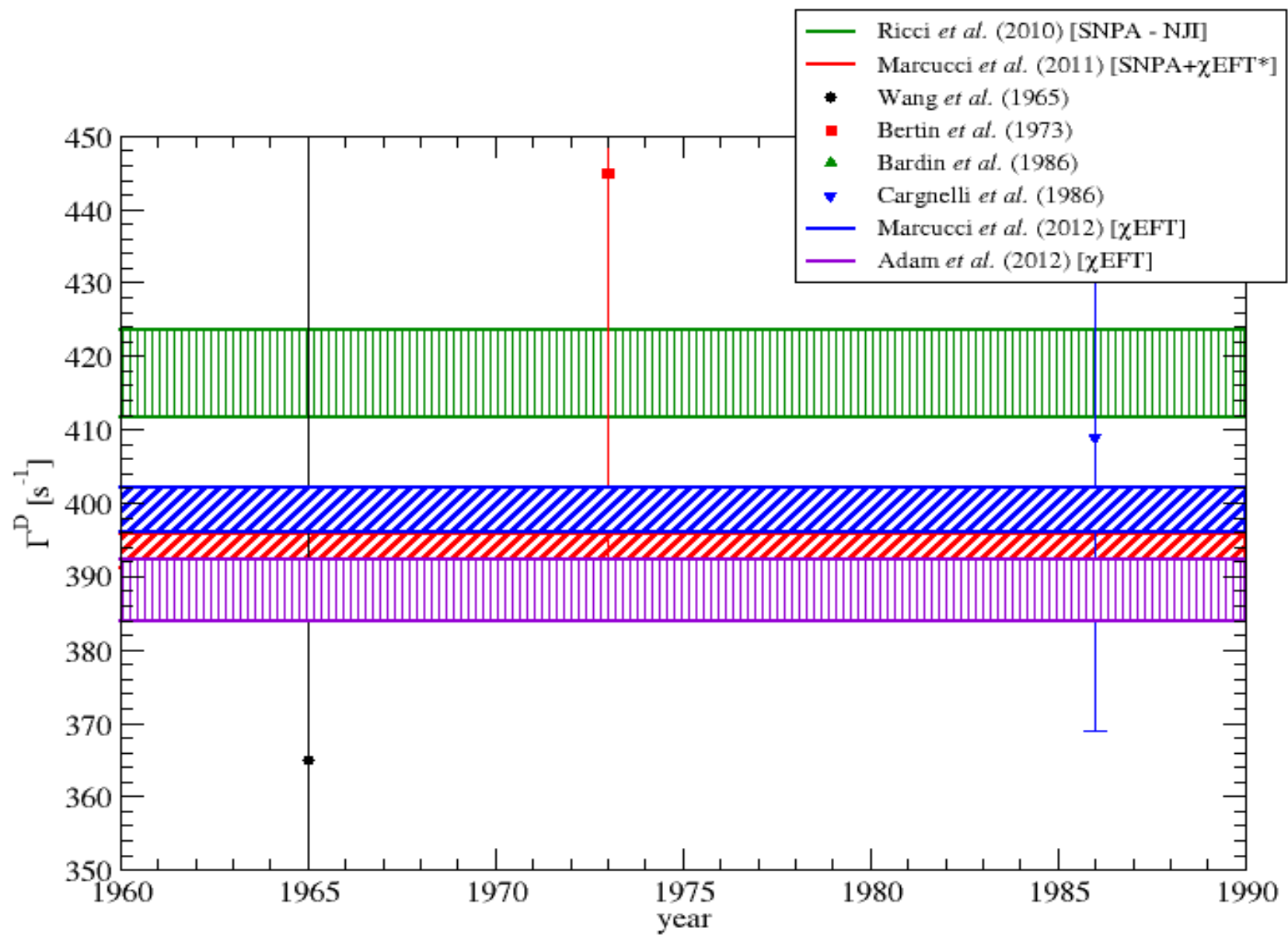
$$\Gamma^D = \mathbf{399(3)} \text{ s}^{-1} \text{ \& } \Gamma_0 = \mathbf{1494(21)} \text{ s}^{-1}$$

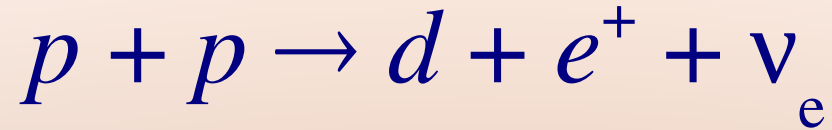
Marcucci *et al.*, PRL **108**, 052502 (2012)

$$\Gamma_0(\text{exp}) = 1496(4) \text{ s}^{-1}$$

$\Gamma^D(\text{exp})$

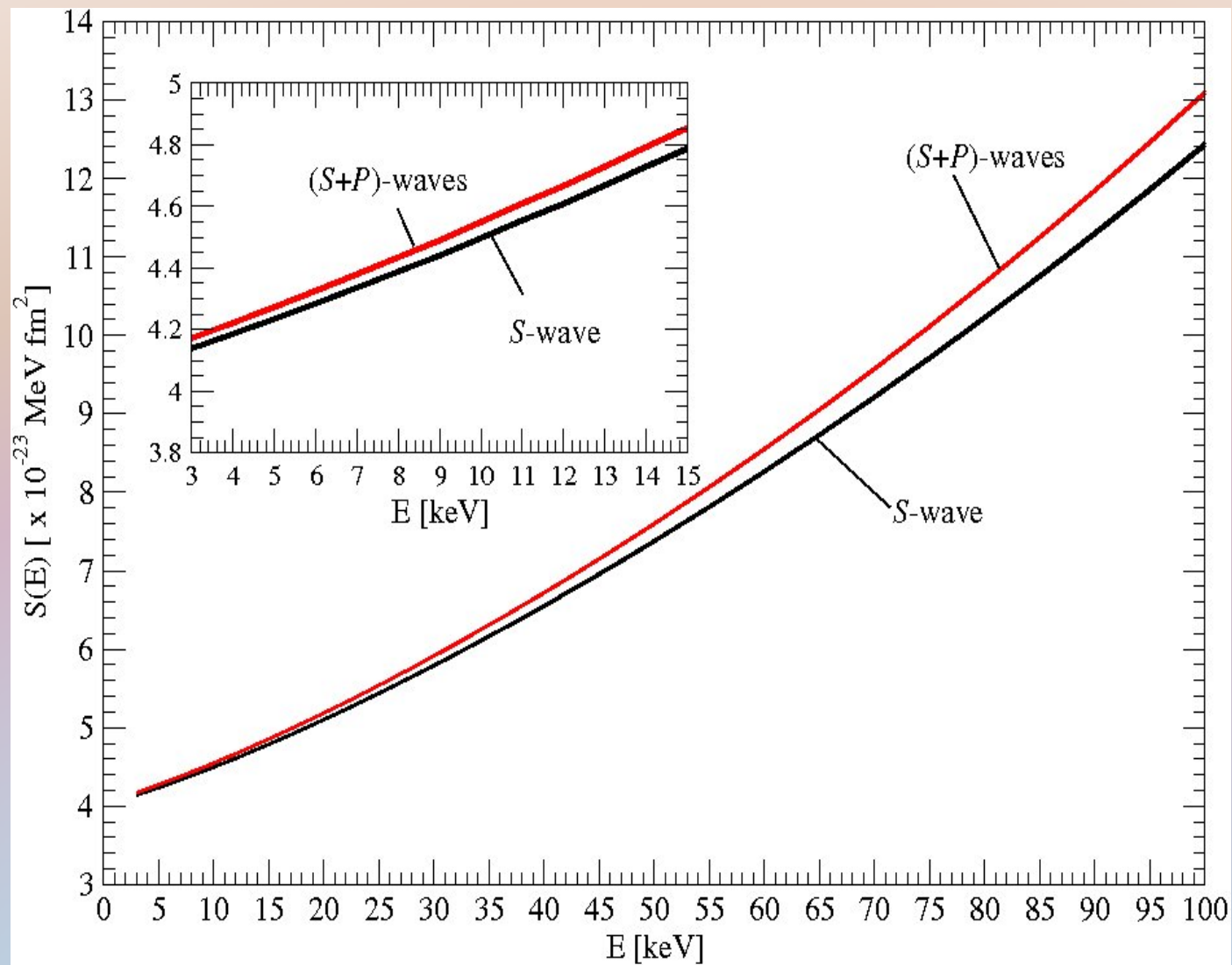






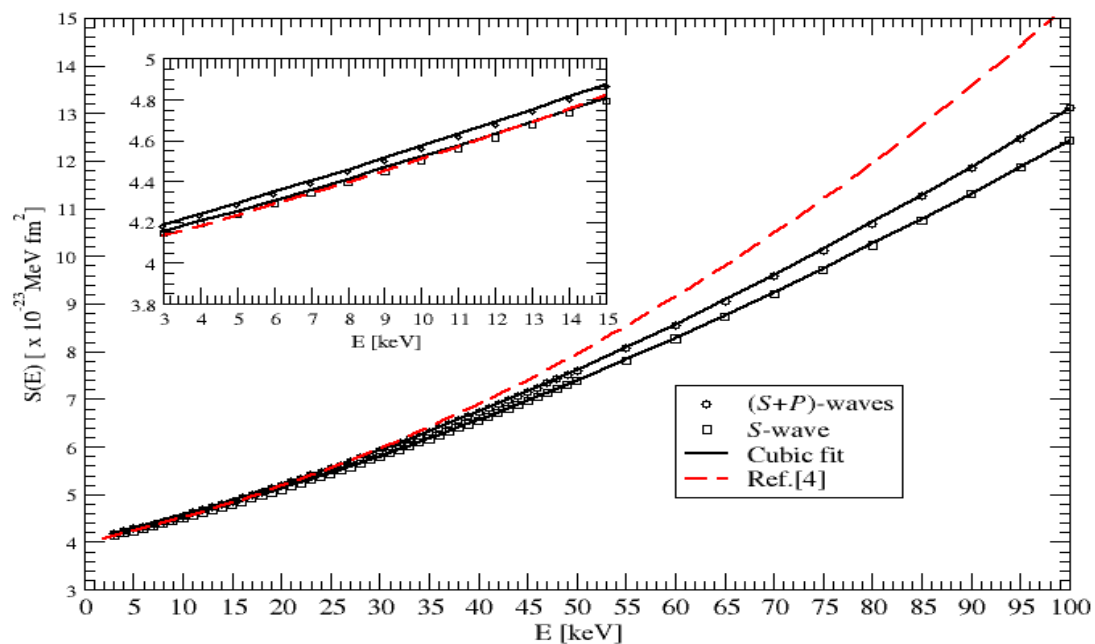
- χ EFT calculation between 0-100 keV (Gamow peak: Sun $E \sim 6$ keV; medium-mass stars $E \sim 15$ keV)
- S - and P -waves included
- “Old” values [Adelberger *et al.*, Rev. Mod. Phys. **83**, 195 (2011)]:
 $S(0) = (4.01 \pm 0.01) \times 10^{-23} \text{ MeV b}$
 $S'(0)/S(0) = (11.2 \pm 0.1) \text{ MeV}^{-1}$
 $S''(0)/S(0) \sim 1\% \text{ effect}$

	1S_0	3P_0	3P_1	3P_2
$\Lambda=500$ MeV	4.008(5)	4.011(5)	4.020(5)	4.030(5)
$\Lambda=600$ MeV	4.008(5)	4.010(5)	4.019(5)	4.029(5)

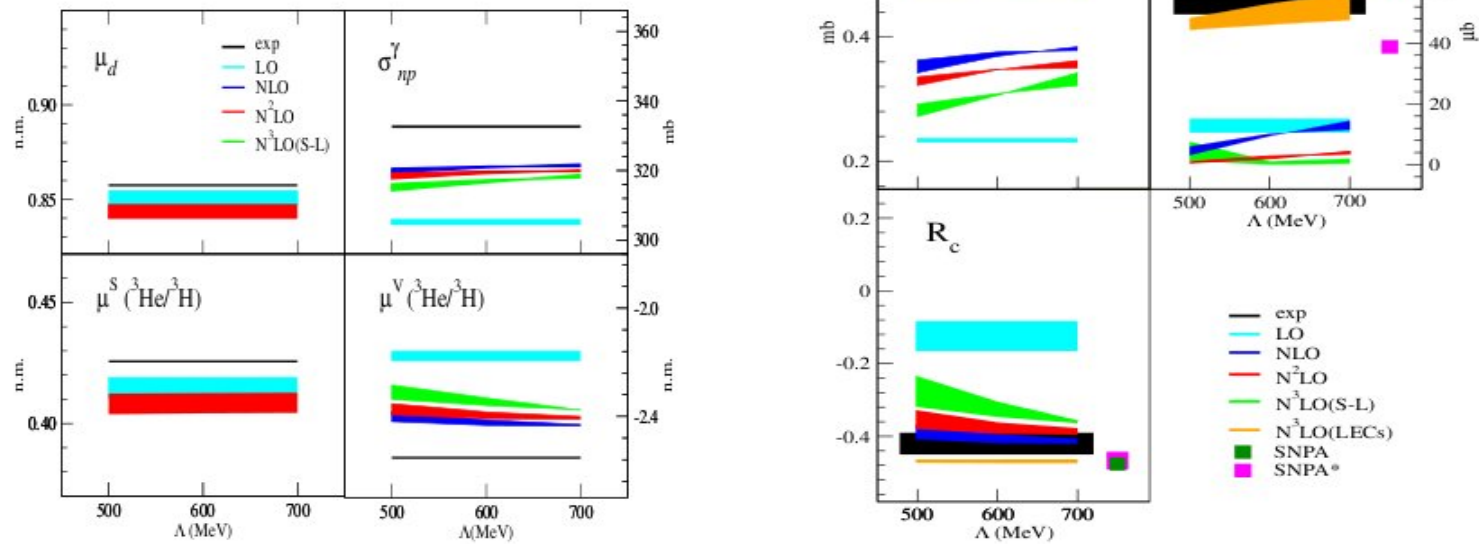


$S^n(0)/S(0)$
in MeV^{-n}

n	1	2	3	4	χ^2
Fit 1	12.59(1)	199.3(1)			8.8×10^{-4}
Fit 2	11.94(1)	248.8(2)	-1183(8)		1.9×10^{-4}
Fit 3	11.34(1)	327.1(5)	-5592(12)	99×10^3	2.0×10^{-5}
S-wave / old values	11.3(1)	170(2)			3.4×10^{-1}



$$n + d \rightarrow {}^3\text{H} + \gamma \text{ \& } n + {}^3\text{He} \rightarrow {}^4\text{He} + \gamma \text{ (\chi EFT*)}$$



Girlanda *et al.*, Phys. Rev. Lett. **105**, 232502 (2010)